

# **Clustering and its observation in unstable nuclei**

**Yanlin Ye**

**School of Physics and State Key Lab. of  
Nucl. Phys.&Tech. Peking University**

**CUSTIPEN Workshop, 2014.08.11, PKU**

# Outline

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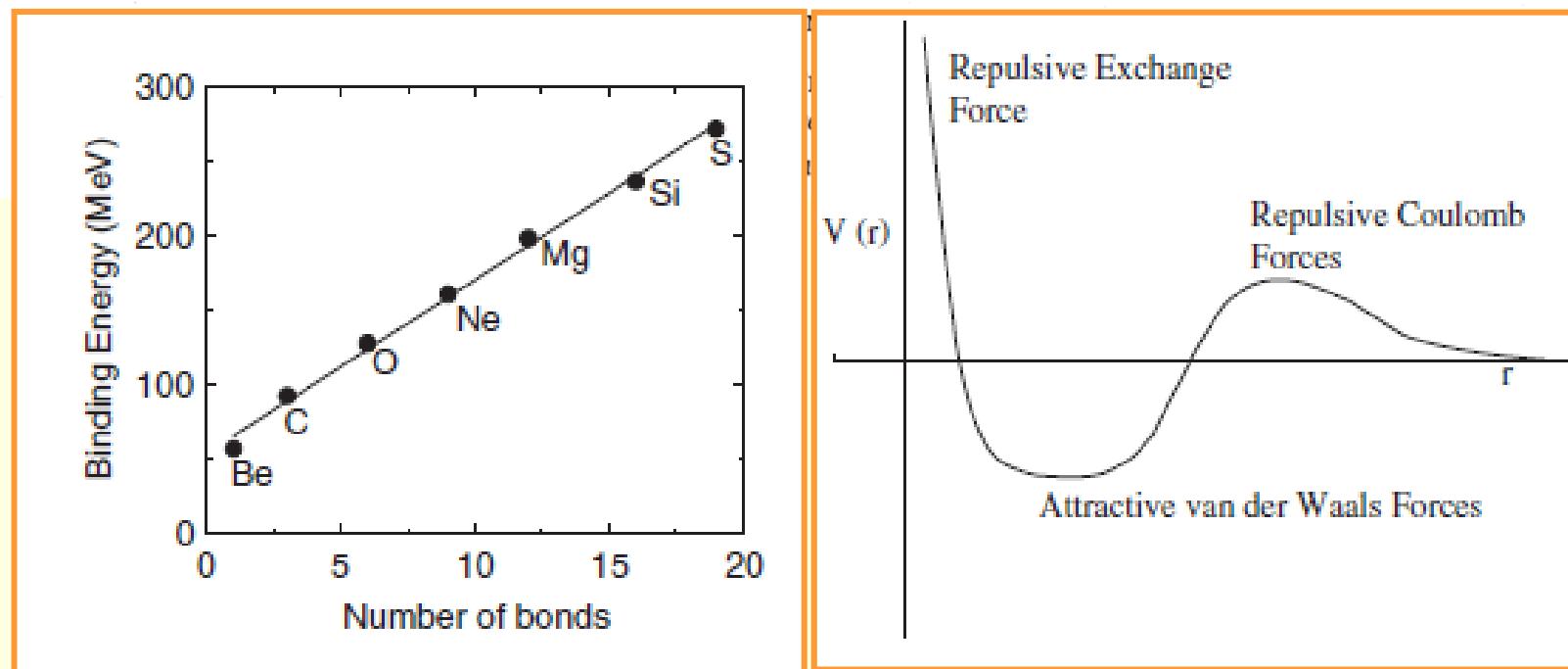
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- I. Historical background
- II. How to observe
- III.  $^{12}\text{Be}$  — an example
- IV. Future perspectives

## The Alpha-Particle Model of the Nucleus

L. R. HAFSTAD

*Department of Terrestrial Magnetism, Carnegie Institution of Washington, Washington, D. C.*



alternating independent-particle and clustering structure — a unique feature of nuclear many-body system.

*Letters to the Editor*

**Interaction between Alpha Particles**

Ichirô Shimodaya, Ryozo Tamagaki  
and Hajime Tanaka

*Department of Physics  
Hokkaido University  
Sapporo*

February 18, 1961

treme tightness. In this note, by applying the pion-theoretical potentials recently verified in two-nucleon problems,<sup>2)</sup> interactions between  $\alpha$ -particles are investigated from the viewpoint of the cluster model, without taking account of the polarization effects of  $\alpha$ -particles.

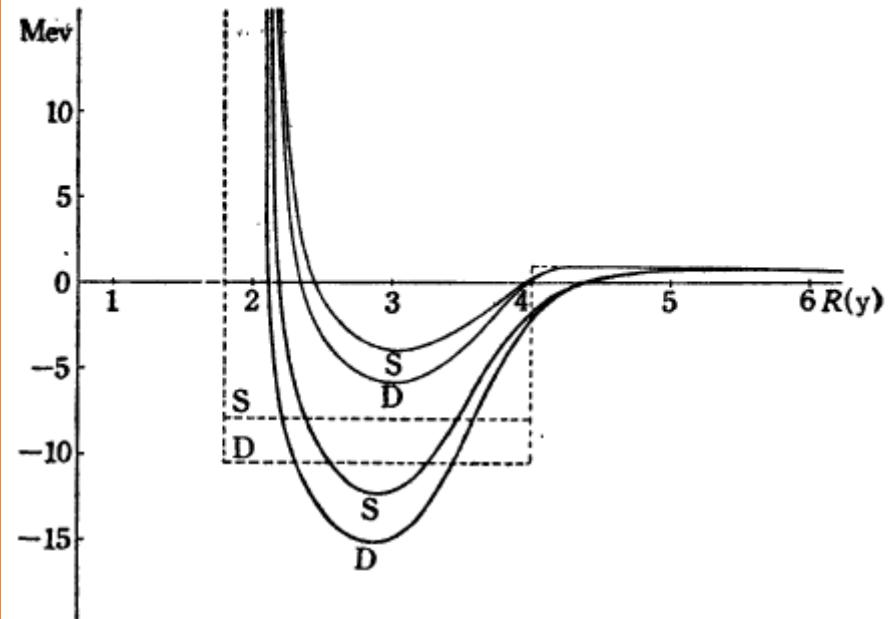
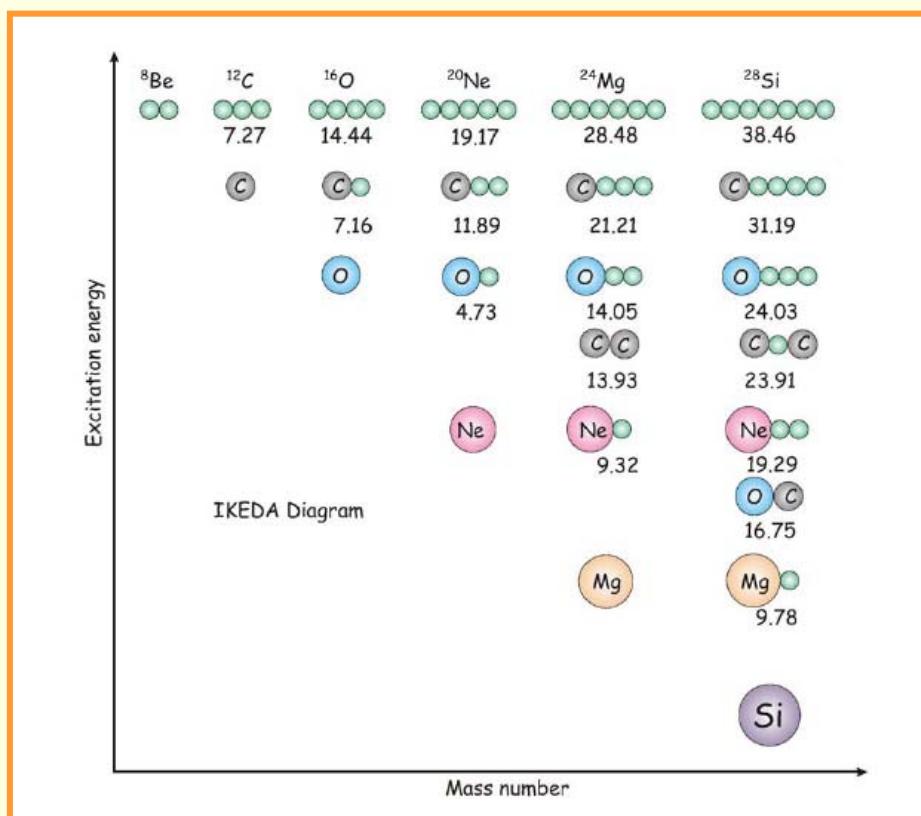


Fig. 1. The dashed lines represent the phenomenologically determined  $\alpha$ - $\alpha$  interactions for S- and D-states.<sup>3)</sup> The upper curves are obtained from the potential with an attractive TPEP only in the singlet even state and the lower curves from the potential with an additional attractive TPEP in the triplet even and triplet odd states.

## The Systematic Structure-Change into the Molecule-like Structures in the Self-Conjugate $4n$ Nuclei

Kiyomi IKEDA,\*<sup>†</sup> Noboru TAKIGAWA and Hisashi HORIUCHI

*Department of Physics, University of Tokyo, Tokyo*

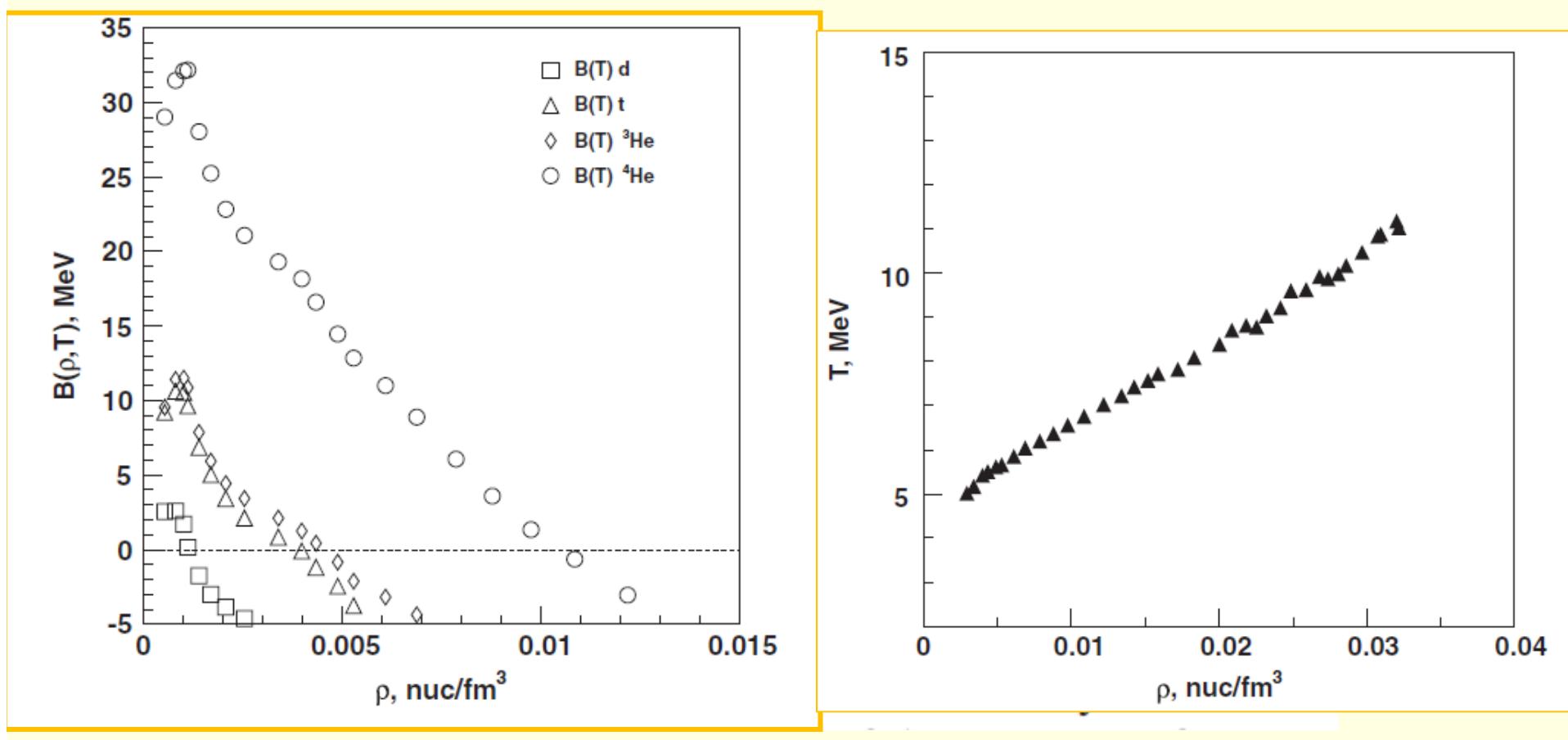


Idea of the  
relative tightness  
of a cluster  
inside a nucleus

## Experimental Determination of In-Medium Cluster Binding Energies and Mott Points in Nuclear Matter

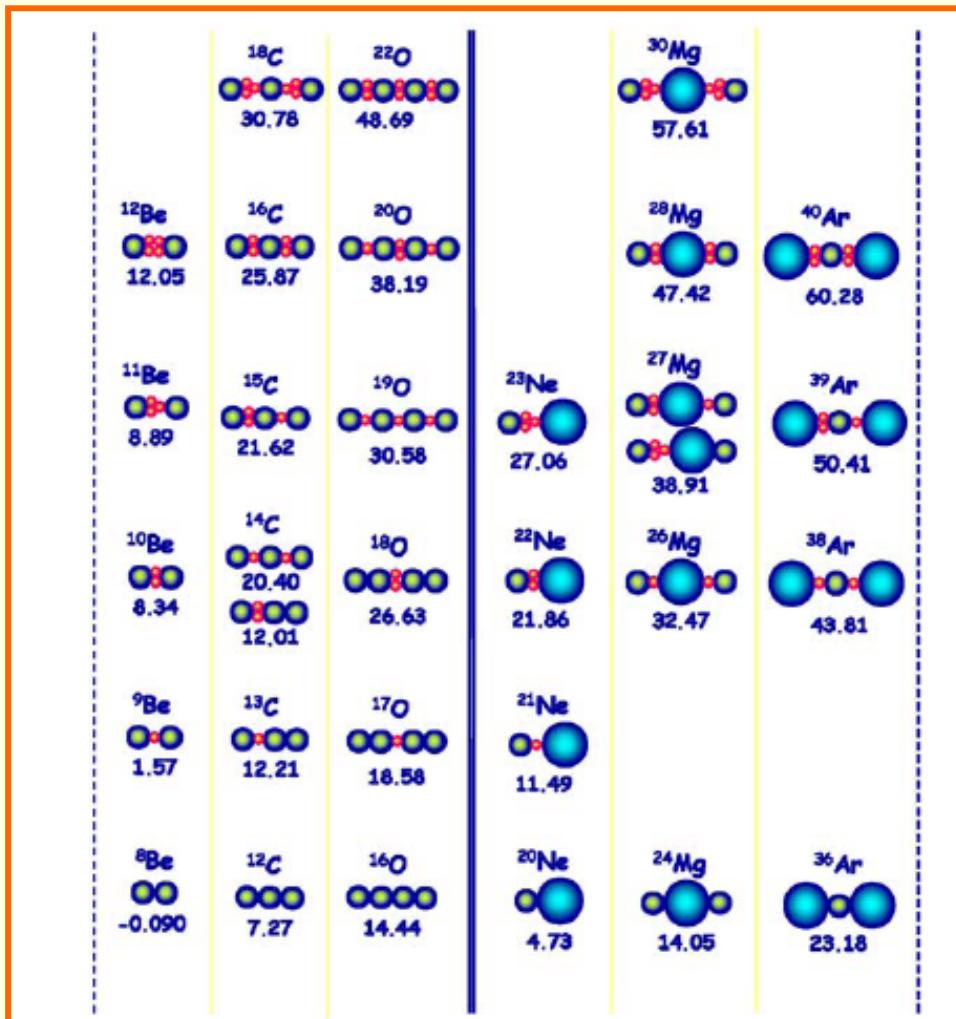
K. Hagel,<sup>1</sup> R. Wada,<sup>2,1</sup> L. Qin,<sup>1</sup> J. B. Natowitz,<sup>1</sup> S. Shlomo,<sup>1</sup> A. Bonasera,<sup>1,3</sup> G. Röpke,<sup>4</sup> S. Typel,<sup>5</sup> Z. Chen,<sup>2</sup> M. Huang,<sup>2</sup> J. Wang,<sup>2</sup> H. Zheng,<sup>1</sup> S. Kowalski,<sup>6</sup> C. Bottosso,<sup>1</sup> M. Barbui,<sup>1</sup> M. R. D. Rodrigues,<sup>1</sup> K. Schmidt,<sup>1</sup> D. Fabris,<sup>7</sup> M. Lunardon,<sup>7</sup> S. Moretto,<sup>7</sup> G. Nebbia,<sup>7</sup> S. Pesente,<sup>7</sup> V. Rizzi,<sup>7</sup> G. Viesti,<sup>7</sup> M. Cinausero,<sup>8</sup>  
G. Prete,<sup>8</sup> T. Keutgen,<sup>9</sup> Y. El Masri,<sup>9</sup> and Z. Majka<sup>10</sup>

<sup>1</sup>Cyclotron Institute, Texas A&M University, College Station, Texas 77843, USA



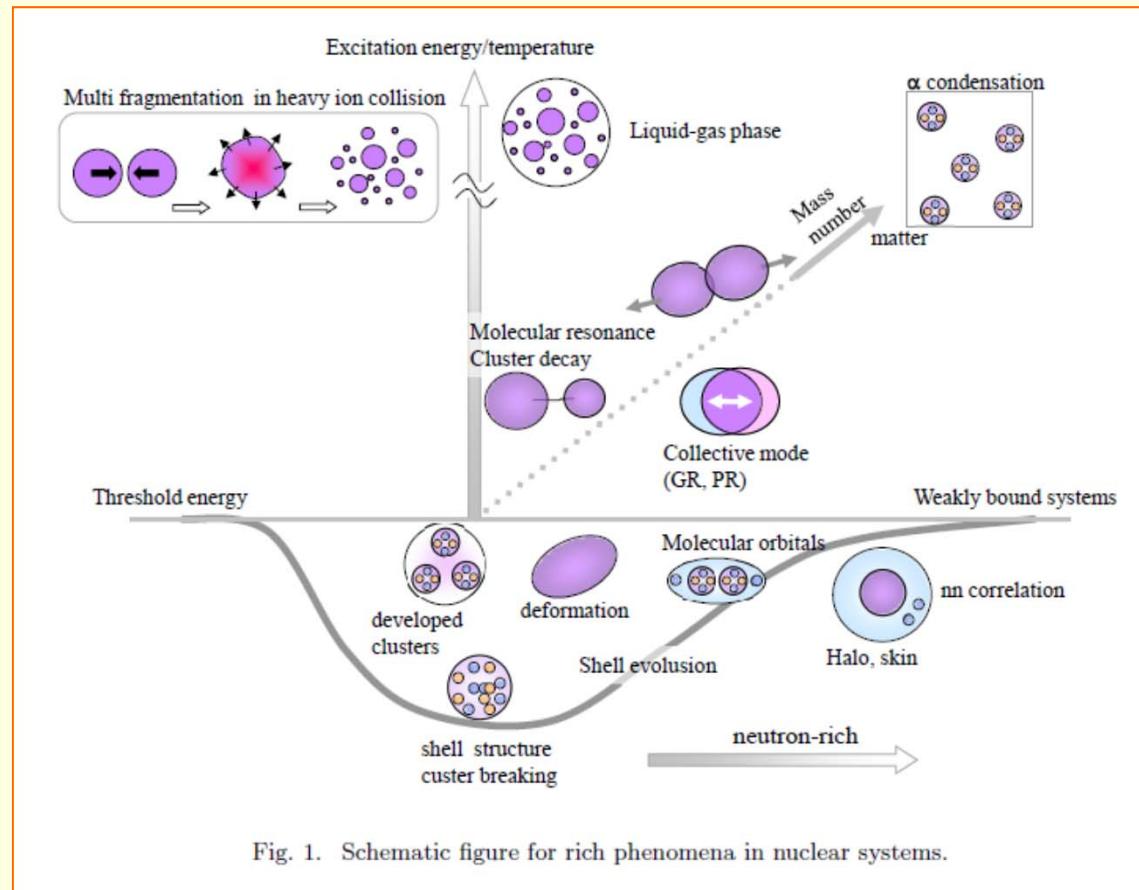
# for unstable nuclei

Physics Reports 432 (2006) 43–113



**Unstable nuclei:  
much more cluster  
configurations  
(and thresholds)  
within a small  $E_x$   
interval.  
— richness of  
nuclear clustering**

# PTEP,2012,01A202



# Recent progress

Progress of Theoretical Physics Supplement No. 192, 2012

## Recent Developments in Nuclear Cluster Physics

Hisashi HORIUCHI,<sup>1,2</sup> Kiyomi IKEDA<sup>3</sup> and Kiyoshi KATŌ<sup>4</sup>

**Theory:AMD, GCM(RGM), MO, GTGM, FMD,  
TCSM, TCHO(DHO), ...**

### Experiment:

$0^+_2$  (7.65 MeV) state in  $^{12}\text{C}$ ,

$0^+_2$  (6.05 MeV) and  $0^+_3$  (12.05 MeV) in  $^{16}\text{O}$ ;

$0^+_4$  (8.03 MeV) in  $^{20}\text{Ne}$

.....

AMD

## Fragment Formation Studied with Antisymmetrized Version of Molecular Dynamics with Two-Nucleon Collisions

A. Ono, H. Horiuchi, T. Maruyama, and A. Ohnishi

*Department of Physics, Kyoto University, Kyoto 606, Japan*

(Received 27 December 1991)

reaction process. The antisymmetrized version of molecular dynamics [3–5], which Feldmeier called fermionic molecular dynamics, treats explicitly the wave function of the total system and hence is able to describe quantum-mechanical effects such as shell effects. However, until now the two-nucleon collision process has not been incorporated into the framework, which has made this framework insufficient for the description of fragment formation.

The present authors have succeeded in incorporating two-nucleon collisions into the antisymmetrized version of molecular dynamics. This means the construction of a new microscopic simulation framework of the heavy-ion reaction. Hereafter we call this new simulation framework simply AMD. The aims of this paper are first to ex-

$$|\Phi(Z)\rangle = \frac{1}{\sqrt{A!}} \det[\varphi_i(j)], \quad \varphi_i = \phi_{Z_i} \chi_{a_i},$$

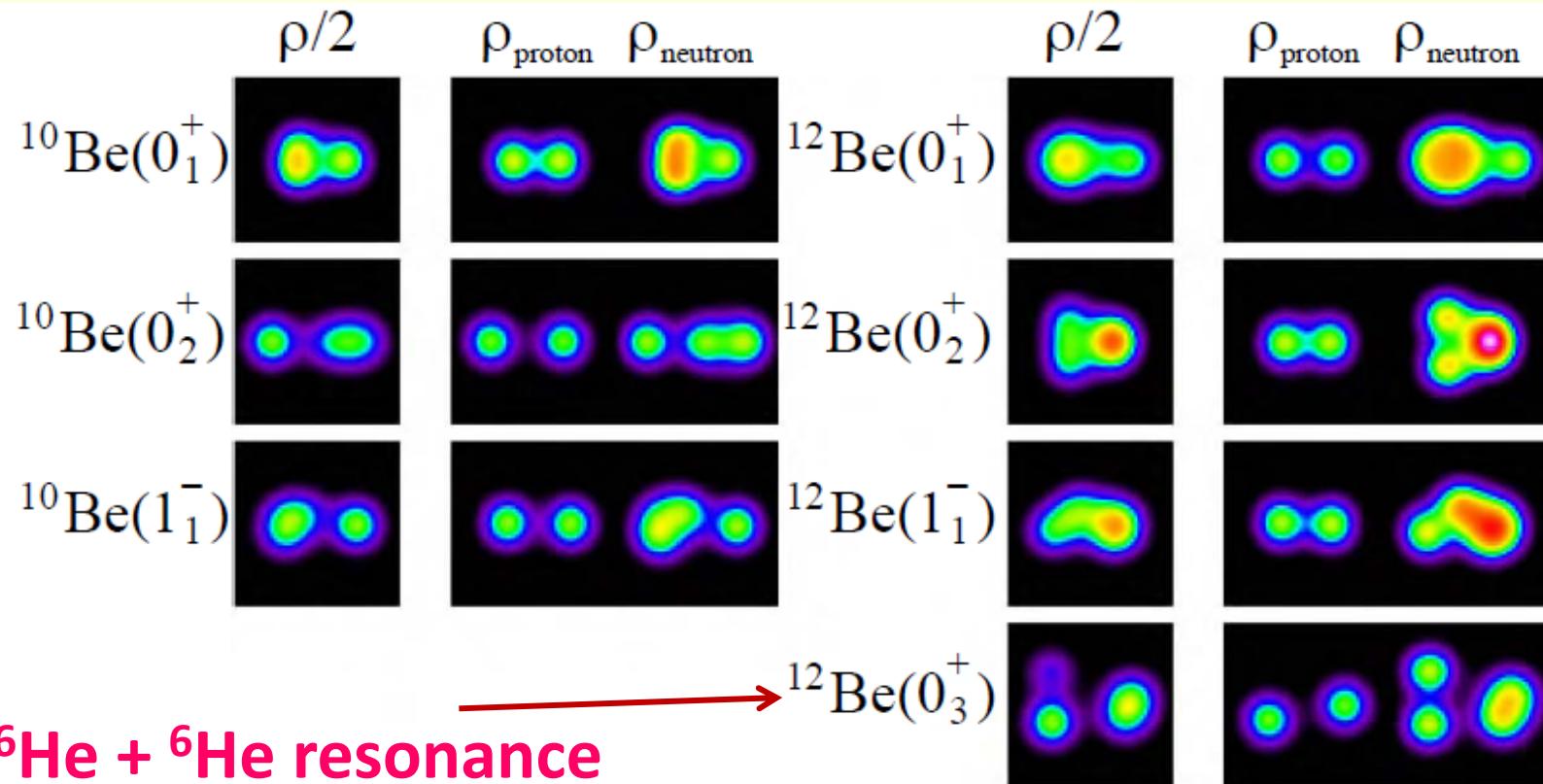
$$\mathcal{H} = \langle H \rangle - T_0 A + \bar{T}'_0 (A - \bar{N}_F).$$

**Cluster structures of the ground and excited states of  $^{12}\text{Be}$  studied with antisymmetrized molecular dynamics**

Y. Kanada-En'yo

*Institute of Particle and Nuclear Studies, High Energy Accelerator Research Organization, Ibaraki 305-0801, Japan*

H. Horiuchi

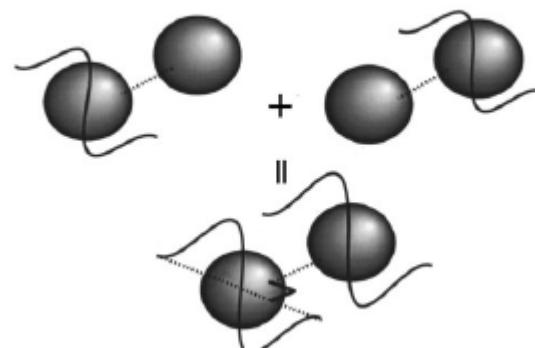
*Department of Physics, Kyoto University, Kyoto 606-8502, Japan* **$^{6}\text{He} + ^{6}\text{He}$  resonance**

## Molecular orbital structures in $^{10}\text{Be}$

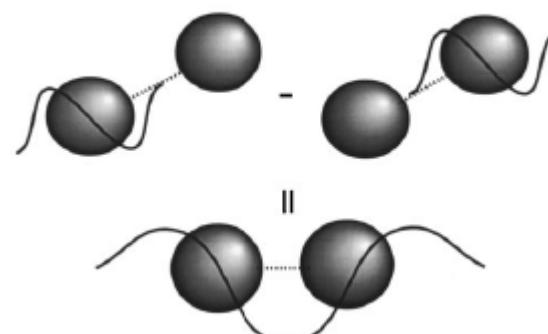
N. Itagaki<sup>1,\*</sup> and S. Okabe<sup>2</sup>

<sup>1</sup>*Graduate School of Science, Hokkaido University, Sapporo 060-0810, Japan*

(a)  $\pi$ -orbit One node



(b)  $\sigma$ -orbit Two nodes



# Application of the generalized two-center cluster model to $^{10}\text{Be}$

M. Ito<sup>a</sup>, K. Kato<sup>b</sup>, K. Ikeda<sup>c</sup>

<sup>a</sup> Institute of Physics, University of Tsukuba, 305-8571 Tsukuba, Japan

<sup>b</sup> Division of Physics, Graduate School of Science, Hokkaido University, 060-0810 Sapporo, Japan

<sup>c</sup> RI Beam Science Laboratory, RIKEN (The institute of Physical and chemical Research), Wako 351-0198, Saitama, Japan

## Using atomic orbitals as basis.

$$\begin{aligned}\Psi^{J^\pi}(^{10}\text{Be}) &= \int dS \sum_K \Phi_K^{J^\pi}(^{10}\text{Be}; S) \\ &= \int dS \sum_{K\beta} C_\beta^{J^\pi K}(S) \Phi_K^{J^\pi}(S),\end{aligned}$$

$$\begin{aligned}\Phi_K^{J^\pi}(^{10}\text{Be}; S) &= \hat{P}_K^J \mathcal{A} \left\{ \psi_L(\alpha) \psi_R(\alpha) \sum_m d_m^{J^\pi K} \varphi(m) \right. \\ &\quad \times \left. \sum_n d_n^{J^\pi K} \varphi(n) \right\} \\ &= \sum_{m,n} C_{m,n}^{J^\pi K}(S) \Phi_{m,n}^{J^\pi K}(S), \\ \Phi_{m,n}^{J^\pi K}(S) &= \hat{P}_K^J \mathcal{A} \{ \psi_L(\alpha) \psi_R(\alpha) \varphi(m) \varphi(n) \} \\ &\equiv \hat{P}_K^J \hat{\Phi}_{m,n}^{J^\pi}(^{10}\text{Be}; S),\end{aligned}$$

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# observables for determining the cluster formation in a resonant state

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i)  $E_x$  - spin systematics:

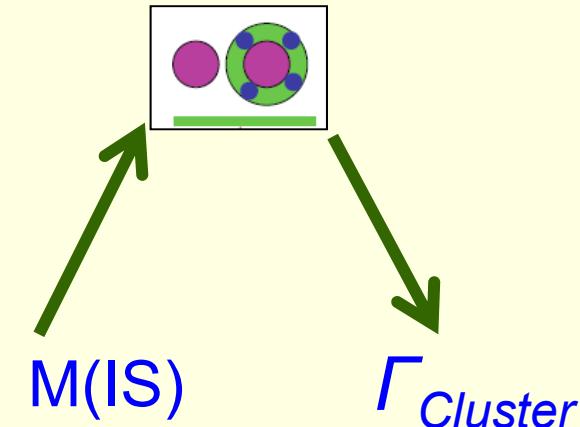
high moment of inertia

ii) Large cluster decay width:

large  $\Gamma_{Cluster}/\Gamma$ ;  $\gamma^2_{Cluster}$ ;  $\theta^2_{Cluster}$

iii) Characteristic transition strength

large M(IS) !!



# i) Determination of the moment of inertia

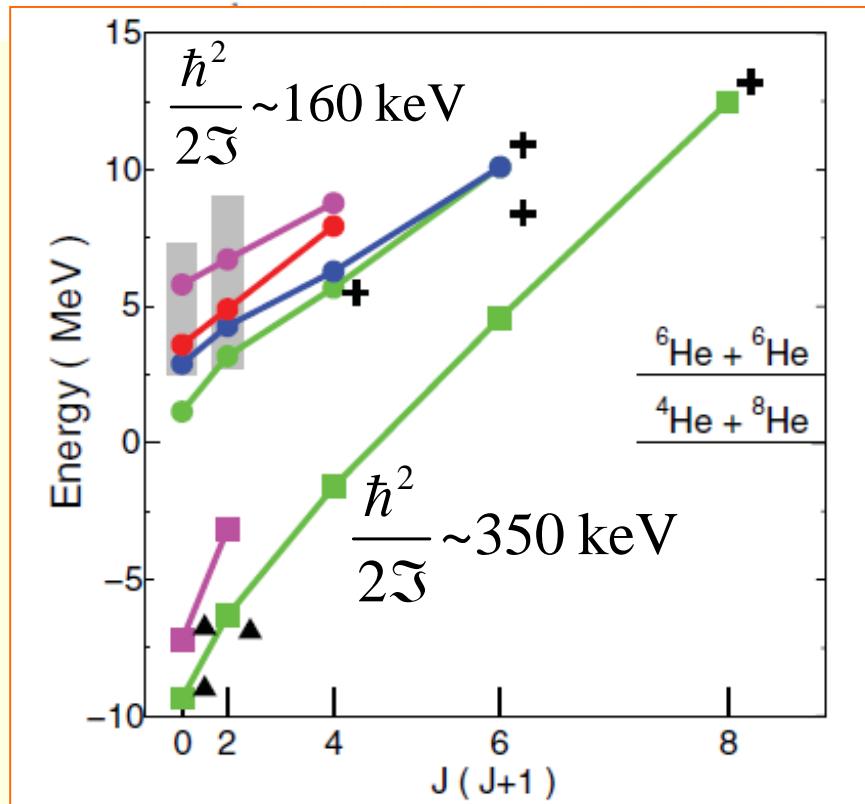
PRL 100, 182502 (2008)

PHYSICAL REVIEW LETTERS

week ending  
9 MAY 2008

## Coexistence of Covalent Superdeformation and Molecular Resonances in an Unbound Region of $^{12}\text{Be}$

M. Ito,<sup>1</sup> N. Itagaki,<sup>2</sup> H.



## ii) Determination of the cluster decay width and the cluster SF

SCIENCE CHINA  
Physics, Mechanics & Astronomy

2014 Vol. 57 No. 9: 1613–1617

### Determination of the cluster spectroscopic factor of the 10.3 MeV state in $^{12}\text{Be}^\dagger$

YANG ZaiHong, YE YanLin\*, LI ZhiHuan, LOU JianLin, XU FuRong, PEI JunCheng,

$$N(E) \propto \frac{\Gamma(E)}{[E - E_r - \Delta(E)]^2 + [\Gamma(E)/2]^2}.$$

$$\Gamma = \Gamma_\gamma + \Gamma_n + \Gamma_p + \Gamma_\alpha + \dots$$

the partial is of probability meaning,  
not energy meaning:  $\Gamma_i / \Gamma = \sigma_i / \sigma$

#### R-matrix analysis

$$\Gamma_\alpha(E) = 2\gamma_\alpha^2 P_I(E),$$

$$P_I(E) = \frac{ka}{(F_I(ka))^2 + (G_I(ka))^2},$$

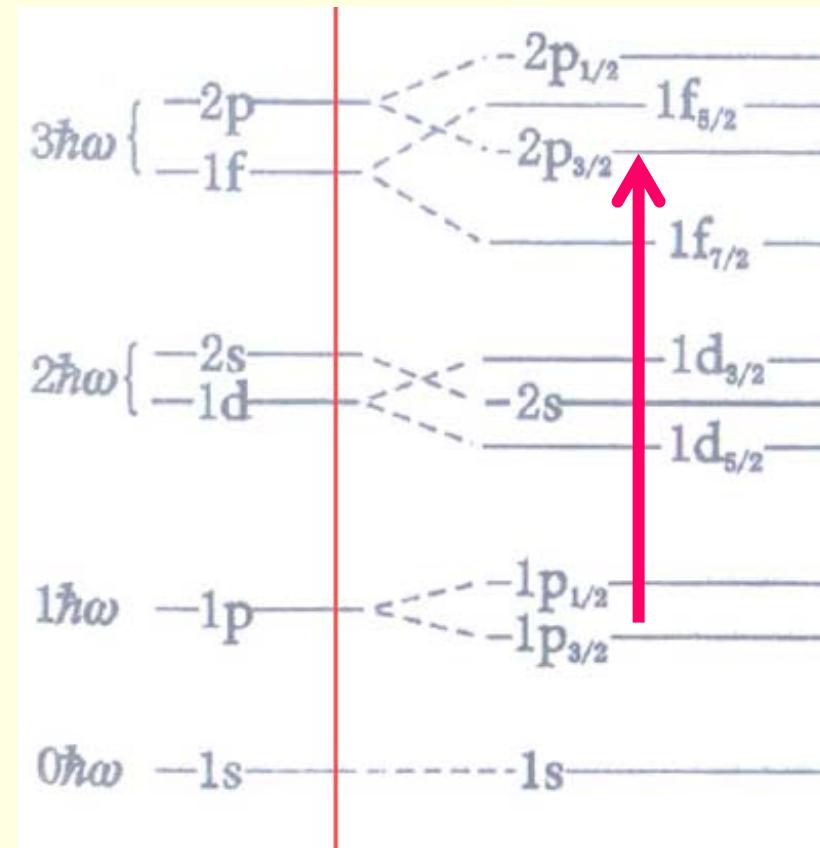
$$\theta_\alpha^2 = \frac{\gamma_\alpha^2}{\gamma_W^2}, \quad \gamma_W^2 = \frac{3\hbar^2}{2\mu a^2}.$$

where  $E$  is the decay energy (or relative energy) and  $a$  the channel radius. The latter is generally given by  $a = r_0(A_1^{1/3} + A_2^{1/3})$  with  $r_0 \approx 1.4$  fm. For  $^{12}\text{Be}$  decaying into  $^4\text{He} + ^8\text{He}$ , the channel radius is about  $a = 5$  fm. This value was also adopted in AMD calculations [32]. In eq. (2)  $F_I(ka)$  and  $G_I(ka)$  are regular and irregular Coulomb wave functions [9,31].

### iii) Determination of the monopole transition strength

T. Yamada et al., PRC85,034315(2012); PTP120,1139(2008)

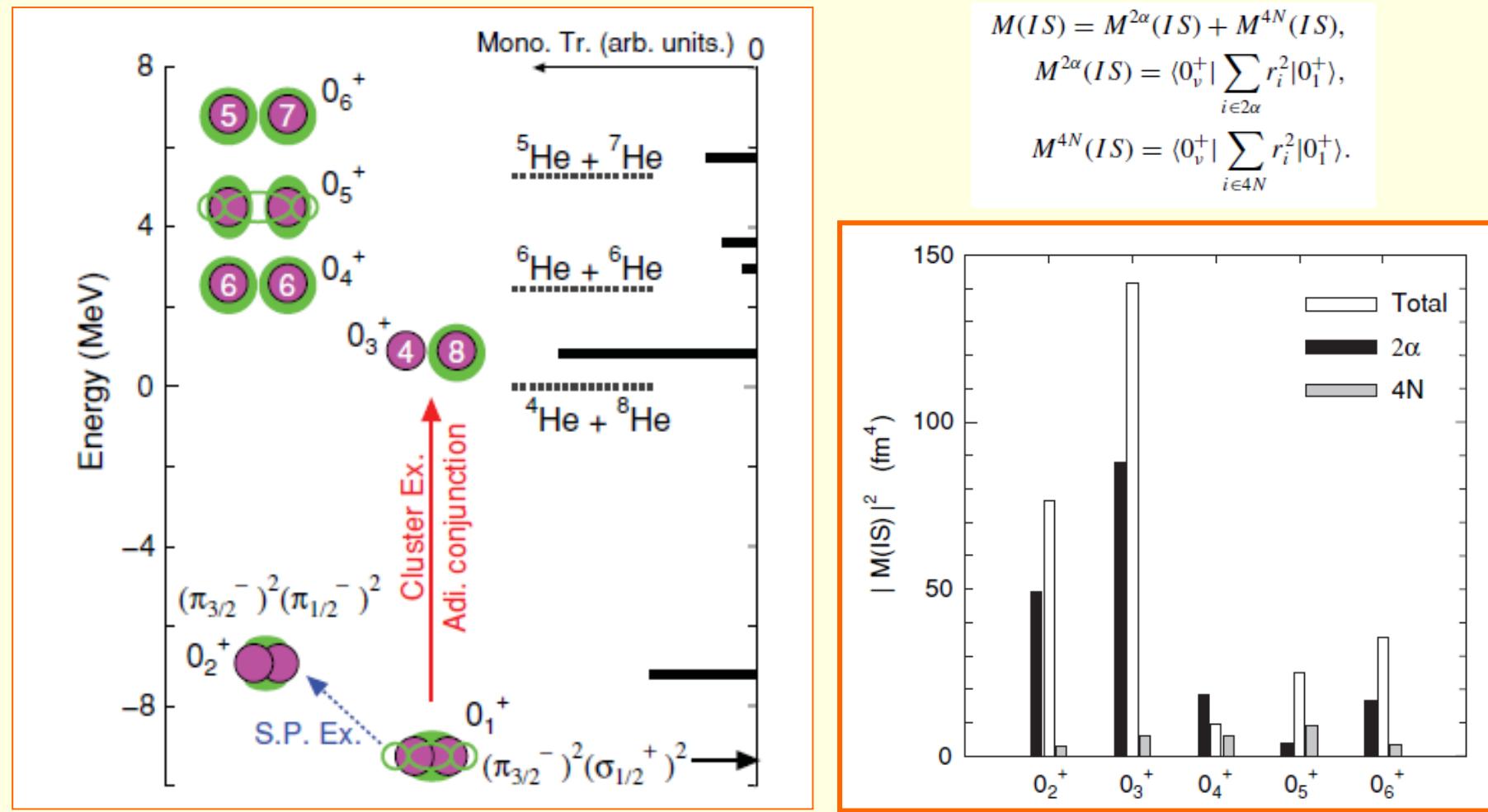
Isoscaler monopole excitation means a jump of about 35 MeV in a simple single-particle picture. A strong M(IS) for  $E_x$  below 20 MeV is an indicator of cluster formation



# Imprint of adiabatic structures in monopole excitations of $^{12}\text{Be}$

Makoto Ito

Department of Pure and Applied Physics, Kansai University, Yamate-cho 3-3-35, Suita 564-8680, Japan,  
 Research Center for Nuclear Physics (RCNP), Osaka University, Mihogaoka 10-1, Suita 567-0047, Japan, and  
 RIKEN Nishina Center for Accelerator-based Science, RIKEN, Wako, 351-0198 Saitama, Japan



# Determining the monopole strength

## Monopole Strength Function

$$S(E) = \sum_n \delta(E - E_n) \left| \langle 0_n^+ | \hat{O} | 0_1^+ \rangle \right|^2$$

$$\hat{O} = \sum_{i=0}^{16} (\mathbf{r}_i - \mathbf{R}_{\text{cm}})^2$$

$$R(E) = \left\langle 0_1^+ \left| \frac{\hat{O}^\dagger \hat{O}}{E - H + i\varepsilon} \right| 0_1^+ \right\rangle$$

$|0_n^+\rangle$ : resonance state with  $E_n - i\Gamma_n/2$

$$\begin{aligned} S(E) &= -\frac{1}{\pi} \text{Im}[R(E)] \\ &= \frac{1}{\pi} \sum_n \frac{\Gamma_n / 2}{(E - E_n)^2 + (\Gamma_n / 2)^2} \left| M(0_n^+ - 0_1^+) \right|^2 \end{aligned}$$

IS-monopole m.e.:  $M(0_n^+ - 0_1^+) = \langle 0_n^+ | \hat{O} | 0_1^+ \rangle$

Energy weighted sum rule (EWSR):

$$\sum_n (E_n - E_1) \left| M(0_n^+ - 0_1^+) \right|^2 = \frac{2\hbar^2}{m} \times 16 \times R^2, \quad R = \sqrt{\frac{1}{16} \left\langle 0_1^+ \left| \sum_{i=1}^{16} (\mathbf{r}_i - \mathbf{R}_{\text{cm}})^2 \right| 0_1^+ \right\rangle}$$

# Outline

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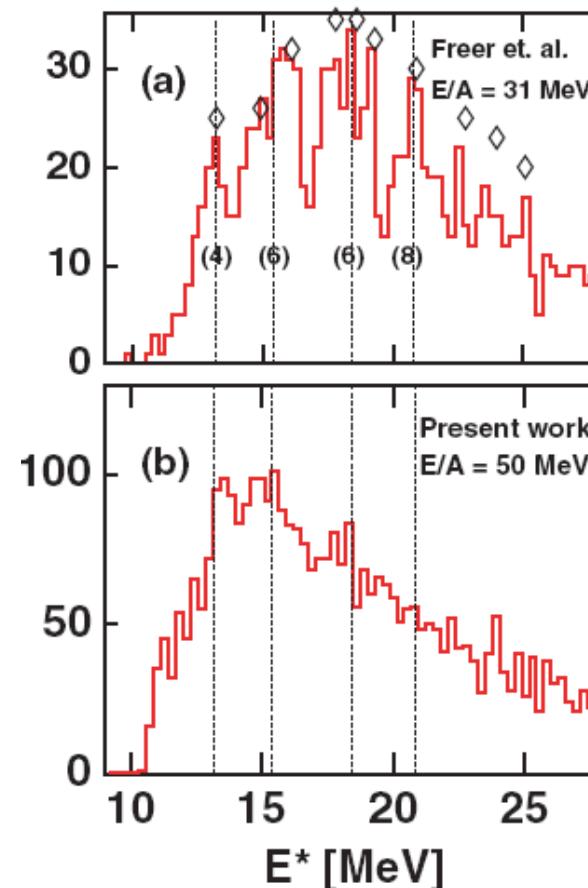
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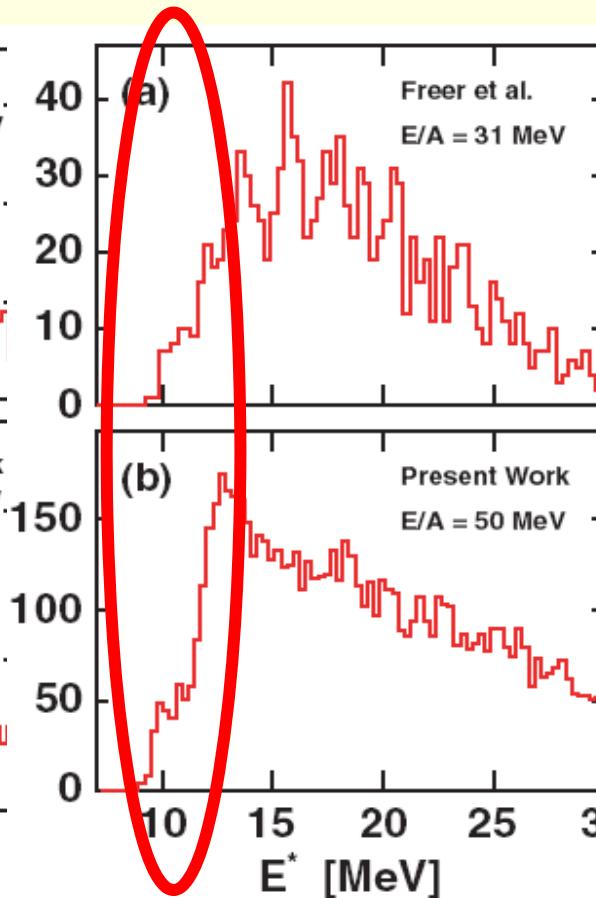
Freer et al., PRL82(1999) 1383; PRC63 (2001)034301

Charity et al., PRC76(2007)064313

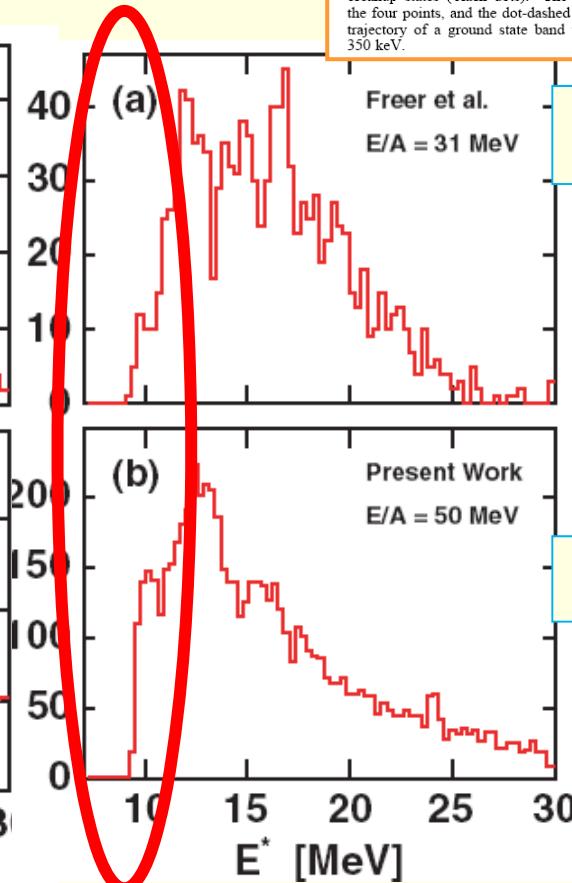
no small angle (low  $E_{\text{rel}}$ ) detection



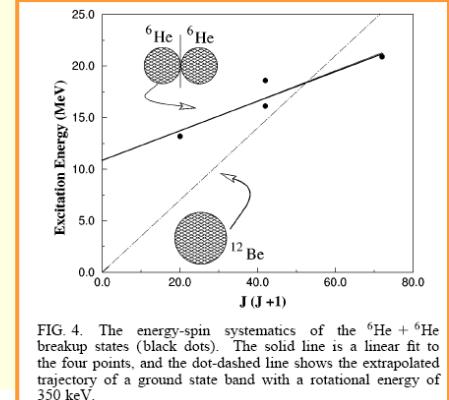
${}^6\text{He} + {}^6\text{He}, \text{CH}_2$



${}^4\text{He} + {}^8\text{He}, \text{with P}$



${}^4\text{He} + {}^8\text{He}, \text{with C}$



Freer

Charity

# Formations of loose clusters in an unbound region of $^{12}\text{Be}$

Makoto Ito

*Department of Pure and Applied Physics, Kansai University, Yamatecho 3-3-35, Suita, Japan,*

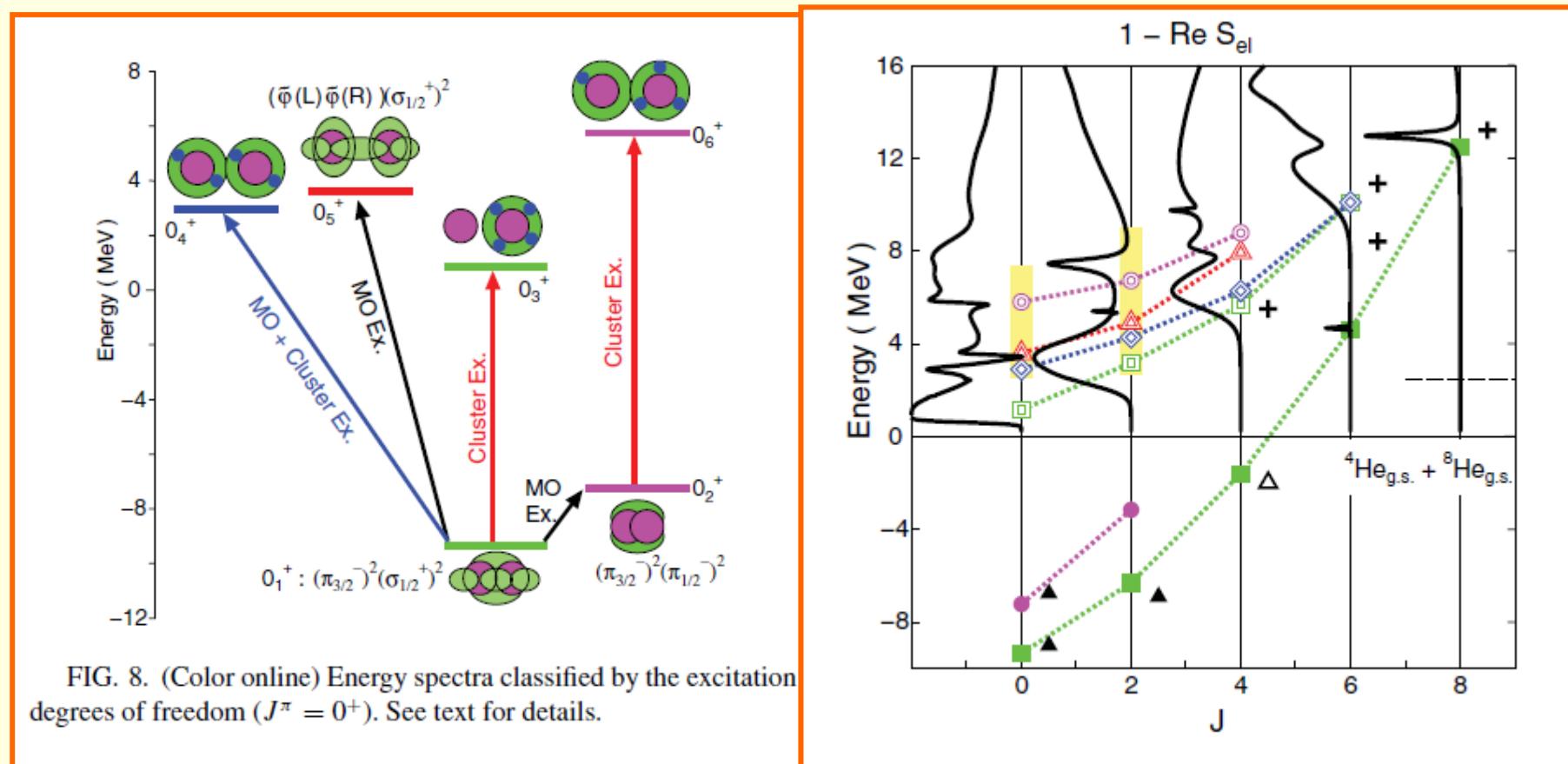
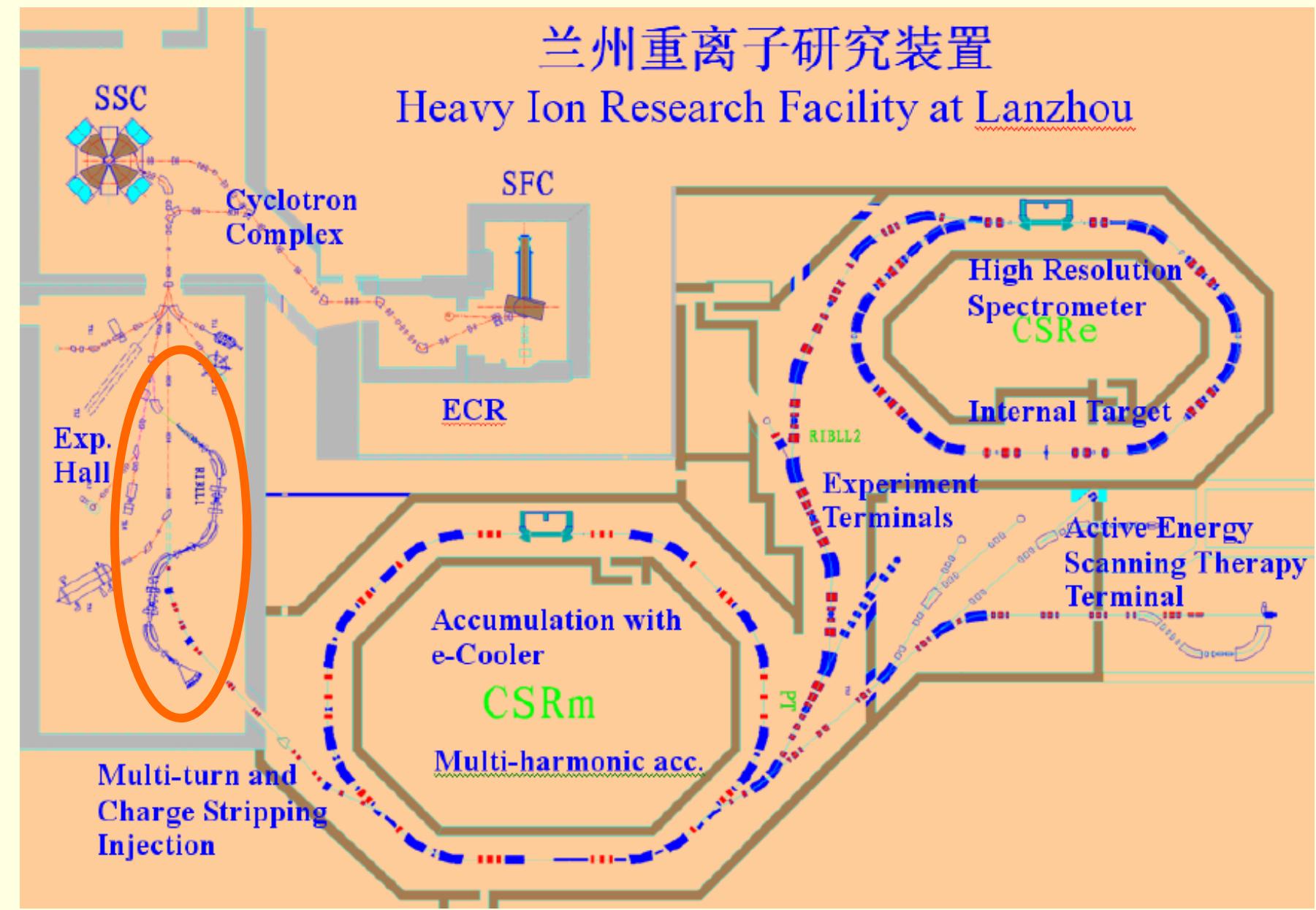


FIG. 8. (Color online) Energy spectra classified by the excitation degrees of freedom ( $J^\pi = 0^+$ ). See text for details.

# A new exp. at RIBLL1@HIRFL, Lanzhou



# Collaborators

PRL 112, 162501 (2014)

PHYSICAL REVIEW LETTERS

week ending  
25 APRIL 2014

## Observation of Enhanced Monopole Strength and Clustering in $^{12}\text{Be}$

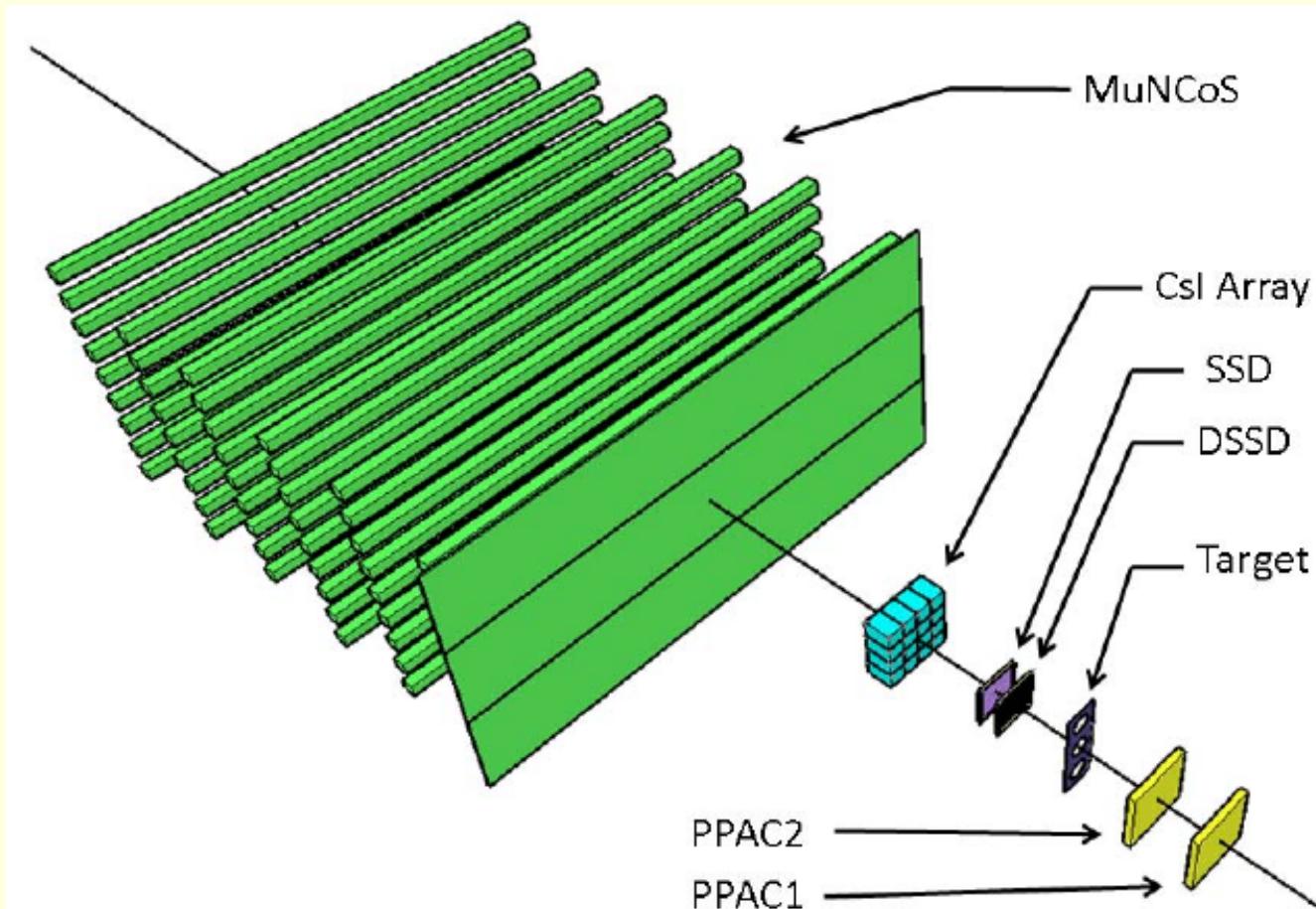
Z. H. Yang (杨再宏),<sup>1</sup> Y. L. Ye (叶沿林),<sup>1,\*</sup> Z. H. Li (李智焕),<sup>1</sup> J. L. Lou (楼建玲),<sup>1</sup> J. S. Wang (王建松),<sup>2</sup> D. X. Jiang (江栋兴),<sup>1</sup> Y. C. Ge (葛渝成),<sup>1</sup> Q. T. Li (李奇特),<sup>1</sup> H. Hua (华辉),<sup>1</sup> X. Q. Li (李湘庆),<sup>1</sup> F. R. Xu (许甫荣),<sup>1</sup> J. C. Pei (裴俊琛),<sup>1</sup> R. Qiao (乔锐),<sup>1</sup> H. B. You (游海波),<sup>1</sup> H. Wang (王赫),<sup>1,3</sup> Z. Y. Tian (田正阳),<sup>1</sup> K. A. Li (李阔昂),<sup>1</sup> Y. L. Sun (孙叶磊),<sup>1</sup> H. N. Liu (刘红娜),<sup>1,3</sup> J. Chen (陈洁),<sup>1</sup> J. Wu (吴锦),<sup>1,3</sup> J. Li (李晶),<sup>1</sup> W. Jiang (蒋伟),<sup>1</sup> C. Wen (文超),<sup>1,3</sup> B. Yang (杨彪),<sup>1</sup> Y. Y. Yang (杨彦云),<sup>2</sup> P. Ma (马朋),<sup>2</sup> J. B. Ma (马军兵),<sup>2</sup> S. L. Jin (金仕纶),<sup>2</sup> J. L. Han (韩建龙),<sup>2</sup> and J. Lee (李晓菁)<sup>3</sup>

<sup>1</sup>*State Key Laboratory of Nuclear Physics and Technology, School of Physics, Peking University, Beijing 100871, China*

<sup>2</sup>*Institute of Modern Physics, Chinese Academy of Science, Lanzhou 730000, China*

<sup>3</sup>*RIKEN Nishina Center, 2-1 Hirosawa, Wako, Saitama 351-0198, Japan*

(Received 10 December 2013; published 22 April 2014)



**Beam:**  $^{12}\text{Be}$ , 29.0MeV/u, ~3000pps

**Target:** Carbon, 100 mg/cm<sup>2</sup>

**DSSD:** 32 2mm-stip, 300μm , covering 0°-12° Lab.

**CsI(Tl):** 4 x 4, 2.5cm\*2.5cm\*3cm,

**Detection focused on the most forward angles**

# Resolution and efficiency

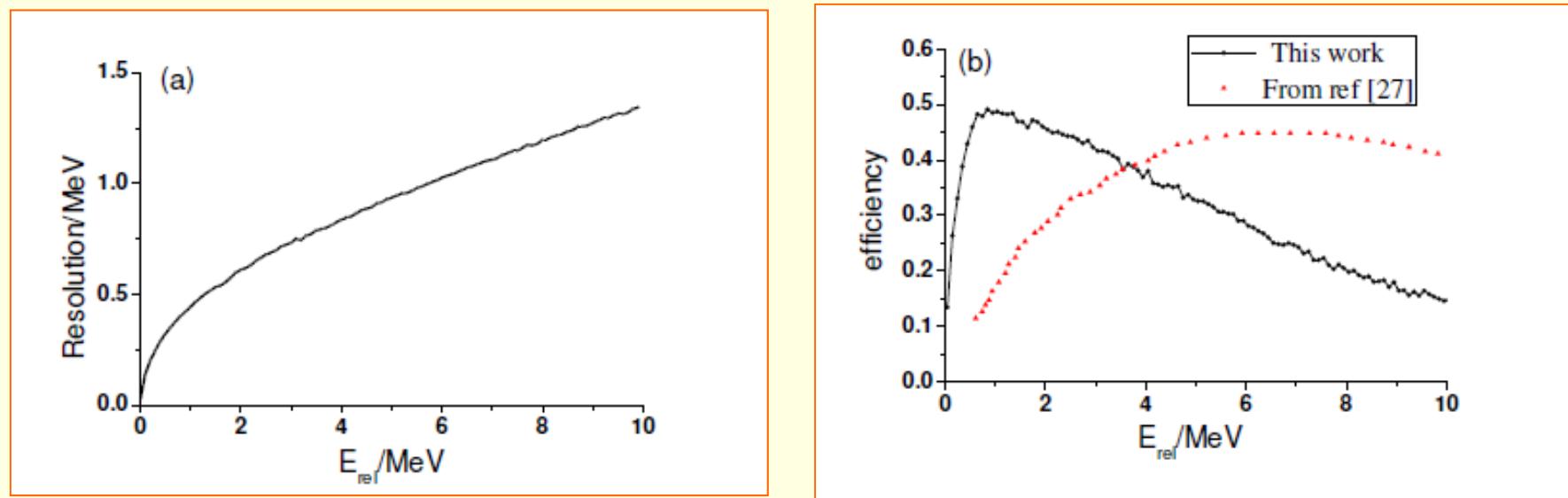
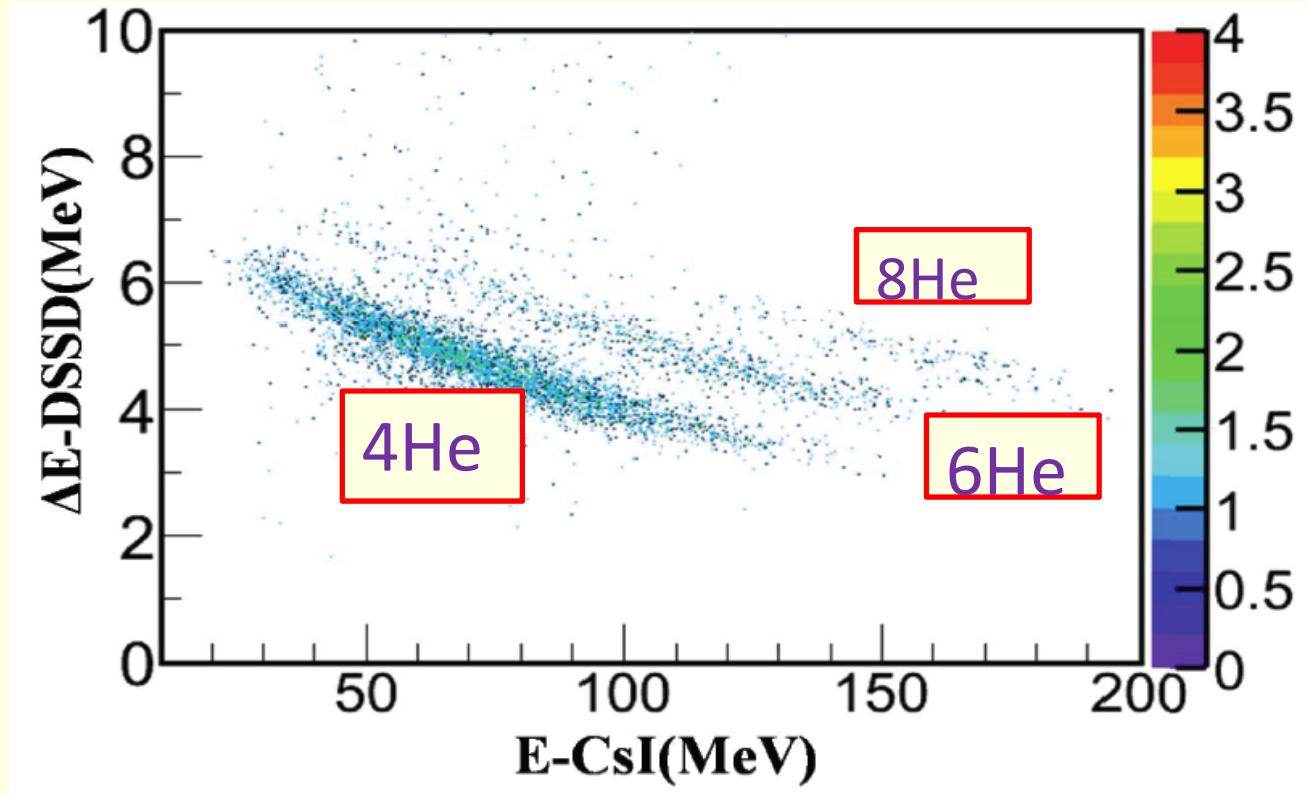


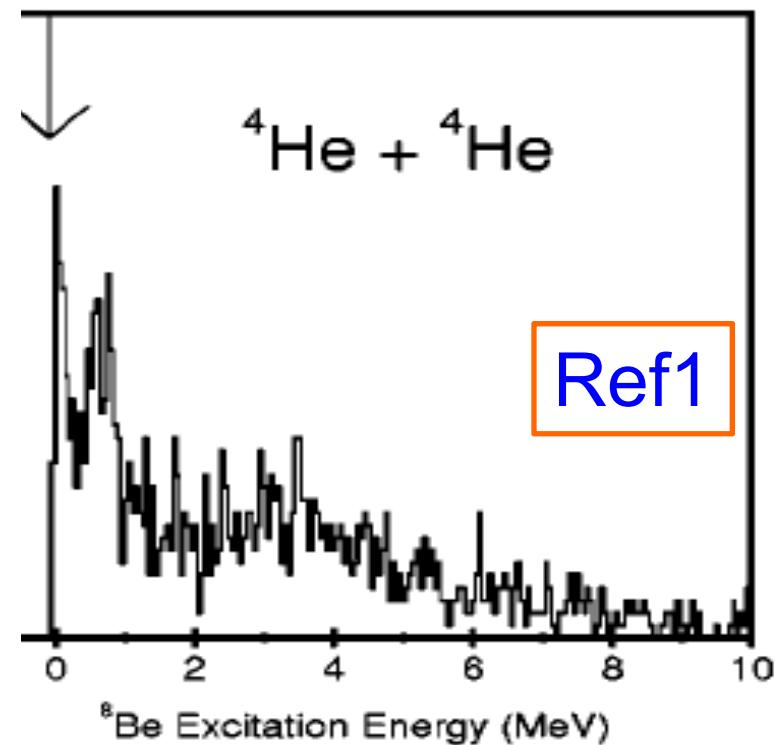
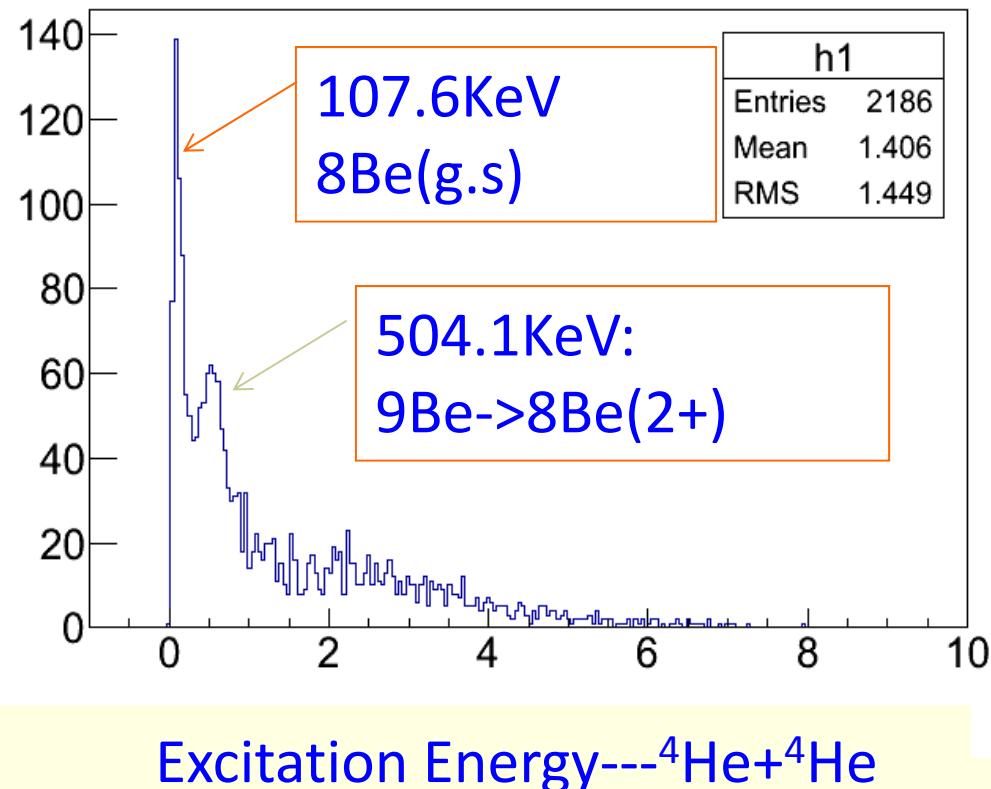
FIG. 2. Resolution(FWHM) of  $E_{rel}$  (a) and detection efficiency (b) for  $^{12}\text{Be}$  decaying into  $^4\text{He} + ^8\text{He}$ . Similar results are also obtained for  $^{12}\text{Be}$  decaying into  $^6\text{He} + ^6\text{He}$ . And for comparison, the efficiency obtained from reference[27] was also shown.

## PID for $2-x$ He fragments

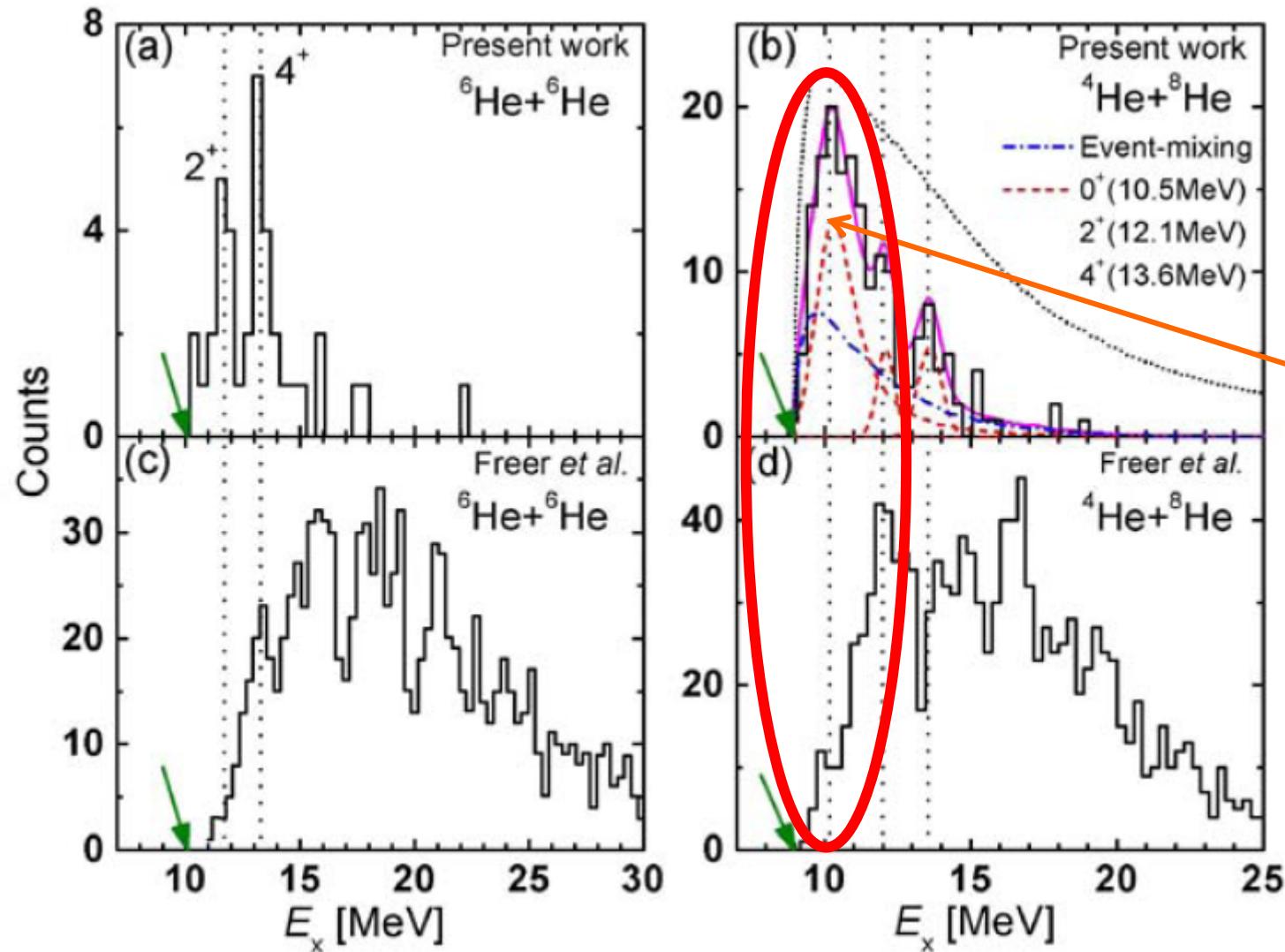


Uniform calibration of the Si strips and treatment of  
PID under intense direct beam:  
[IEEE-NS 61(2014)596, NIMA728(2013)52]

## verification for ${}^4\text{He} + {}^4\text{He}$ channel



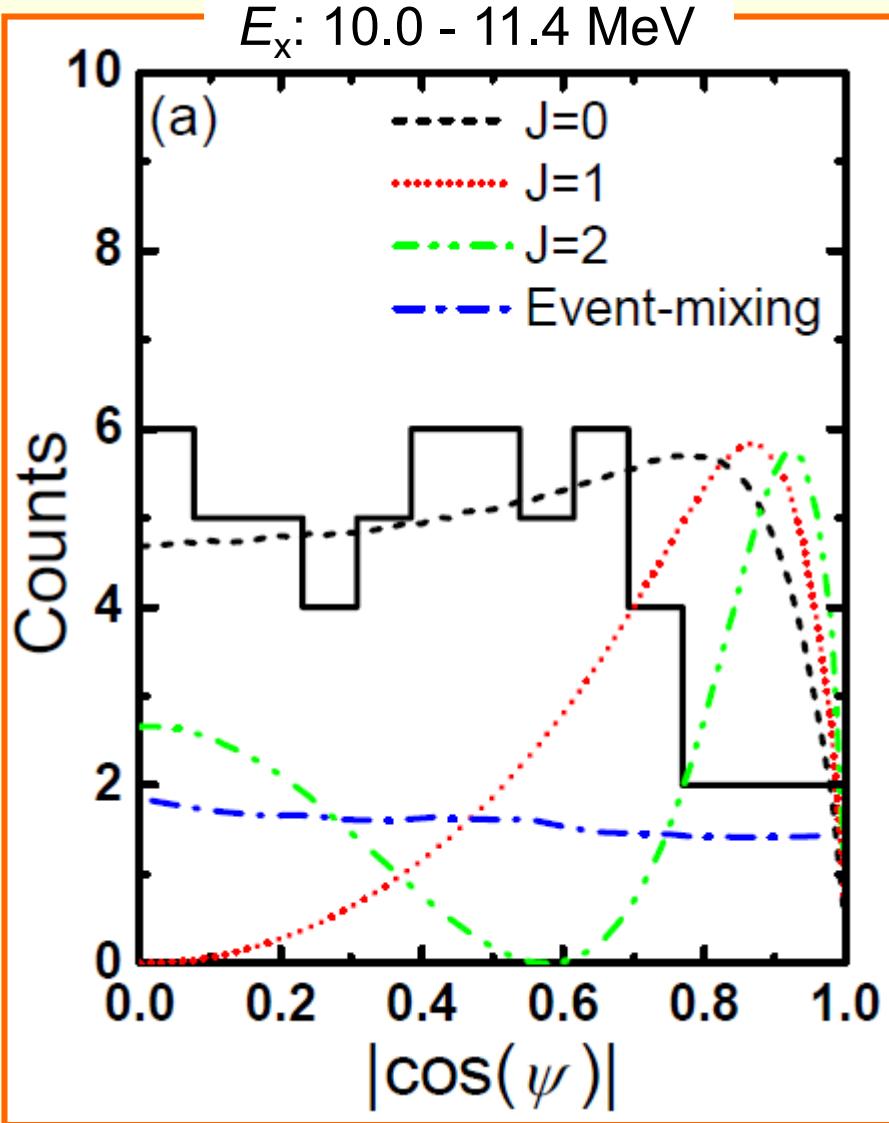
Ref1: PLB580(04)129- ${}^{14}\text{Be}$  breakup



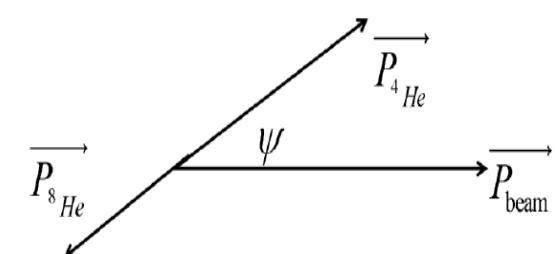
Large and unusual 10.3 MeV state;

Our exp:  ${}^6\text{He} + {}^6\text{He}$  11.7 13.3 MeV  
 ${}^4\text{He} + {}^8\text{He}$  10.3 12.1 13.6 MeV

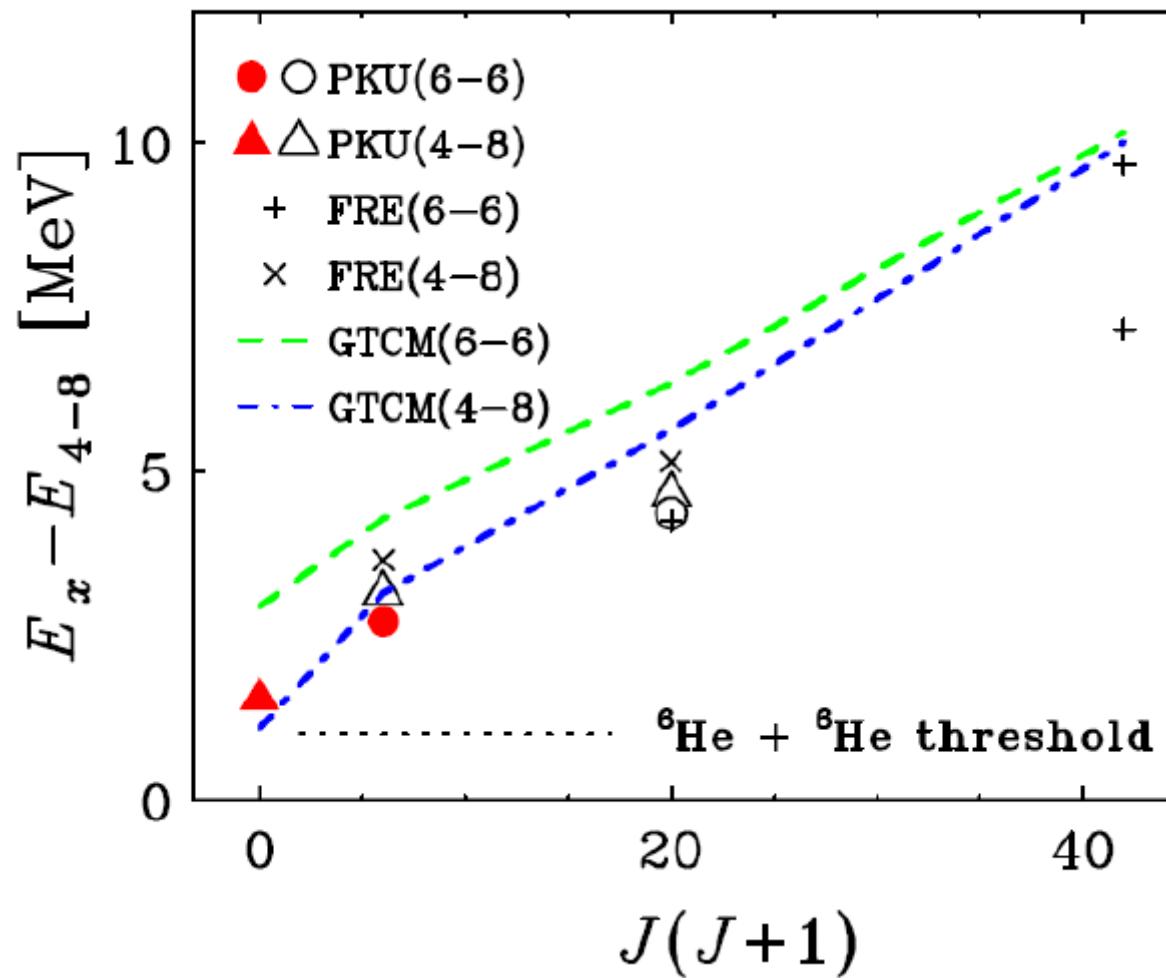
# Spin: Angular correlation analysis for the 10.3 MeV state in ${}^4\text{He} + {}^8\text{He}$ channel



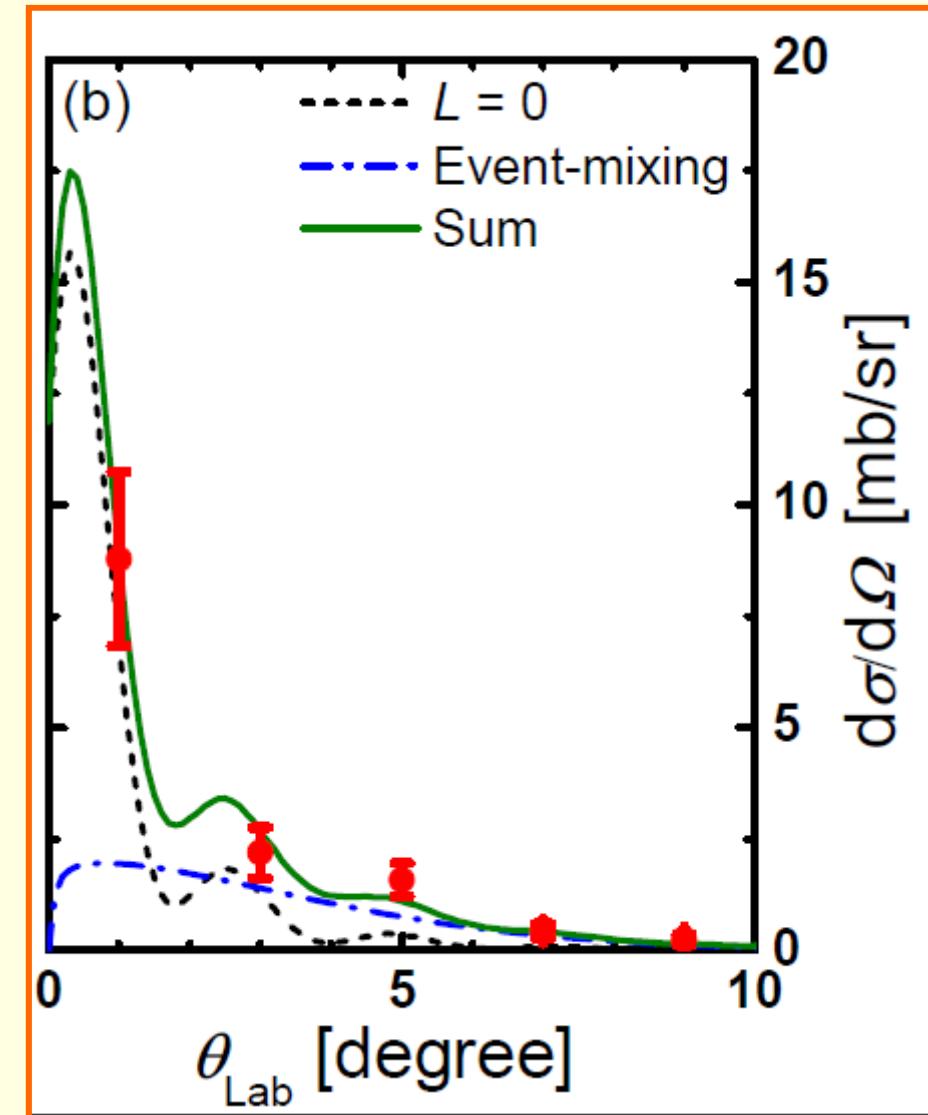
For small angle inelastic scattering leading to a resonant state with an angular momentum  $J$ , which subsequently breaks up into spin-0 fragments, the projected angular correlation spectrum is proportional to  $|P_J(\cos(\Psi))|^2$ , with  $\Psi$  being the fragment c.m. angle relative to the beam direction.



# Confirming the MR band with large moment of inertia



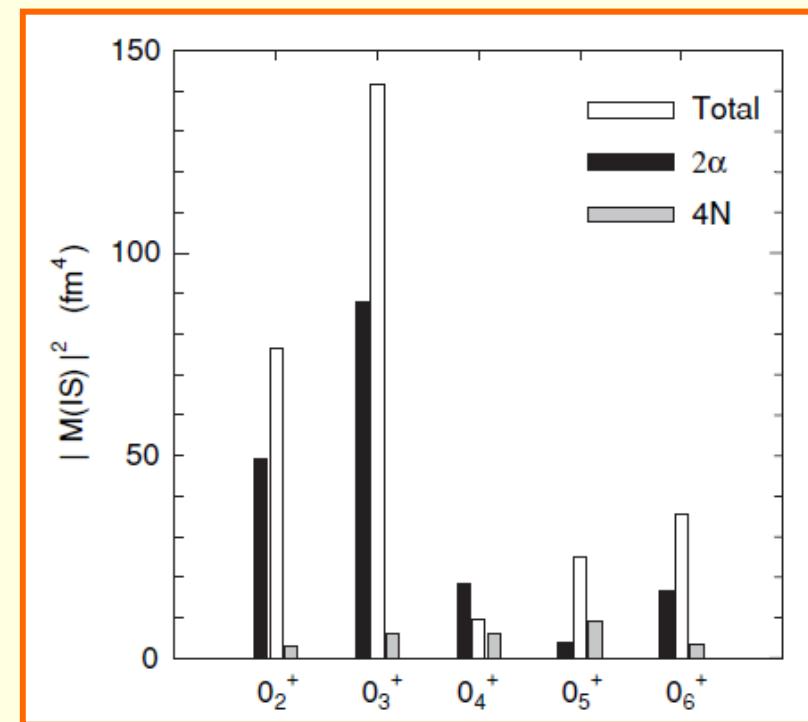
## DWBA calculation



Fraction:  $0.034(10) \times 2.2.$

EWSR:  $6727.9 \text{ fm}^4 \text{ MeV},$

$M(\text{IS})$ :  $7.0 \pm 1.0 \text{ fm}^2,$



# Determining the cluster decay width

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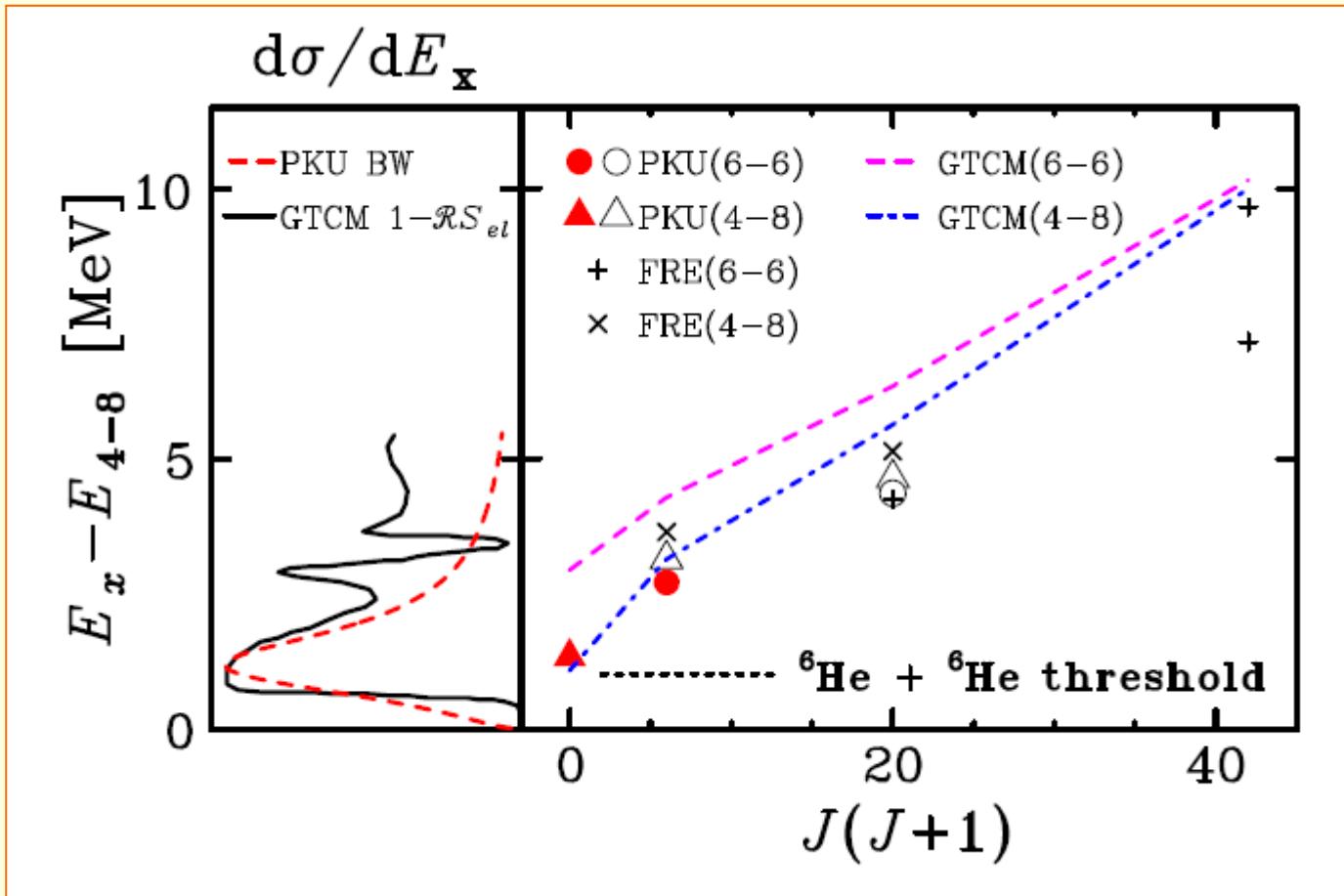
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10.3 MeV ( $0^+$ ) state:

$$\sigma = \pi \hat{\lambda}^2 \frac{\Gamma_a \Gamma_b}{(E' - E_0)^2 + (\Gamma/2)^2}$$

$$\Gamma = \sum_i \Gamma_i = 1.5(2) \text{ MeV}$$

$$\Gamma = \Gamma_\gamma + \Gamma_n + \Gamma_p + \Gamma_\alpha + \dots$$



10.3 MeV( $0^+$ ) state:  $\Gamma = 1.5(2)$  MeV;  $\Gamma = \Gamma_{He} + \Gamma_{be}$

Kosheninnikov[12]:  $\Gamma_{Be}/\Gamma = 0.28 \pm 0.12$

$\Gamma_{He}/\Gamma = 1 - \Gamma_{Be}/\Gamma = 0.72(12); \quad \Gamma_{He} = 1.1(2)$  MeV

$\gamma^2_{He} = 0.50(9); \quad \theta^2_{He} = 0.53(10)$  (comparable to  ${}^8Be$ )

- For the first time a strong monopole strength has been determined in unstable nuclei, providing a clear evidence for cluster formation in  $^{12}\text{Be}$ .
- Angular-correlation method is very sensitive to the spin of the resonance. MR band in  $^{12}\text{Be}$  has been justified based on the  $E_x$ -spin systematics .
- A large cluster-decay width, and consequently a large cluster SF, are obtained for the 10.3 MeV state in  $^{12}\text{Be}$ .

All these findings demonstrate a dominating cluster structure in  $^{12}\text{Be}$  just above the  $^4\text{He} + ^8\text{He}$  threshold.

# Outline

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- I. Historical background
- II. How to observe
- III.  $^{12}\text{Be}$  — an example
- IV. Future perspectives

# For clustering in ground state

## — QFS at $> 100$ MeV/u

Ex:  $^8\text{He}(\text{p}, \text{p}^6\text{He})$  at RIPS

RIKEN-RIBF Exp. RRC48, ;

Z.X. Cao, Y.L.Ye et all, PLB707(2012)46

- Primary Beam:  $^{13}\text{C}$ , 115MeV/A, 470enA
- Primary Target: Be(12mm), F1 Wedge: Al(962mg/cm<sup>2</sup>)
- Second Beam  $^8\text{He}$ , 82MeV/A  $\sim 3 \times 10^5$ pps
- Second Target: CH<sub>2</sub>(0.0830mg/cm<sup>2</sup>), C(0.1339mg/cm<sup>2</sup>), Empty

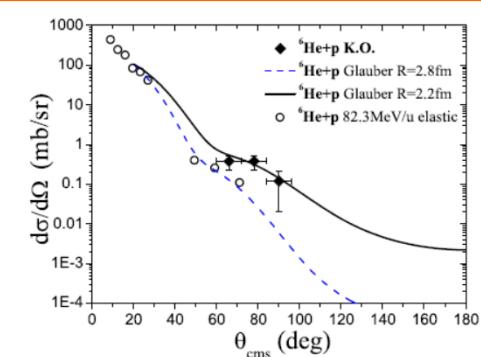
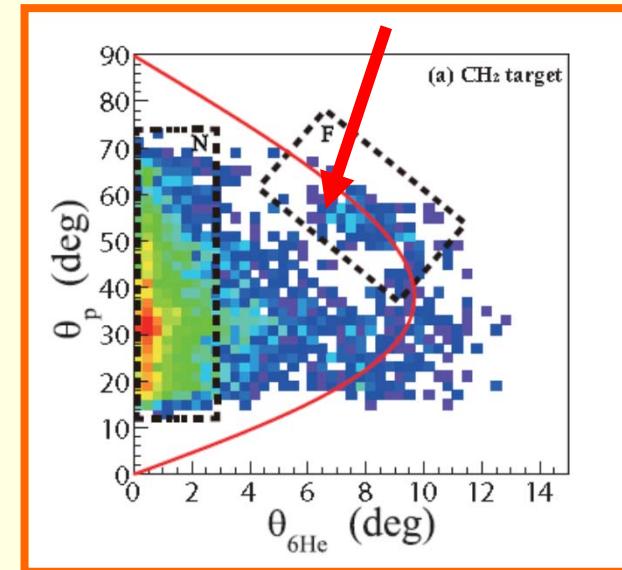
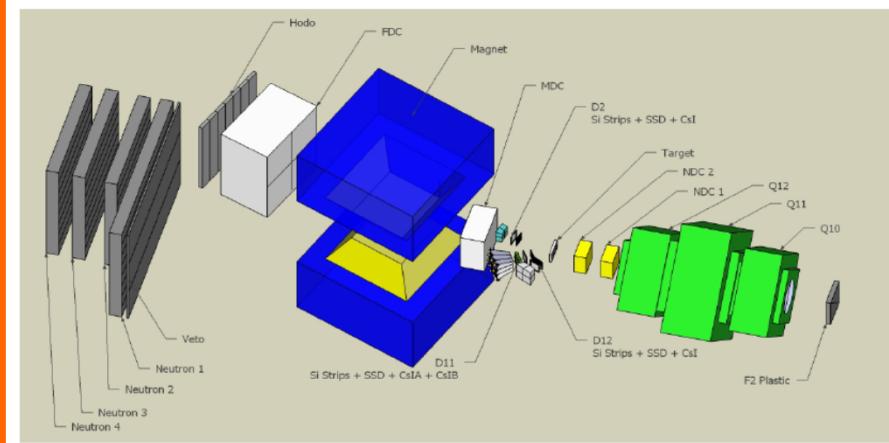
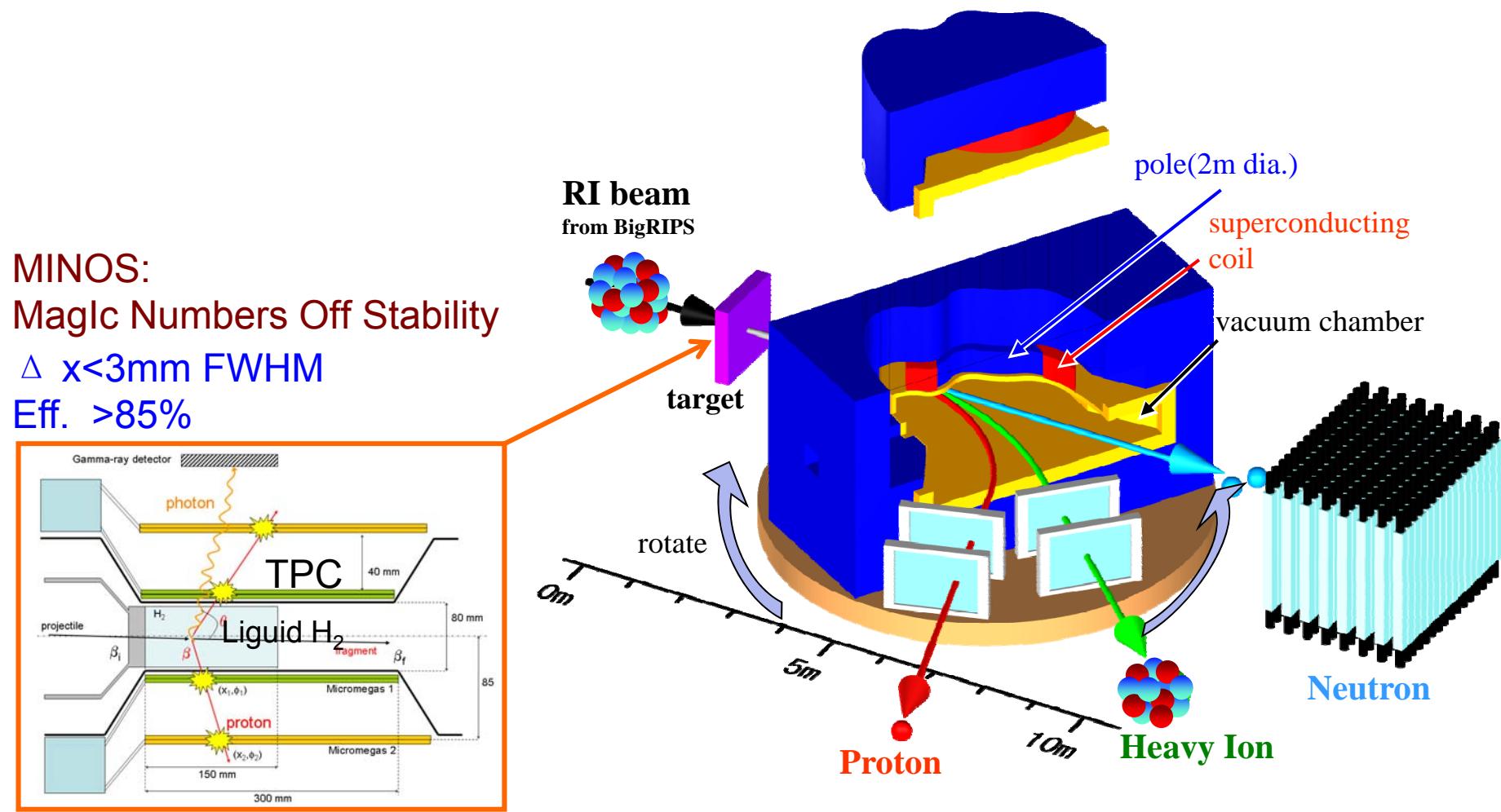


Figure 4: Differential cross sections of  $^6\text{He}$  core fragments knocked out (K.O.) from  $^8\text{He}$  projectiles at 82.3 MeV/u (the filled diamonds). Data for elastic scattering of  $^6\text{He}$  on proton target are also presented by the circles [22]. The dashed line represents the Glauber model calculation for elastic scattering, whereas the solid line displays the same kind of calculation but with a reduced matter radii for  $^6\text{He}$ .

# New proposals at BigRIPS + AMURAI .....



# For clustering in resonant states

## — beams < 30 MeV/u

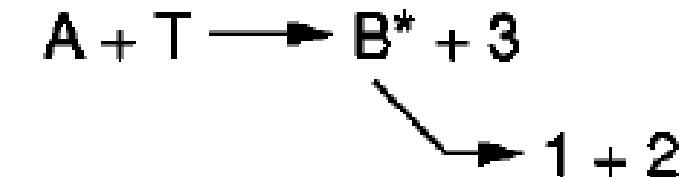
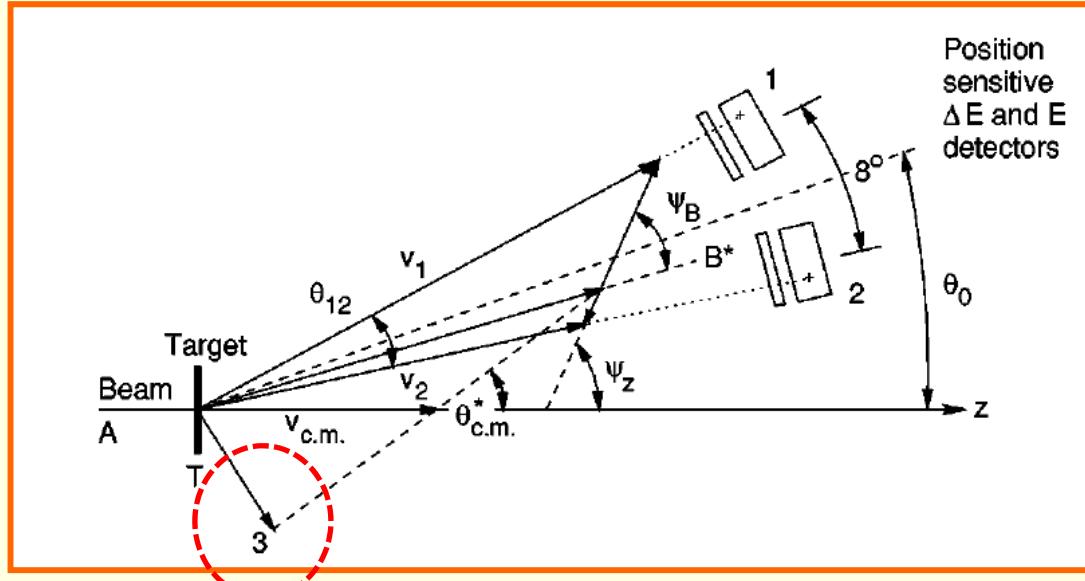
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- peak position (band?)
- spin-parity (band?)
- area (cross section) as a function of angle
- shape and width (R-matrix analysis)
- decay branches (partial widths) and angular correlation

Need both missing mass (MM) and invariant mass (IM) measurements

# missing mass (inelastic or transfer)

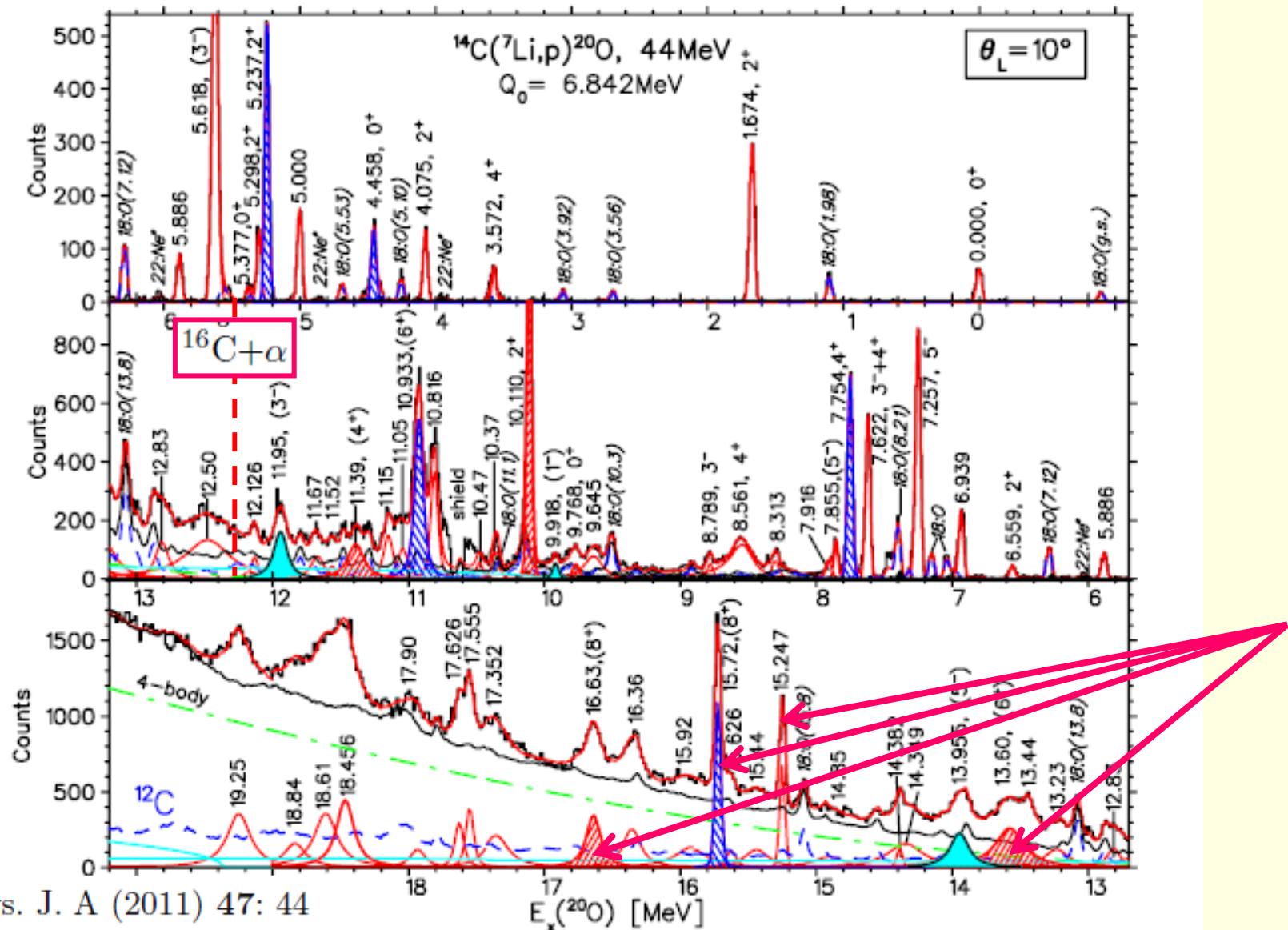


$$Q = T_3 + T_{B^*} - T_A = m_T + m_A - m_3 - m_{B^*}$$

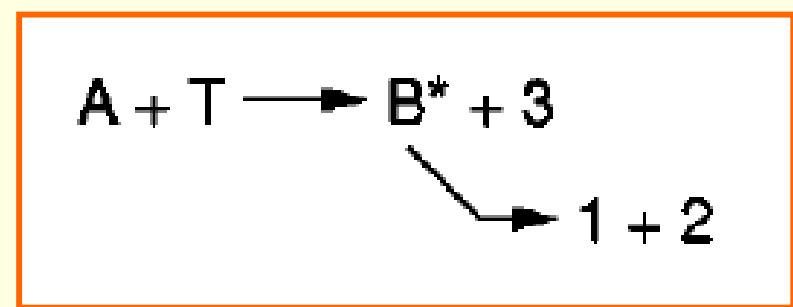
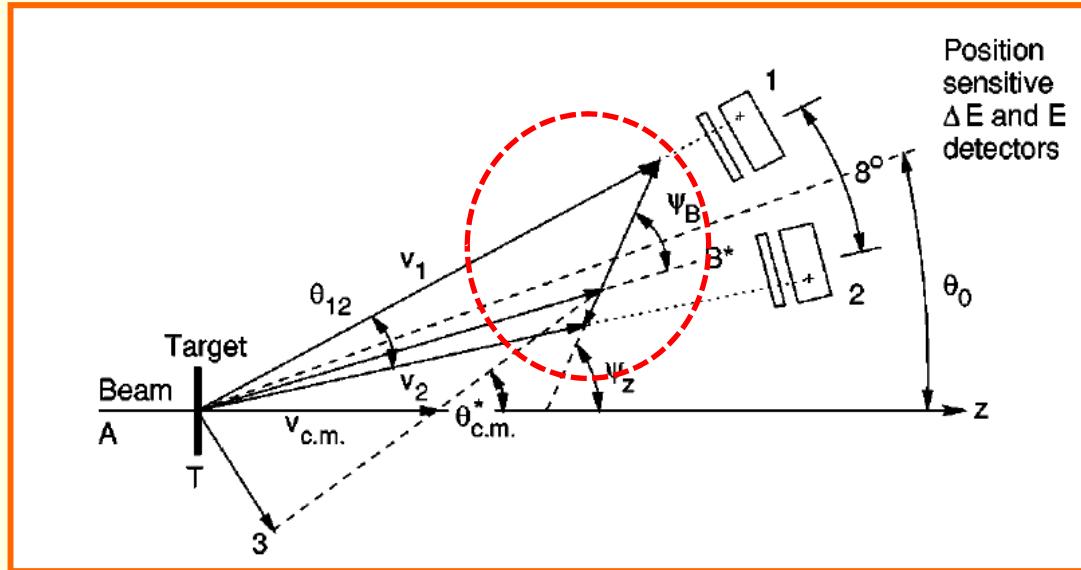
$$m_{B^*} = m_T + m_A - m_3 - Q$$

$$Q = \left( \frac{m_A}{m_B} - 1 \right) T_A + \left( \frac{m_3}{m_B} + 1 \right) E_3 - \frac{2(m_A m_3 T_A T_3)^{1/2} \cos \theta}{m_B}$$

Members of the  $K = 0^+_2$ ,  $1^-_2$ , and  $0^+_4$  bands of  $^{20}\text{O}$  (with tentative assignments) are marked by downward hatched (blue), filled (cyan), and upward hatched (red) areas, respectively.



# invariant mass



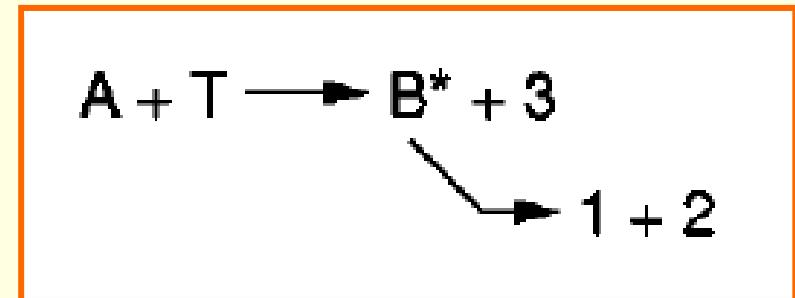
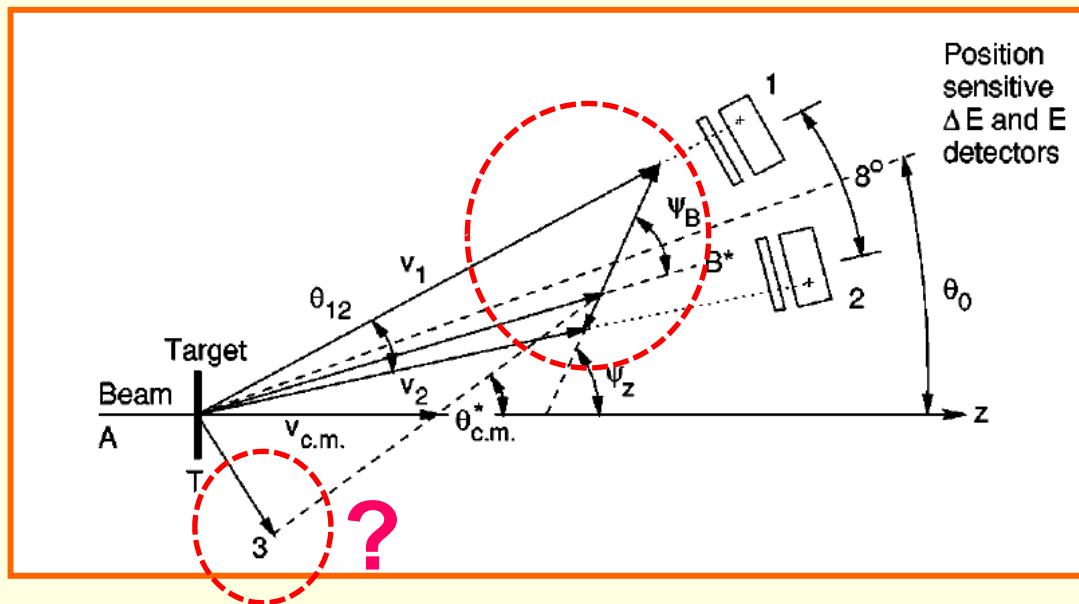
$$E_{B^*} = E_1 + E_2, \quad \vec{p}_{B^*} = \vec{p}_1 + \vec{p}_2$$

$$m_{B^*}c^2 = [E_{B^*}^2 - c^2 p_{B^*}^2]^{1/2} = [(E_1 + E_2)^2 - c^2 |\vec{p}_1 + \vec{p}_2|^2]^{1/2}$$

$$E_S = (m_1 + m_1 - m_B)c^2$$

$$E_x = m_{B^*}c^2 - m_Bc^2 = E_S + E_{\text{rel}}$$

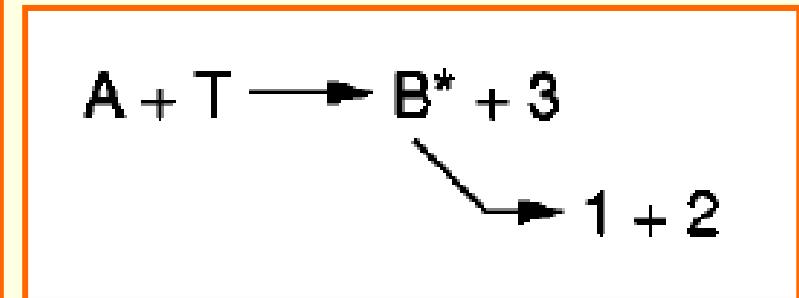
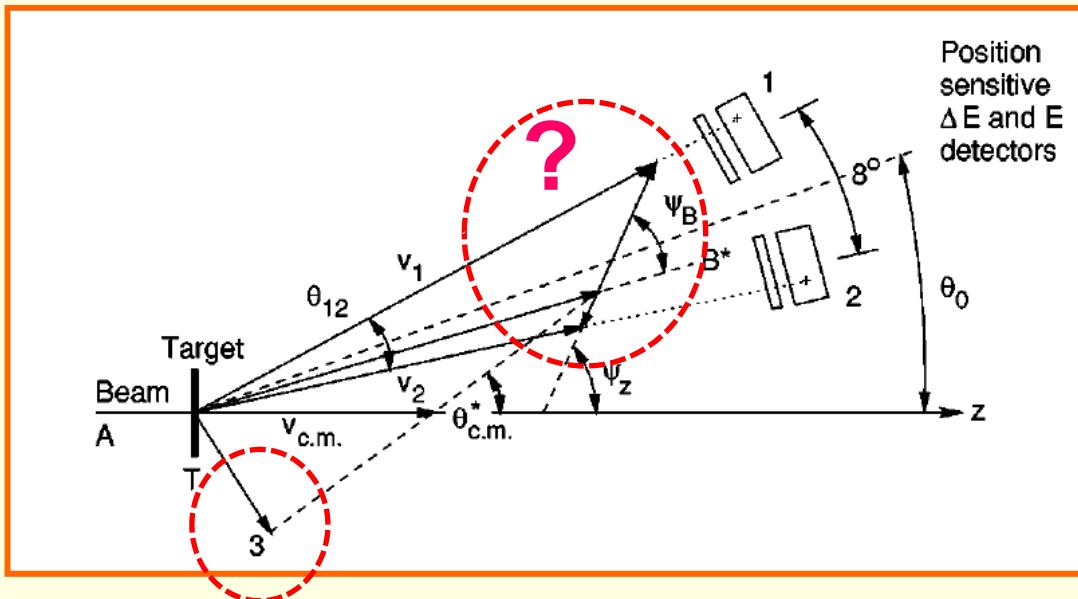
# RI beam & recoil target: IM + MM



- for RI beam excitation (IM) & recoil target (MM)
- good experiences for IM measurement
  - MM at low recoil energies?

\* one proposal made at HIRFL-RIBLL

# Stable beam & excited target: MM + IM



for stable beam (MM) and target excitation (IM)

- good experiences on MM measurement
- IM at low recoil energies

\* one proposal made at CIAE

# Summary

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- Clustering should be a general phenomenon in light unstable nuclei.
- Consistent evidences are needed to experimentally ping down a cluster state, such as large momentum of inertial, large cluster decay partial width and large selective excitation strength.
- QFS at higher energies and MM + IM measurements at lower energies are good ways to observe the evidences of clustering

Thank you for  
your attention

TABLE VI. The theoretical values of the partial decay widths and the reduced widths for the  ${}^6\text{He} + {}^6\text{He}$  and  ${}^8\text{He} + {}^4\text{He}$  decays from excited states of  ${}^{12}\text{Be}$ . The channel radius is chosen to be  $a = 5$  fm.

$J_n^+$	${}^6\text{He} + {}^6\text{He}$		${}^8\text{He} + {}^4\text{He}$	
	$\gamma_{^6\text{He}}^2(a)$	$\Gamma_{^6\text{He}}(\text{keV})$	$\gamma_{^4\text{He}}^2(a)$	$\Gamma_{^4\text{He}}(\text{keV})$
$0_3^+$	$2.5 \times 10^{-1}$	$7 \times 10^2$	$1.3 \times 10^{-2}$	$4 \times 10^1$
$2_4^+$	$8.3 \times 10^{-2}$	1	$3.5 \times 10^{-3}$	3
$4_2^+$	$1.3 \times 10^{-1}$	7	$1.7 \times 10^{-2}$	5
$6_2^+$	$4.3 \times 10^{-2}$	16	$2.2 \times 10^{-3}$	1
$8_1^+$			$1.6 \times 10^{-2}$	1

# Impact on the nuclear-astrophysics

Progress of Theoretical Physics Supplement No. 196, 2012

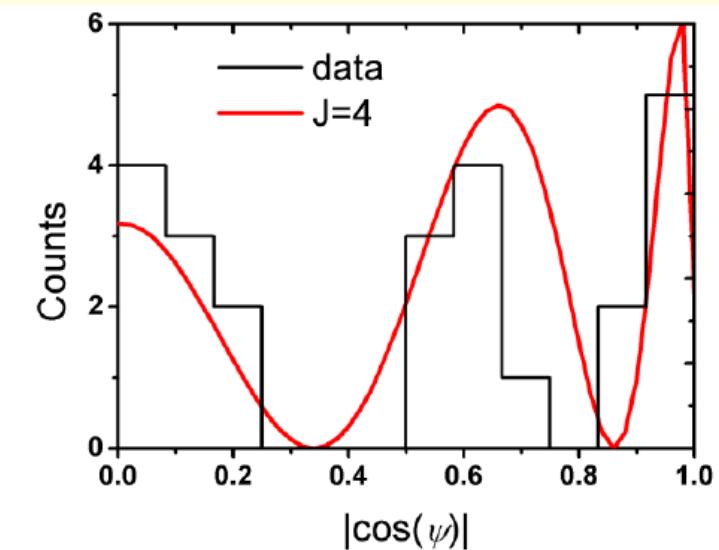
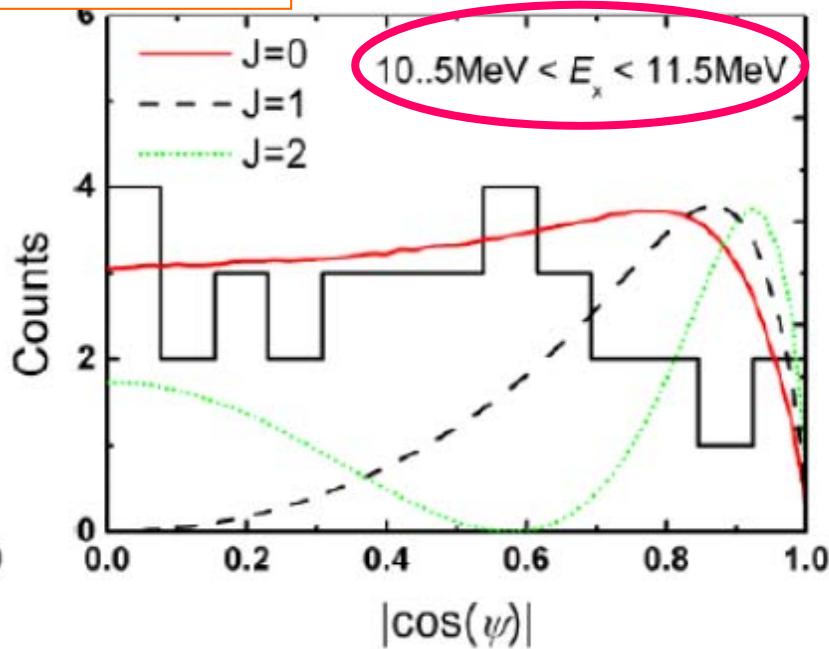
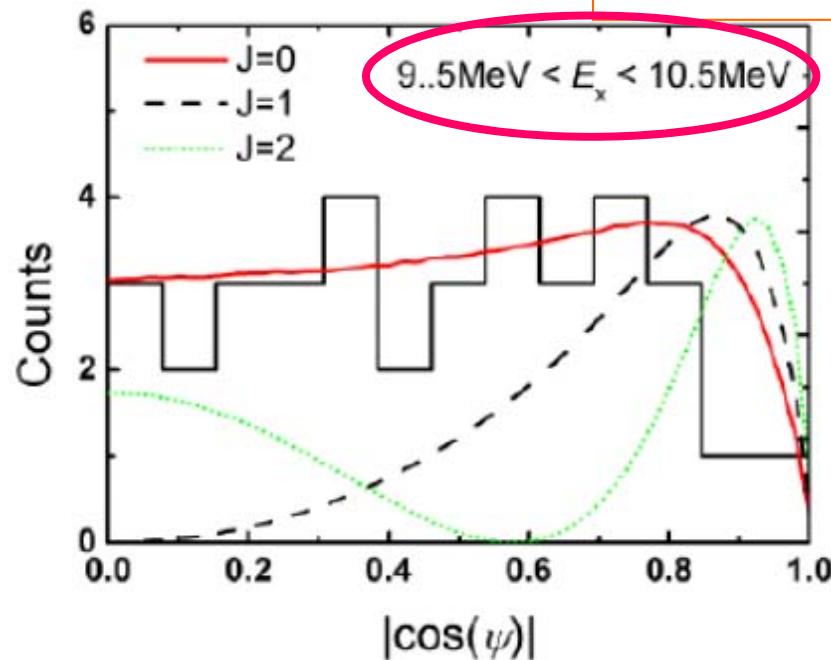
## Alpha-Cluster Dominance in the $\alpha p$ Process in Explosive Hydrogen Burning

Shigeru KUBONO,<sup>1</sup> N. Binh DAM,<sup>2</sup> S. HAYAKAWA,<sup>1</sup> H. HASHIMOTO,<sup>1</sup> D. KAHL,<sup>1</sup>  
H. YAMAGUCHI,<sup>1</sup> Y. WAKABAYASHI,<sup>3</sup> T. TERANISHI,<sup>4</sup> N. IWASA,<sup>5</sup>  
T. KOMATSUBARA,<sup>6</sup> S. KATO,<sup>7</sup> A. CHEN,<sup>8</sup> S. CHERUBINI,<sup>9</sup> S. H. CHOI,<sup>10</sup>  
I. S. HAHN,<sup>11</sup> J. J. HE,<sup>12</sup> Hong Khiem LE,<sup>2</sup> C. S. LEE,<sup>13</sup> Y. K. KWON,<sup>13</sup>  
S. WANAJO<sup>14</sup> and H.-T. JANKA<sup>14</sup>

<sup>1</sup>*Center for Nuclear Study, University of Tokyo, Wako 351-0198, Japan*

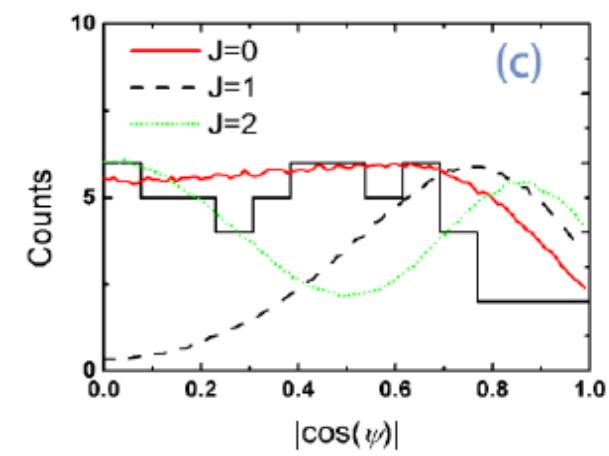
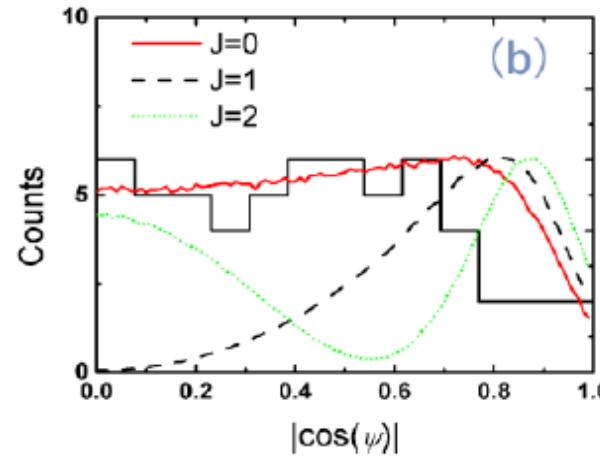
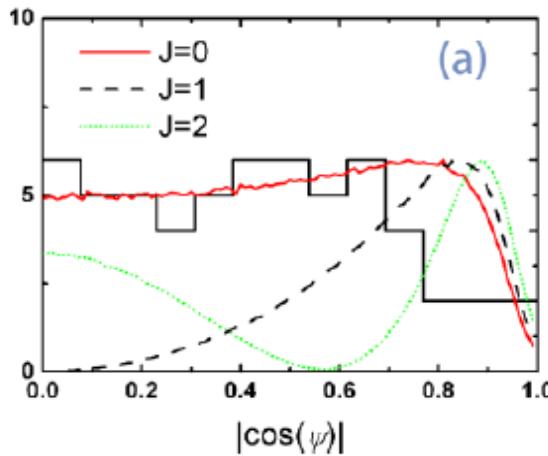
Nucleosynthesis by alpha particles and heavier  $4n$  nuclei are of great interest as they would involve nuclear cluster resonances. The role of nuclear clustering is discussed for nucleosynthesis with the Cluster Nucleosynthesis Diagram (CND) proposed before, especially those involving alpha induced reactions, based on our recent works of  $(\alpha,p)$  reactions with low energy RI beams. We present experimental results that alpha resonances play a crucial role for the  $(\alpha,p)$  reaction cross sections. Molecular resonances are also briefly discussed along this line for O- and C-burning.

## 10.3 MeV state



## 13.6 MeV state

## 10.3 MeV state



$|\cos\psi|$  resolution

0.1

0.2

0.4

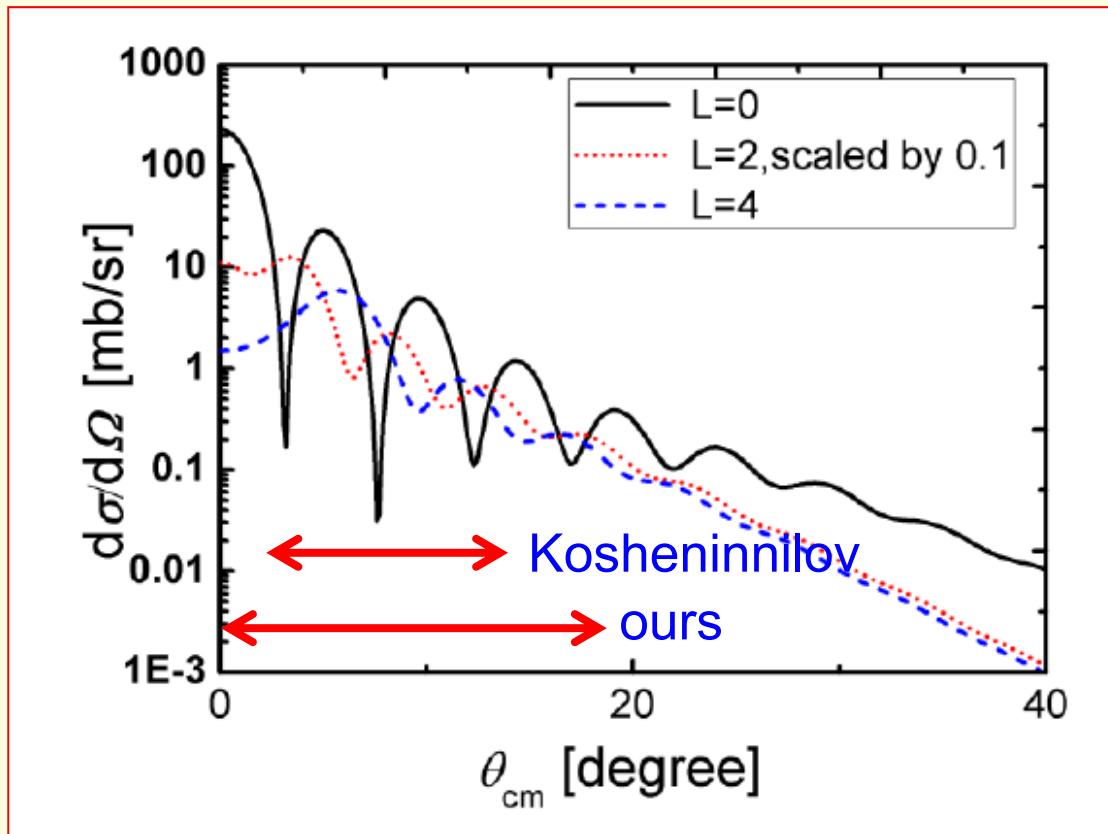
# All possible decay channels

10.3 MeV(0+) state:  $\Gamma = 1.5(2)$  MeV;  $\Gamma = \Gamma_{He} + \Gamma_{Be}$

表格 6.3.2  $^{12}\text{Be}$  各破碎道概率的相空间估算。

反应道	阈值 [MeV]	概率 ( $E_x=15\text{MeV}$ )	概率 ( $E_x=12\text{MeV}$ )	文献结果 [33]
$^4\text{He} + ^8\text{He}$	9. 6	39%	27. 6 %	36 %
$^6\text{He} + ^6\text{He}$	10. 1	21%	13. 1%	19. 3 %
$^4\text{He} + ^6\text{He} + 2\text{n}$	11. 08	0. 19%	1. 1E-3 %	0. 027 %
$^{11}\text{Be} + \text{n}$	3. 17	44. 3%	38. 3%	40. 9 %
$^{10}\text{Be} + 2\text{n}$	3. 67	10. 4%	5. 6 %	3. 7 %
$^9\text{Be} + 3\text{n}$	10. 48	0. 098%	2. 1E-3 %	0. 028 %
$^8\text{Be} + 4\text{n}$	12. 06	6. 9E-5 %	-----	3. 4E-6 %

# Overall dominance of the $0^+$ state



DWBA calculations for the excitation of  $^{12}\text{Be}$  from its ground state to the 10.3 MeV excited state, when interacting with a C target.