



PKU-CUSTIPEN Nuclear Reaction Workshop  
**"Reactions and Spectroscopy  
of Unstable Nuclei"**  
Supported by CUSTIPEN, NSFC, CCAST,  
Peking U, Beijing Normal U.



# Time dependence of the isospin composition of the emission particles in the fission events of Ar+Au at 35 MeV/u

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- ▶ EOS of asymmetric nuclear matter at sub-saturation densities
- ▶ Fission and its possible relevance to  $E_{\text{sym}}(\rho)$

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- ▶ Fission Distributions
- ▶ Spectra Fitting of Light Charged particles

### ▶ New Experiment data

### ▶ Summary



# Symmetry Energy:

Energy cost to convert protons to neutrons in nuclear medium

**Symmetry energy**

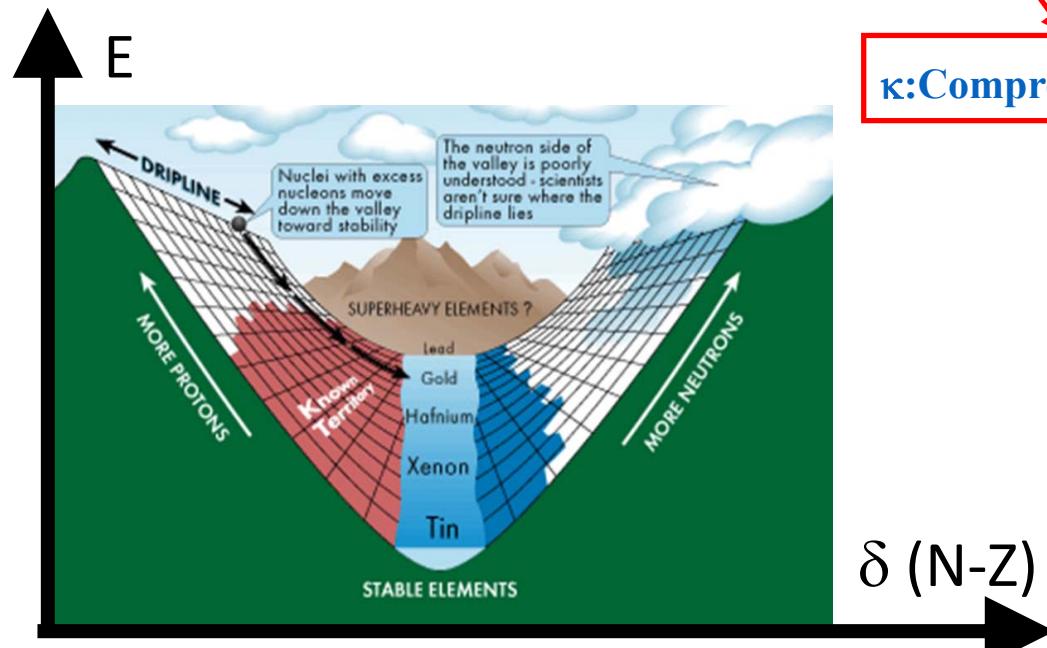
$$E = -a_V A + a_S A^{2/3} + a_C \frac{Z^2}{A^{1/3}} + a_a \frac{(N-Z)^2}{A} + E_{\text{mic}}$$

$$a_V = 16 \text{ MeV} \quad a_S = 18 \text{ MeV} \quad a_a = 21 \text{ MeV} \quad a_C = 0.7 \text{ MeV}$$

$$E(\rho, \delta) = E_0(\rho) + \delta^2 E_{\text{sym}}(\rho) = a_V + \frac{\kappa}{18} \varepsilon^2 - \frac{\kappa^2}{162} \varepsilon^3 + \dots + \delta^2 \left( E_{\text{sym}} + \frac{L}{3} \varepsilon + \dots \right)$$

$\kappa$ : Compressibility

$E_{\text{sym}}$



$$E_{\text{sym}}(\rho) = E_{\text{sym}}(\rho_0) \left( \frac{\rho}{\rho_0} \right)^\gamma$$

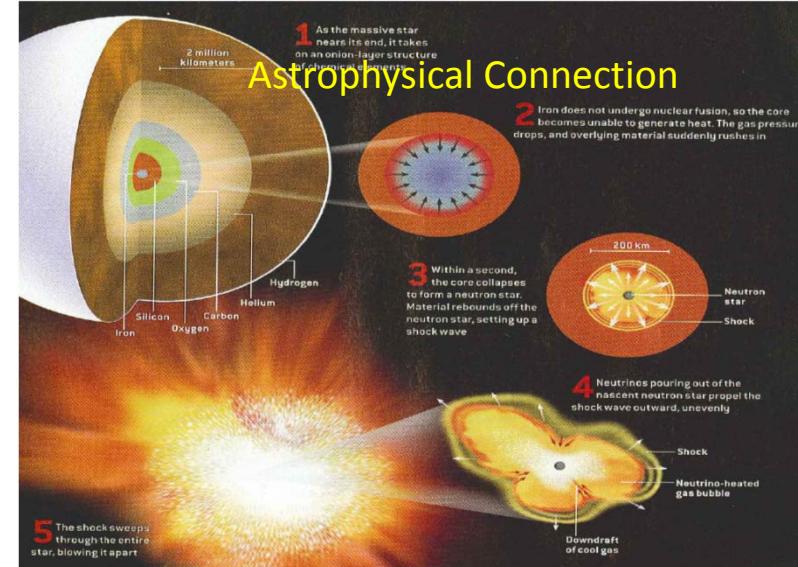
$$\delta = \frac{N - Z}{N + Z}$$



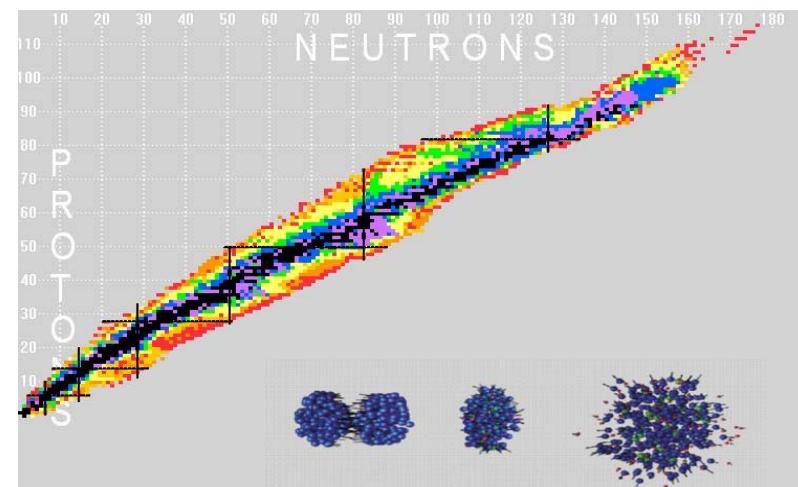
# $E_{\text{sym}}(\rho)$ plays an essential role in astrophysics/nuclear physics

Astrophysics connection  
 → Proton fraction  
 → M-R relation  
 →  $\rho_c$  for D-Urca  
 → Transition density  
 .....  
 ....

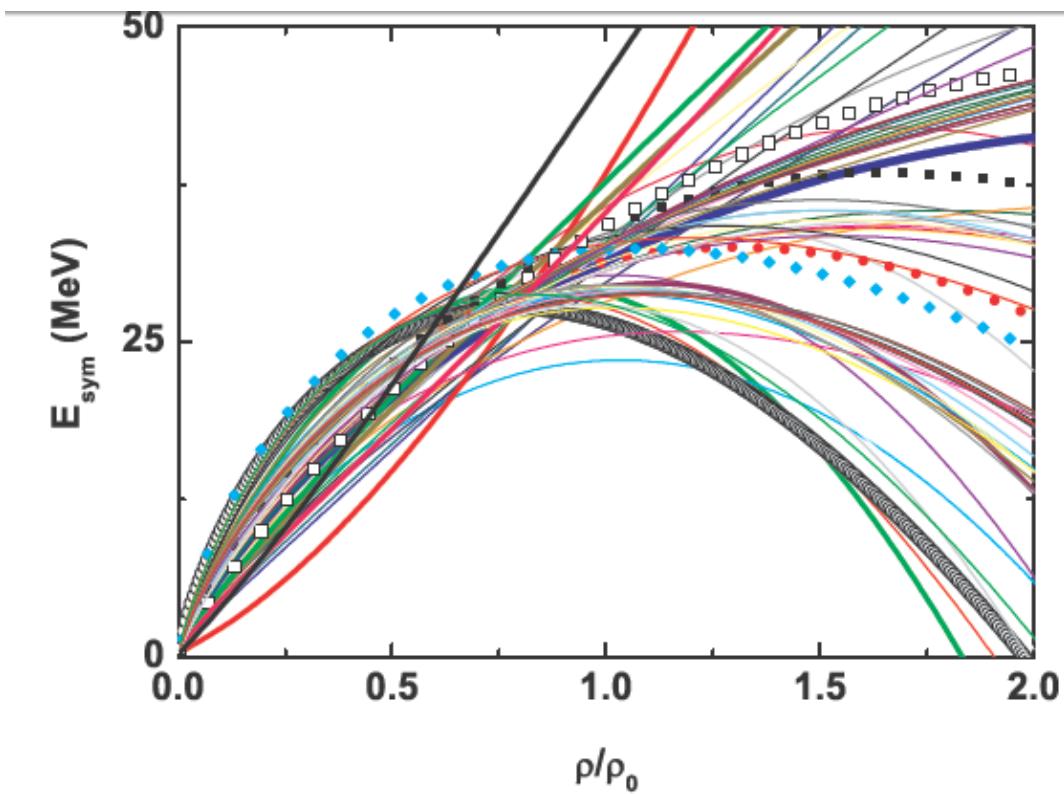
Phy. Rep. 442(2007) 109; NPA777(2006)479  
 PRC76(2007),025801; PRC75(2007) 015801  
 PRC74 (2006),035802; Astro. J. 676 (2008) 1170  
 Phy. Rep. 411(2005) 325; PLB 642, 436 (2006)



Nuclear Physics connection  
 → Nuclear Binding Energy  
 → 3 body force  
 → Tensor force  
 → Collision dynamics...



$E_{\text{sym}}(\rho)$  very uncertain, particularly at  $\rho > \rho_0$



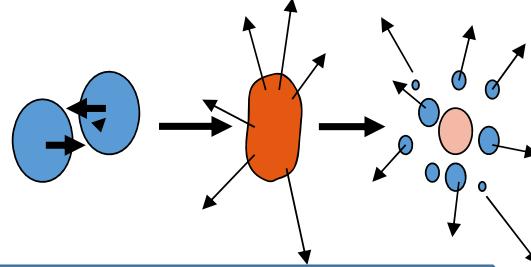
L.W. Chen, C.M. Ko and B.A. Li, Phys. Rev. C72, 064309 (2005); C76, 054316 (2007).

While at sub-saturation densities.....



# A list for sub-saturation density

**At sub-saturation densities**



- Global nucleon optical potential in n/p-A collisions or (p,n) reactions
- Neutron Skin thickness of Pb-208 (PREX experiment at JLAB)
- Isospin scalaring and isospin fractionaiton in multifragmentation
- Isospin diffusion
- n/p ratio of fast and pre-equilibrium nucleons
- N/Z composition of the emitted fragments
- GDR strength
- Correlation function
- .... ....

$$S_0 = 32.5 \pm 2.5 \text{ MeV} \quad L = 55 \pm 25 \text{ MeV}$$

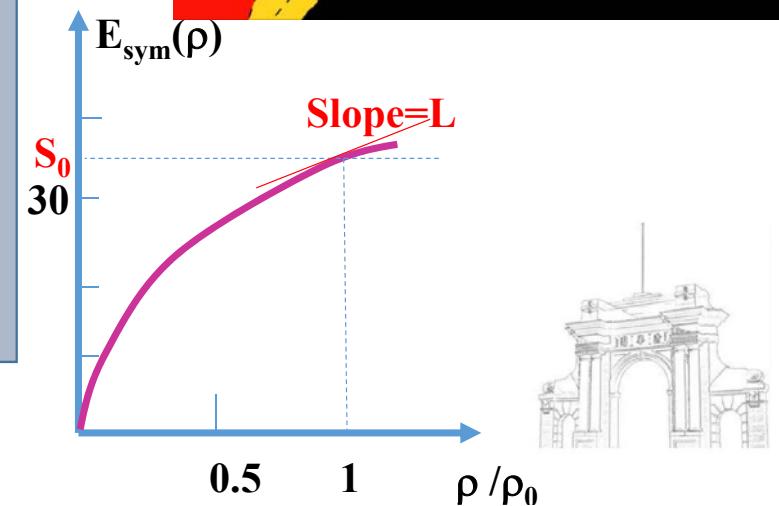
Topical Issue on Nuclear Symmetry Energy  
edited by Bao-An Li, Àngels Ramos,  
Giuseppe Verde and Isaac Vidaña

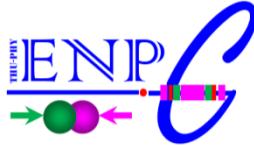
**Astro-physics**

From: Constraints on the symmetry energy  
using the mass-radius relation of neutron stars  
by James M. Lattimer and Andrew W. Steiner



Springer





# How long the $E_{\text{sym}}$ effects can persist in HIC?

Neutron Skin

Isospin scaling

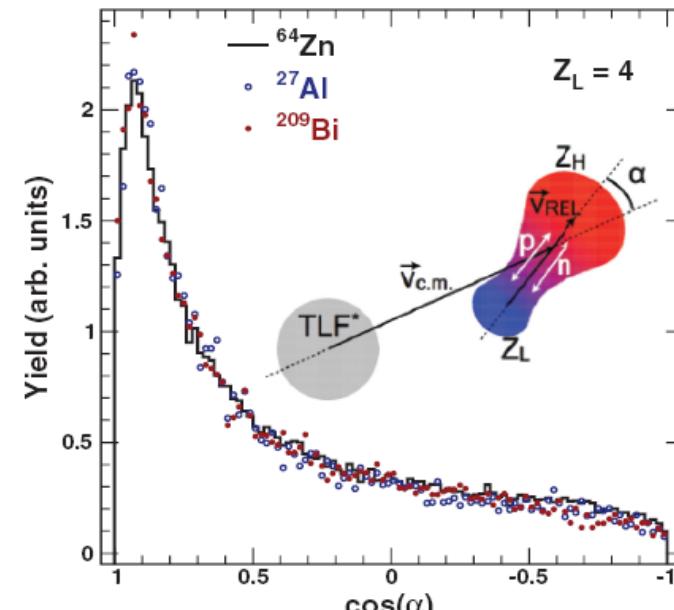
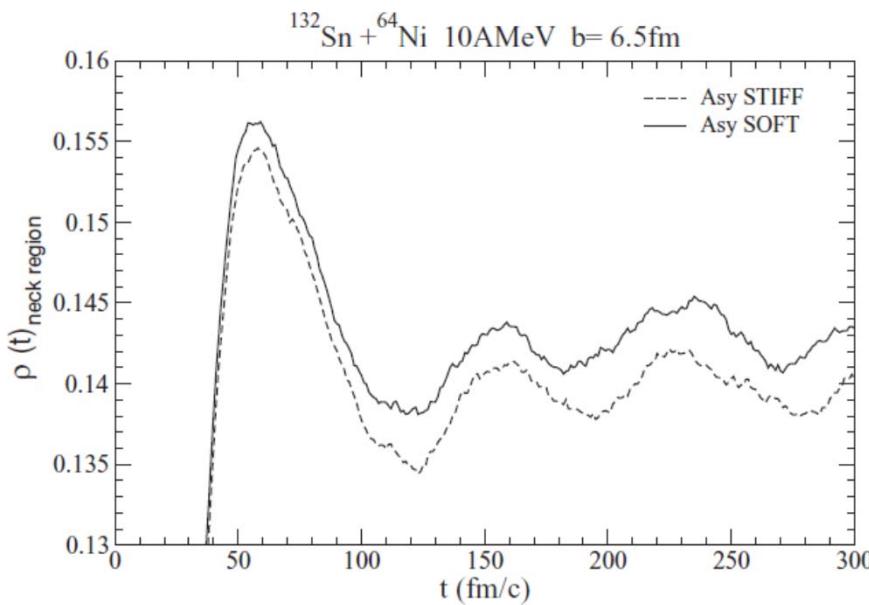
SLOW

$10^{-19} \text{ s}$

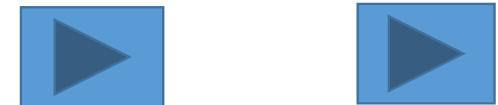
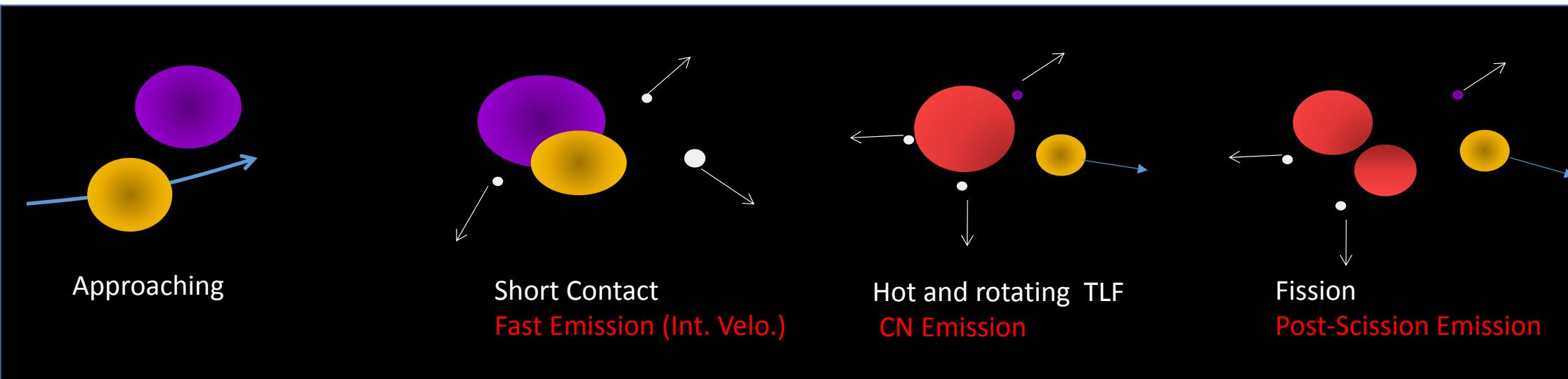
Intermediate Process ?

FAST

$10^{-21 \sim 22} \text{ s}$



# Using fission to study the long time effect of $E_{\text{sym}}(\rho)$



**Animation by Tian Junong**

- Possible Advantages:
- Neck part: Very neutron rich, Low Densities
- Time Scale: Between statistical emission (Q effect) and two body process (very short)

One Step backward: Isospin effect of the particle emission



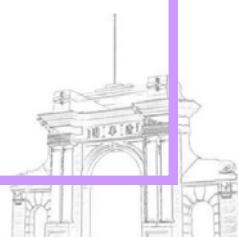
## ▼ Content

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### ▼ Experiment and Results

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- ▶ Spectra Fitting of Light Charged particles
- ▶ Future experiment



# Experimental Set Up

- 35 MeV/u Ar+ Au.
- Trigger: 2 fold fragments .AND. 1 LCP
- 2 fold fragments .AND. 1 Proj.-like

- 1) Six PPAC covering ~1/3 whole space
- 2) All about 30 cm to the target
- 3) 3 Si-CsI and 3 Si-Si-CsI (158,127,80) telescopes
- 4) One 12-unit Si-BGO hodoscope

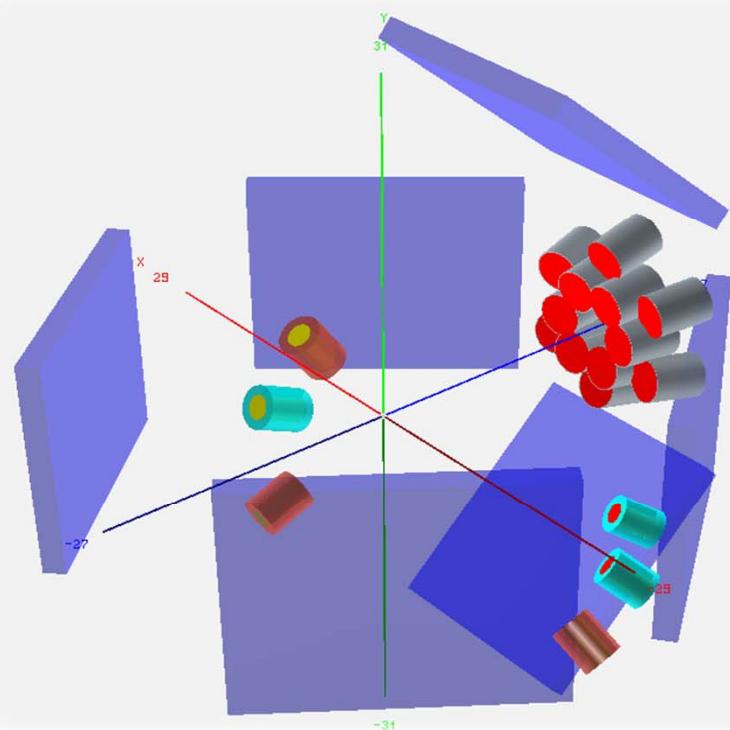
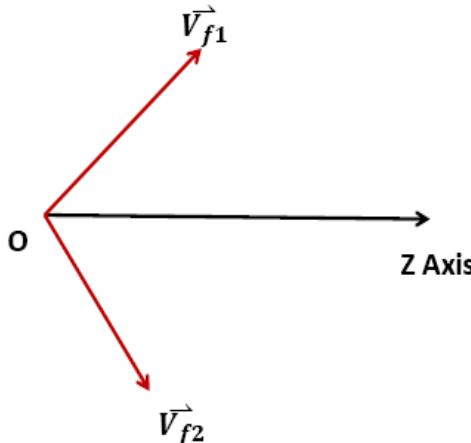


TABLE I: The parameters of the 6 LCP telescopes

Tele. No.	1	2	3	4	5	6
$d$ (mm)	12.0	10.2	10.4	14.0	14.0	14.0
$L$ (cm)	11.5	11.5	11.5	26.0	21.6	28.5
$\theta$ ( $^{\circ}$ )	158	155	127	80	59	44
$\phi$ ( $^{\circ}$ )	-90	90	90	-145	-139	-133
$\Delta E_1$ ( $\mu$ m)	50	50	50	50	50	50
$\Delta E_2$ ( $\mu$ m)	400	/	400	400	/	/
$E_{\text{CsI}}$ (mm)	40	40	40	40	40	40

# Fission Event Measurement and Reconstruction



$$\frac{m_{f1}}{m_{f2}} = \frac{|V_{f2}|_\perp}{|V_{f1}|_\perp}$$

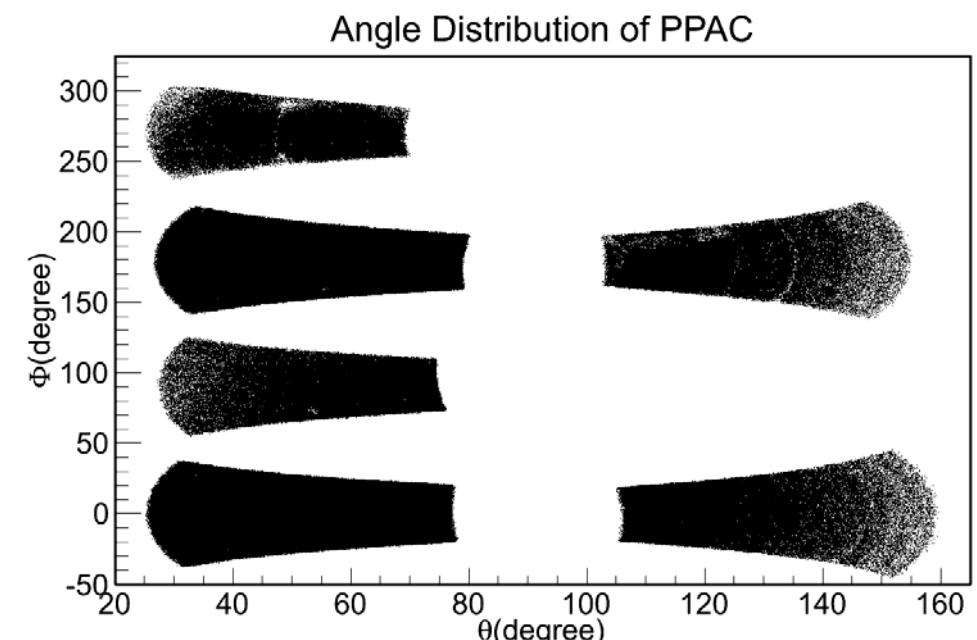
$$m_{CN} = m_{f1} + m_{f2}$$

$$m_{CN} \vec{V}_{CN} = m_{f1} \vec{V}_{f1} + m_{f2} \vec{V}_{f2}$$

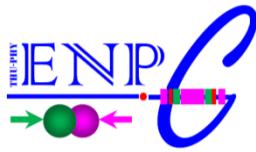
$$\vec{V}_{CN} = \frac{m_{f1} \vec{V}_{f1} + m_{f2} \vec{V}_{f2}}{m_{f1} + m_{f2}}$$

$$\eta = \frac{1 - \frac{m_{f2}}{m_{f1}}}{1 + \frac{m_{f2}}{m_{f1}}}$$

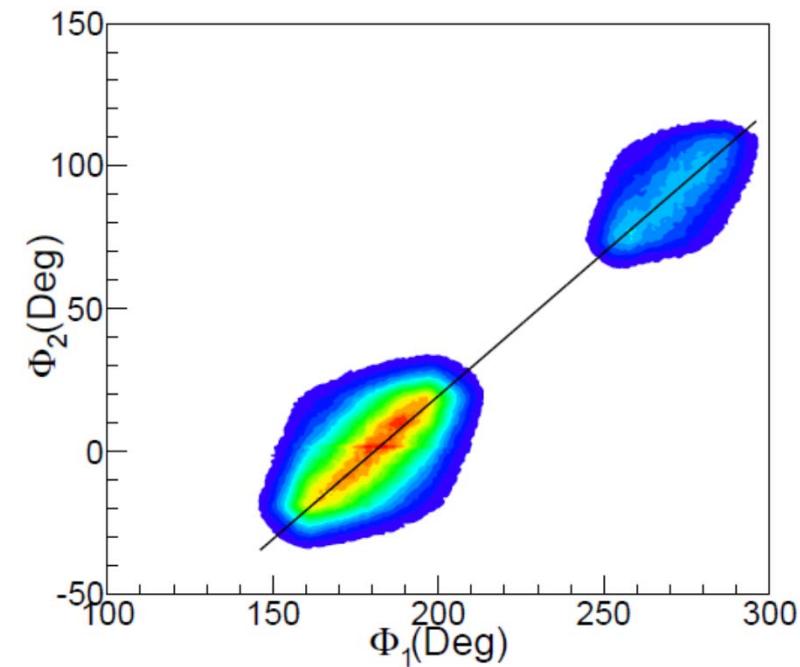
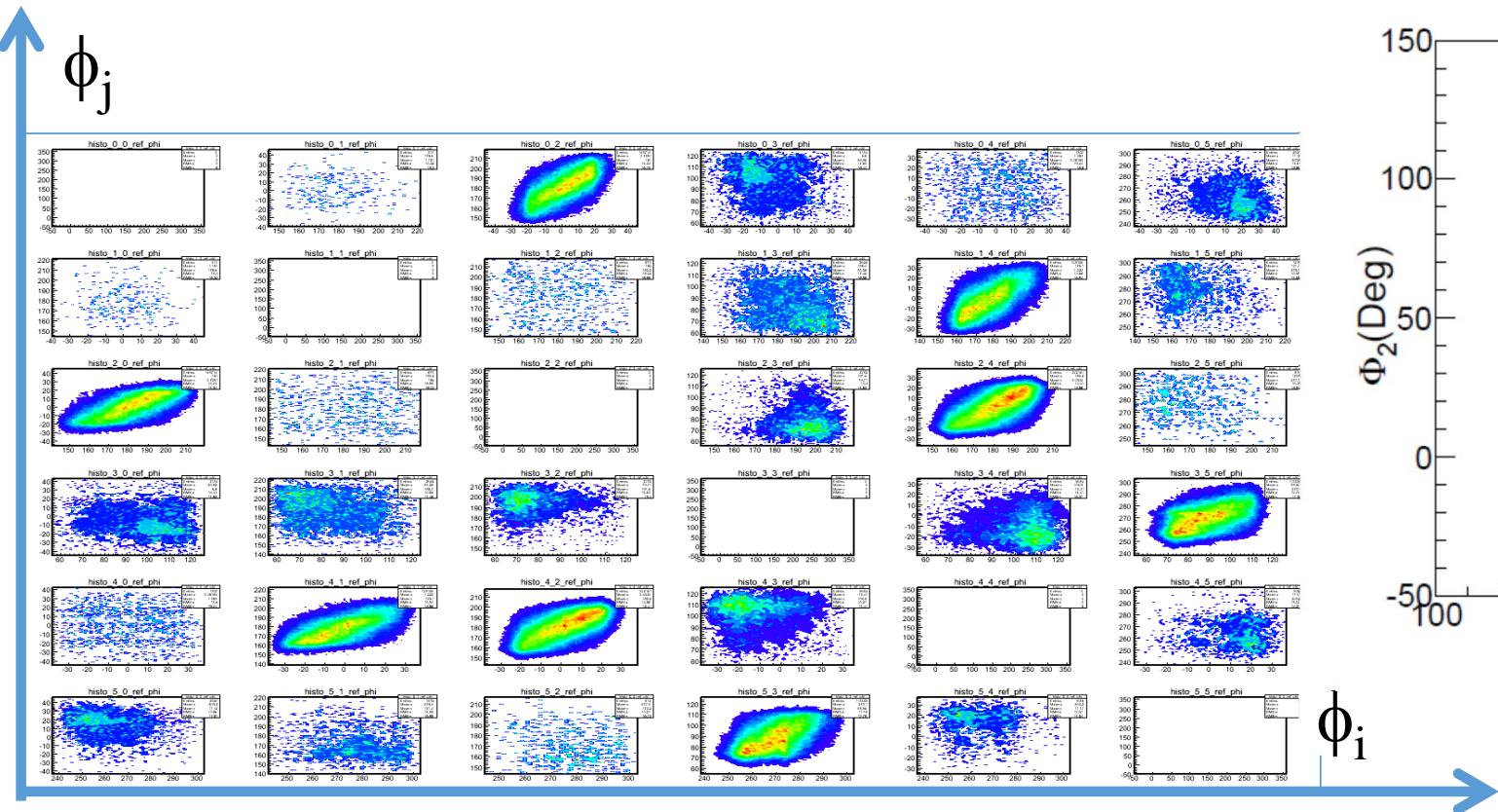
$$\vec{V}_{CN} = \frac{\vec{V}_{f1} + \frac{m_{f2}}{m_{f1}} \vec{V}_{f2}}{1 + \frac{m_{f2}}{m_{f1}}}$$



- Folding angle method → velocity of fragments, mass ratio ...

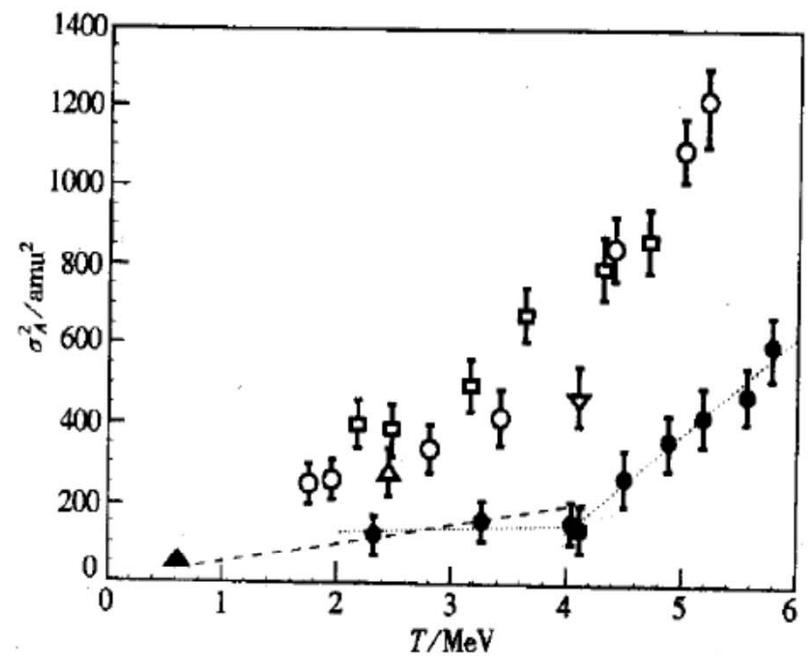
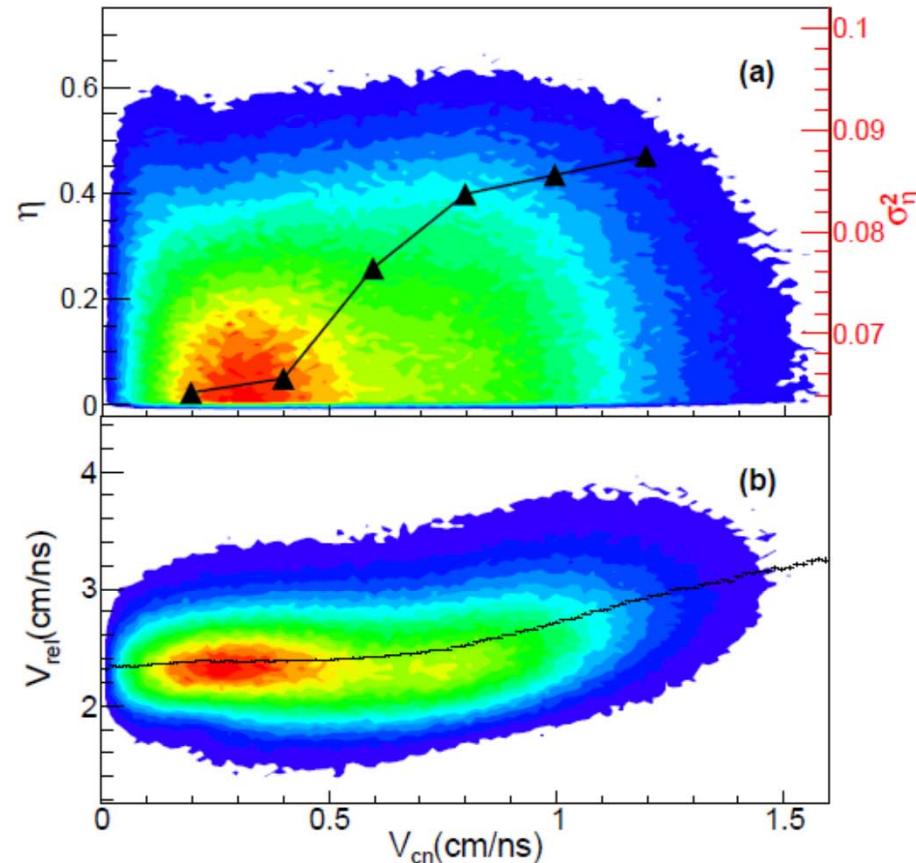


# 1) Fission fragments correlation



- 2-fold events with face-to-face PPACs fired show good back-to-back correlation!

# Fission Distribution

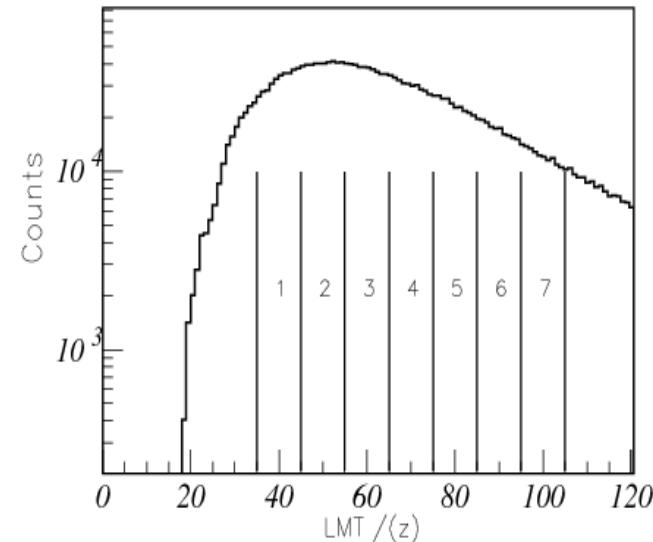
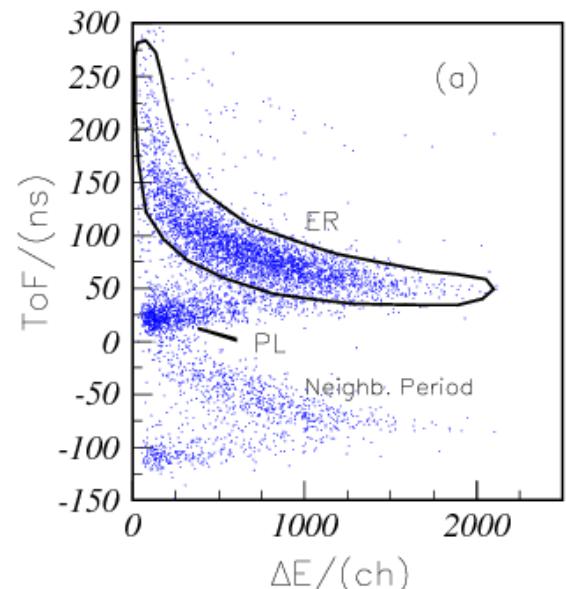
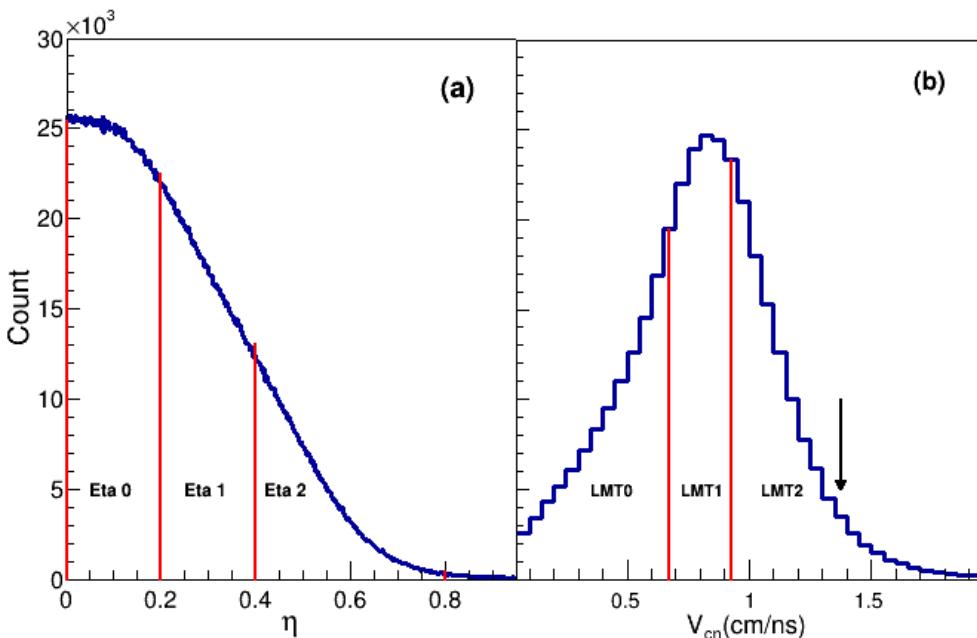


S. Harar, Nucl. Phys. A 471, 205c (1987)  
 J. W. Zheng et al, HEPNP. 23, 409 (1999)

- 1) Relative velocity peaks at 2.4 (Viola systematics), and showing slight asymmetry
- 2) At low and high  $V_{\text{add}}$ , the relative velocity exhibits different manner



# LMT 同文献的比较



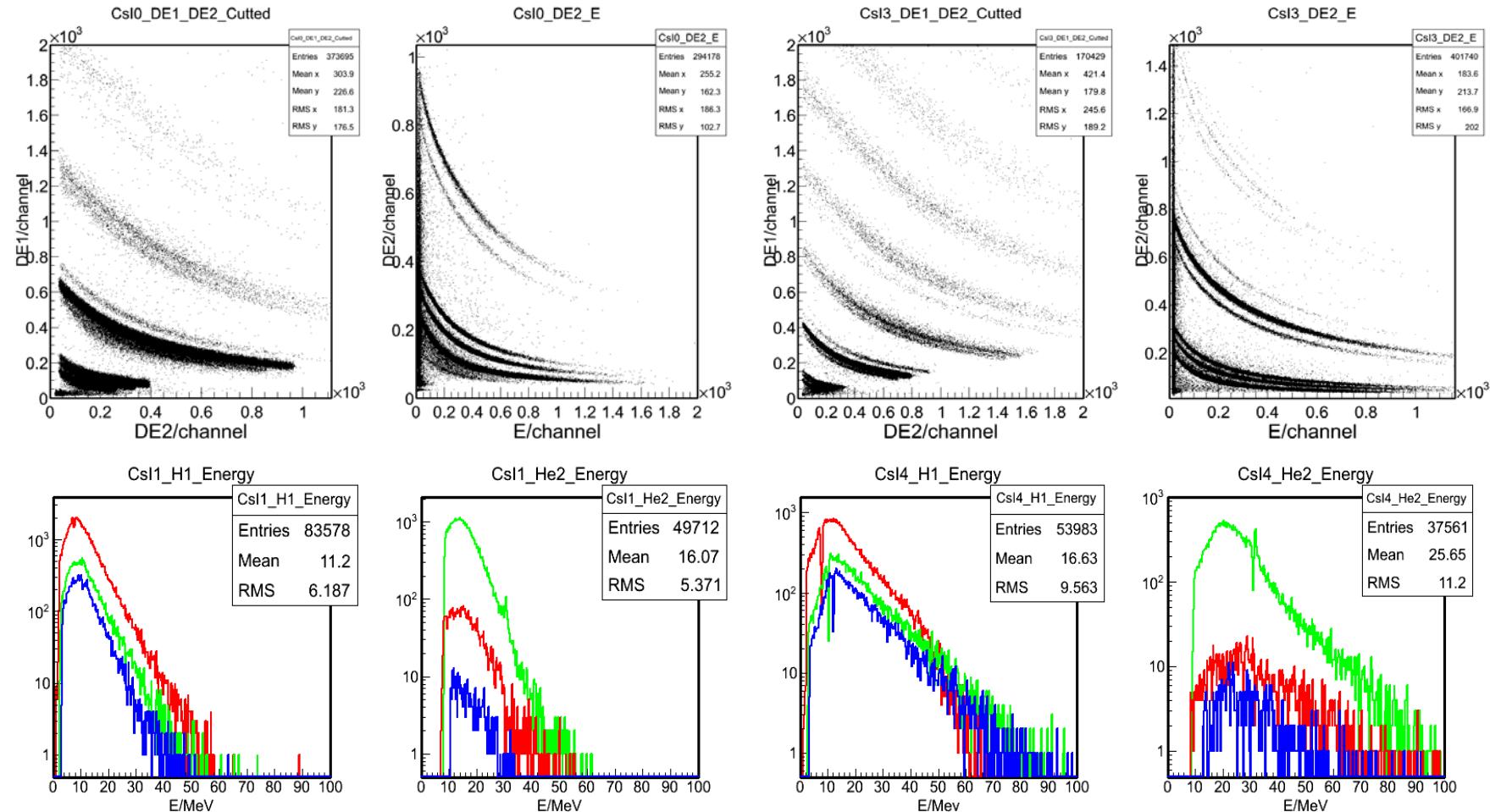
Z. G. Xiao, et al., HEPNP. 25, 643 (2001)

$$\langle LMT \rangle = \begin{cases} 1.273 - 0.092\sqrt{E_{in}/A} & \sqrt{E_{in}/A} > 3.2(\text{MeV/u})^{1/2} \\ 1 & \sqrt{E_{in}/A} \leq 3.2(\text{MeV/u})^{1/2} \end{cases}$$

- LMT most probable at 0.56, consistent with Ar+Sn at 35 MeV/u.
- Slightly deviate from the empirical prediction at 0.72, presumably the beam energy exceeds the range.

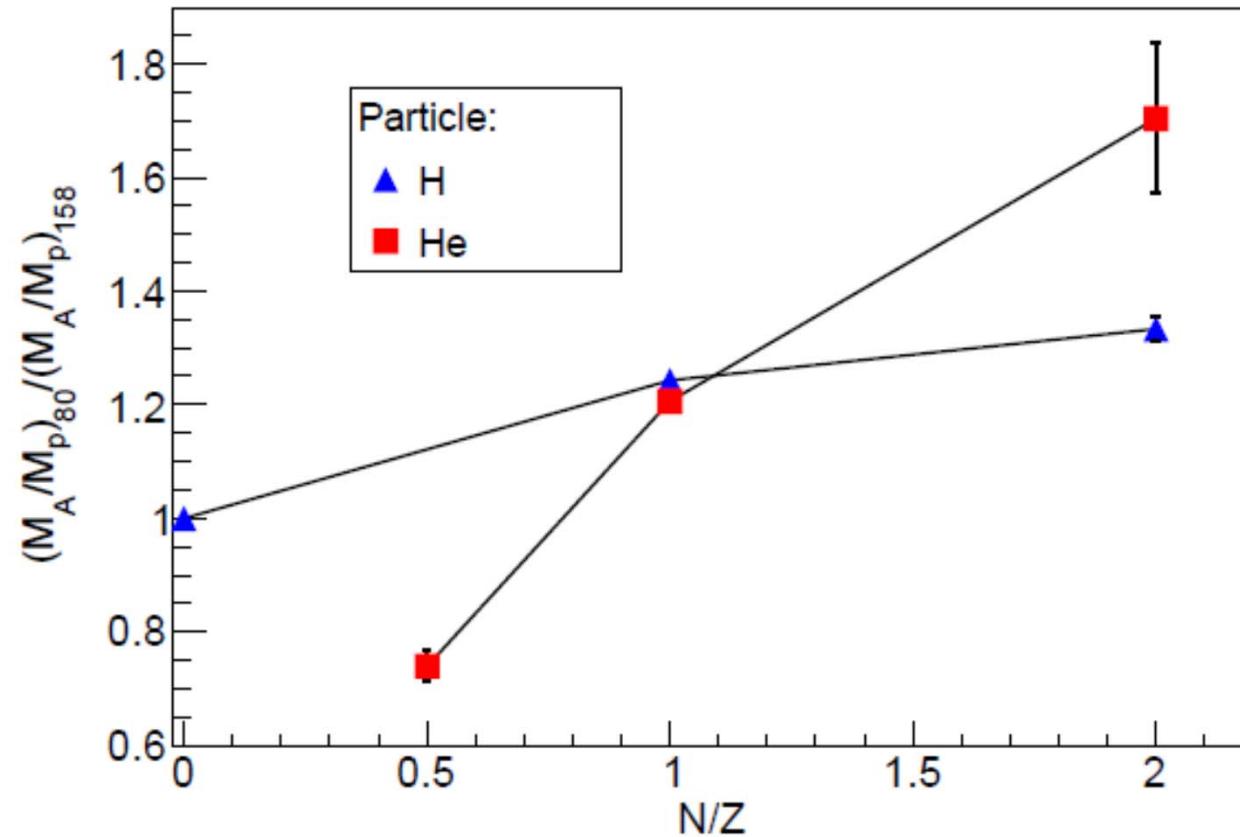


# LCPs in coincidence with fission



- Mass Resolved spectra obtained at 2 degrees: 158, 80

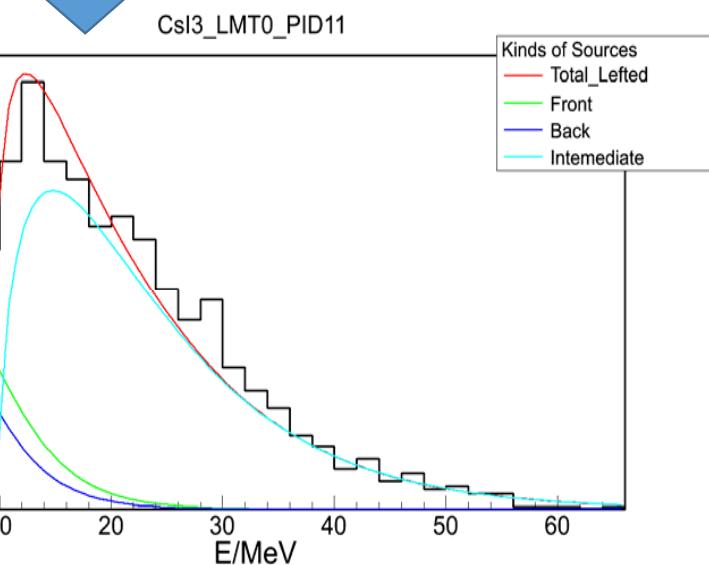
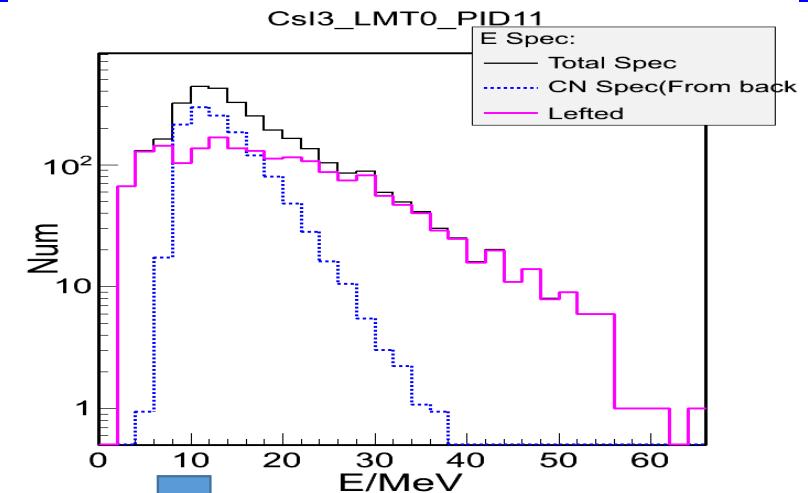
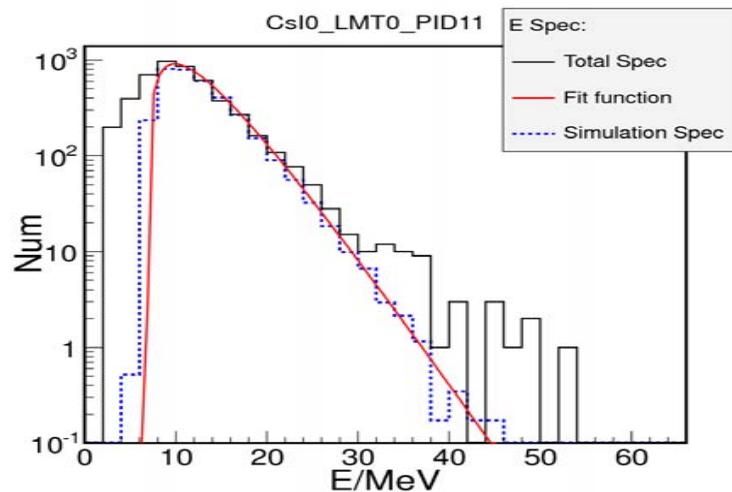
# Double angular ratio of particle yield



- Model independently, particles emitted at smaller angle are more neutron rich
- Smaller angle emitted particles experience more dynamical contribution



# Three moving source analysis



- Three moving source: CN, FF and Int. Velocity

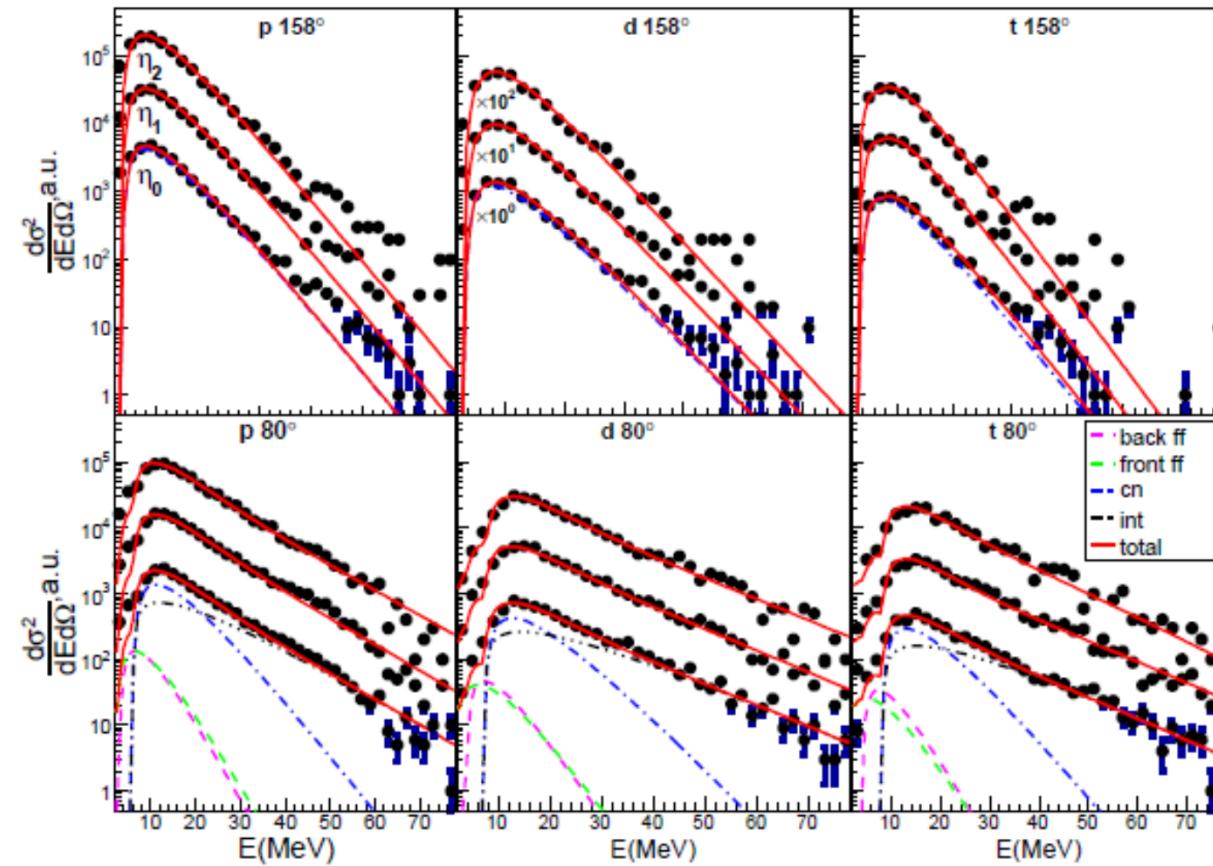
$$\frac{d^2\sigma}{d\Omega dE} = \frac{N}{2(\pi T)^{3/2}} (E - E_c)^{1/2} \exp [-(E - E_c)/T]$$

**STEP 1:** Fit large angle telescope with CN source

**STEP 2:** Apply the CN parameters to the middle angle detector

**STEP 3:** Fit the middle angle spectrum

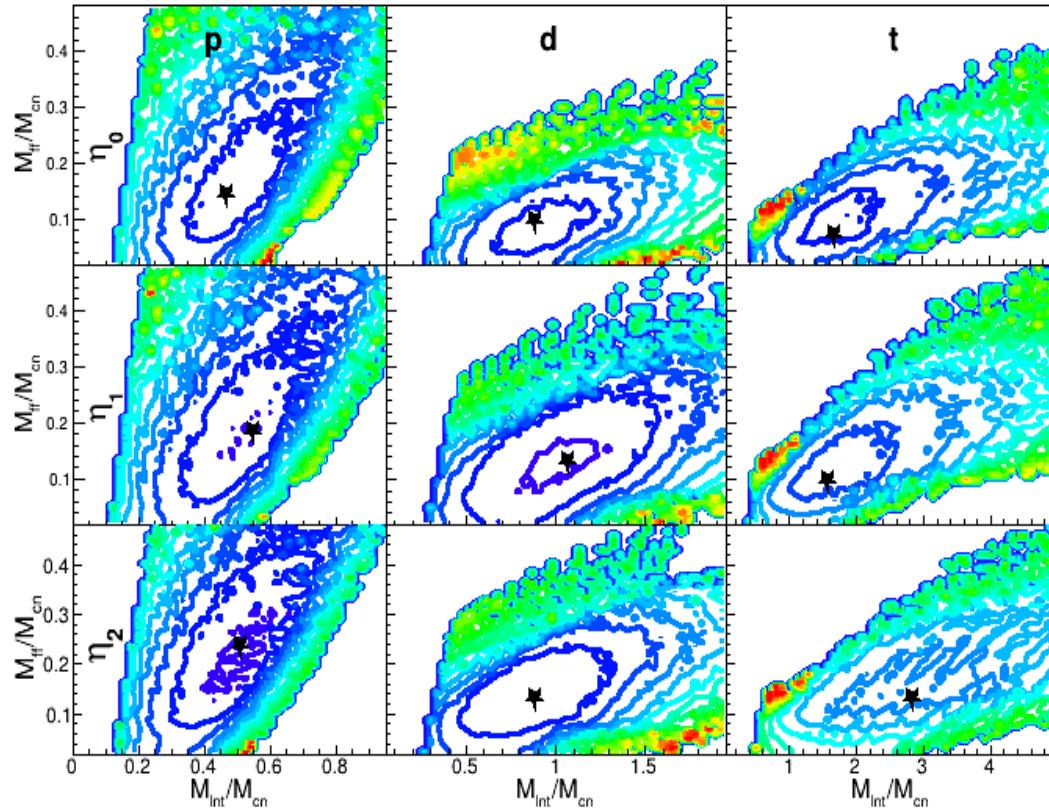
# Energy spectra analysis vs mass asymmetry



$$\frac{d^2\sigma}{d\Omega dE} = \frac{N}{2(\pi T)^{3/2}} (E - E_c)^{1/2} \exp [-(E - E_c)/T]$$



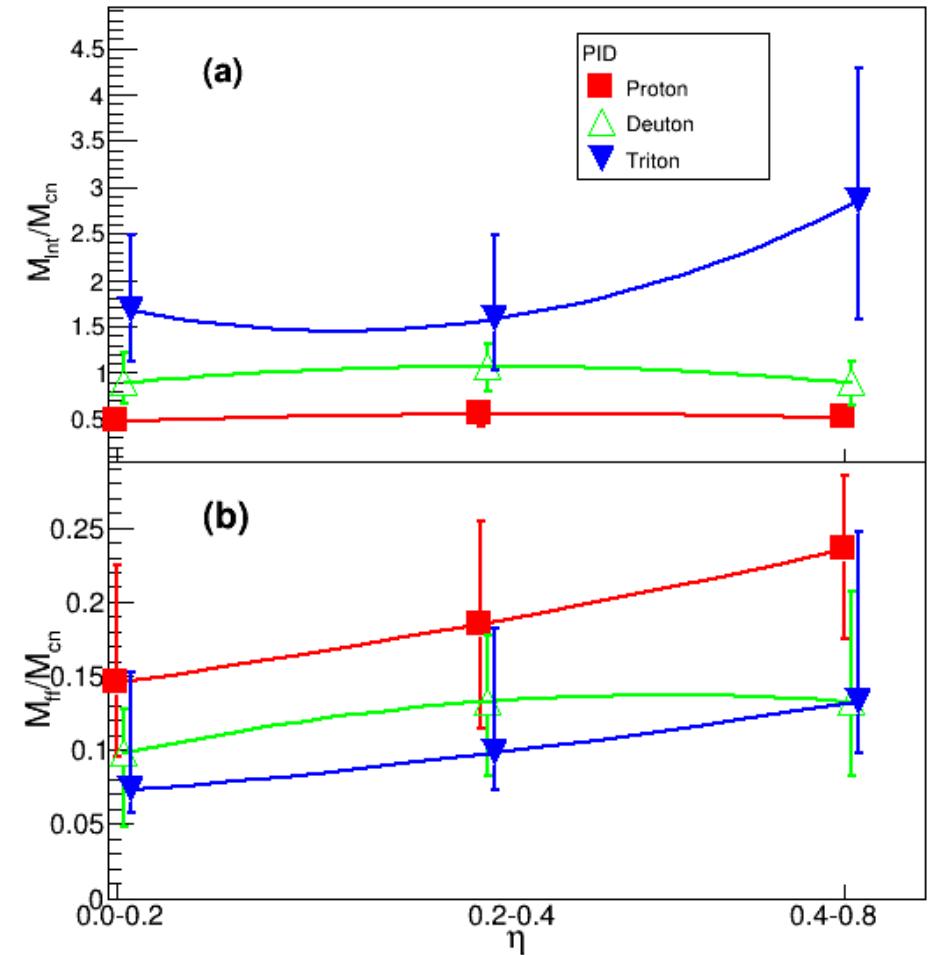
# Minimum $\chi^2$ analysis



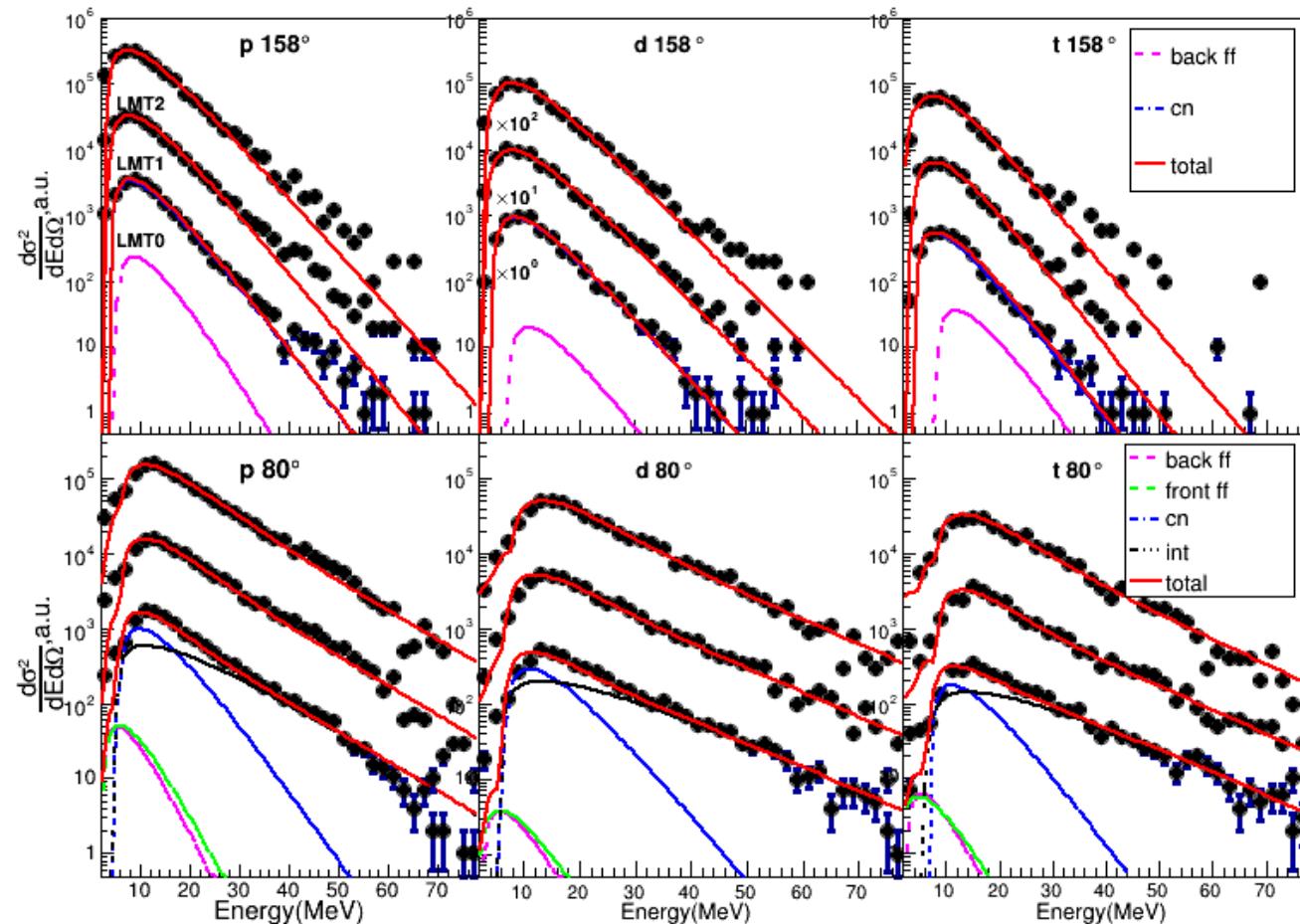
→  $M_{ff}/M_{cn}$  vs.  $M_{inv}/M_{cn}$

→ The two ratios show different hierarchy

→ **The particles emitted in early stage are neutron rich!**



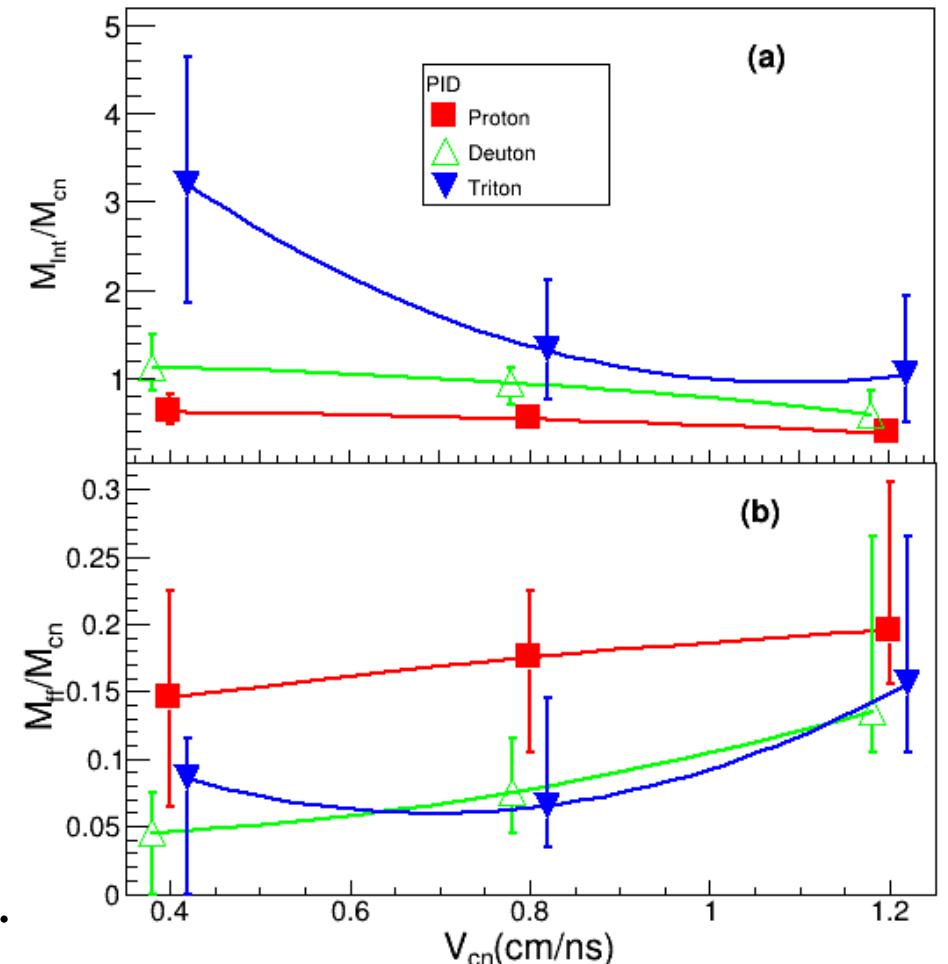
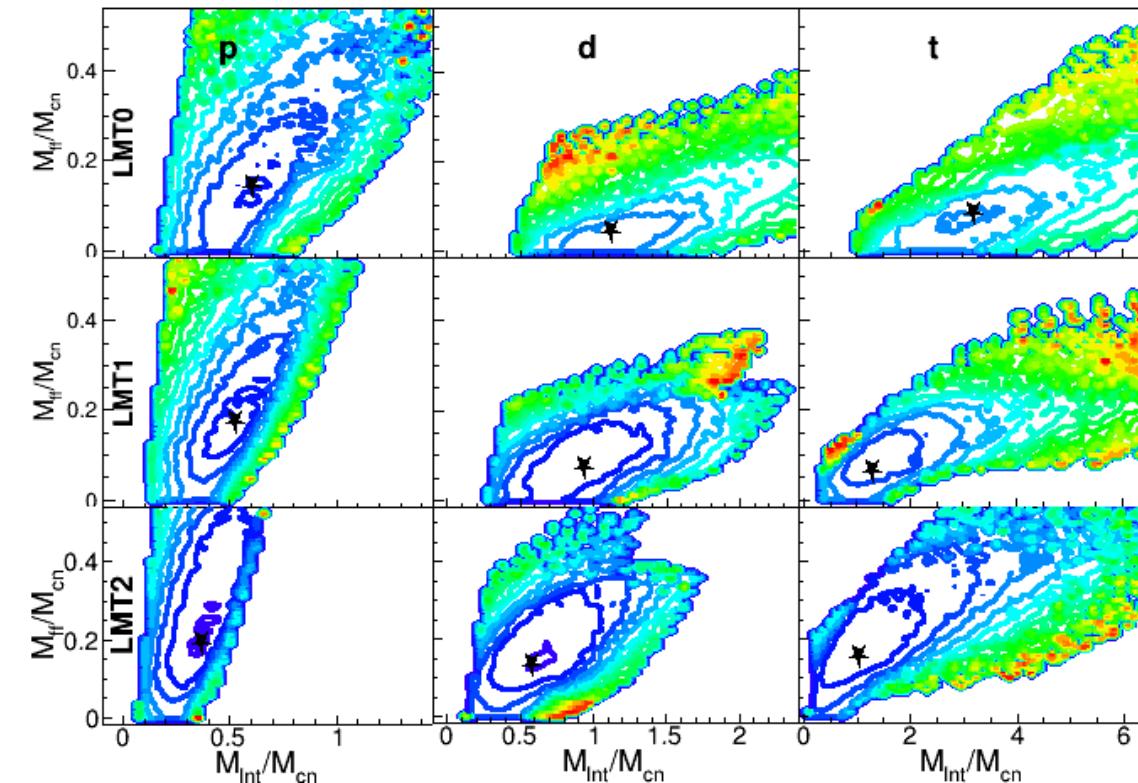
# Energy spectra vs. LMT



- As a function of LMT



# Minimum $\chi^2$ analysis

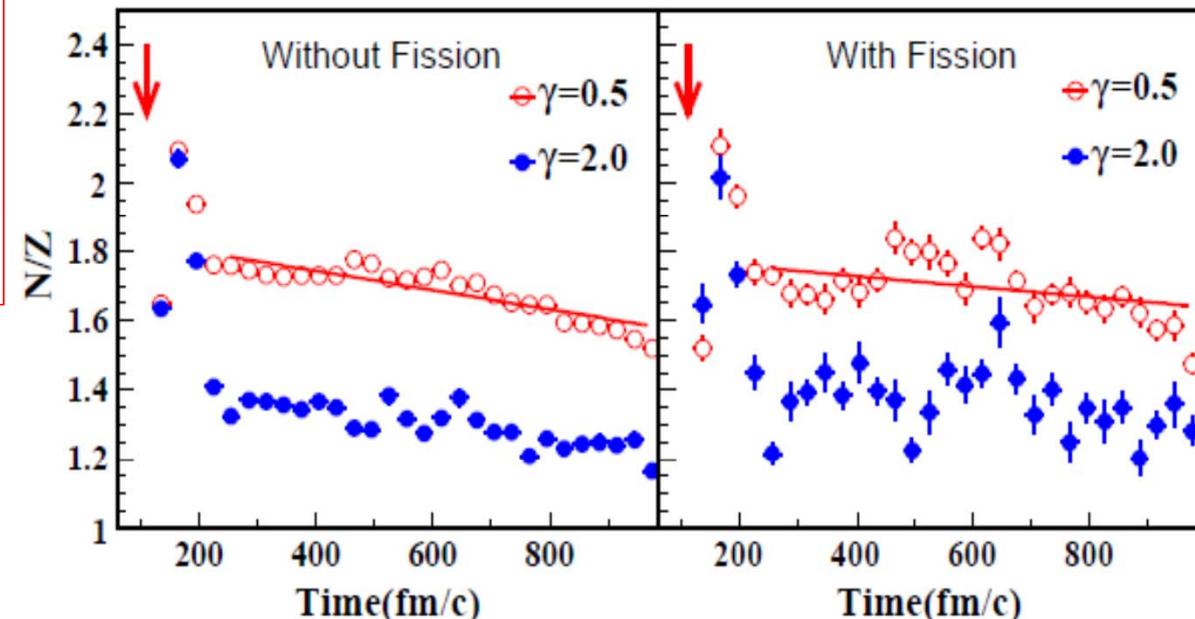


- The hierarchy of Multiplicity ratio remains.
- Error bars are large for the FF source.

# IQMD calculations

$$V_{\text{loc}} = \frac{\alpha}{2} \frac{\rho^2}{\rho_0} + \frac{\beta}{\sigma+1} \frac{\rho^{\sigma+1}}{\rho_0^\sigma} + \frac{g_0}{2\rho_0} (\nabla \rho)^2 + \frac{C_s}{2} \left[ \frac{\rho^{\gamma+1}}{\rho_0^\gamma} - \frac{\kappa_s}{\rho_0} (\nabla \rho)^2 \right] \delta^2 + g_\tau \frac{\rho^{\eta+1}}{\rho_0^\eta}$$

$\alpha$	207 MeV	$\beta$	138 MeV
$\sigma$	7/6	$g_0$	18 MeV · fm <sup>2</sup>
$C_s$	32 MeV	$\kappa_s$	0.08 fm <sup>2</sup>
$g_\tau$	14 MeV	$\eta$	5/3



1) Along the whole decay chain, the average N/Z decreases with time.

→ **The neutron richness of the emitted particles is enhanced at the beginning of the emission.**

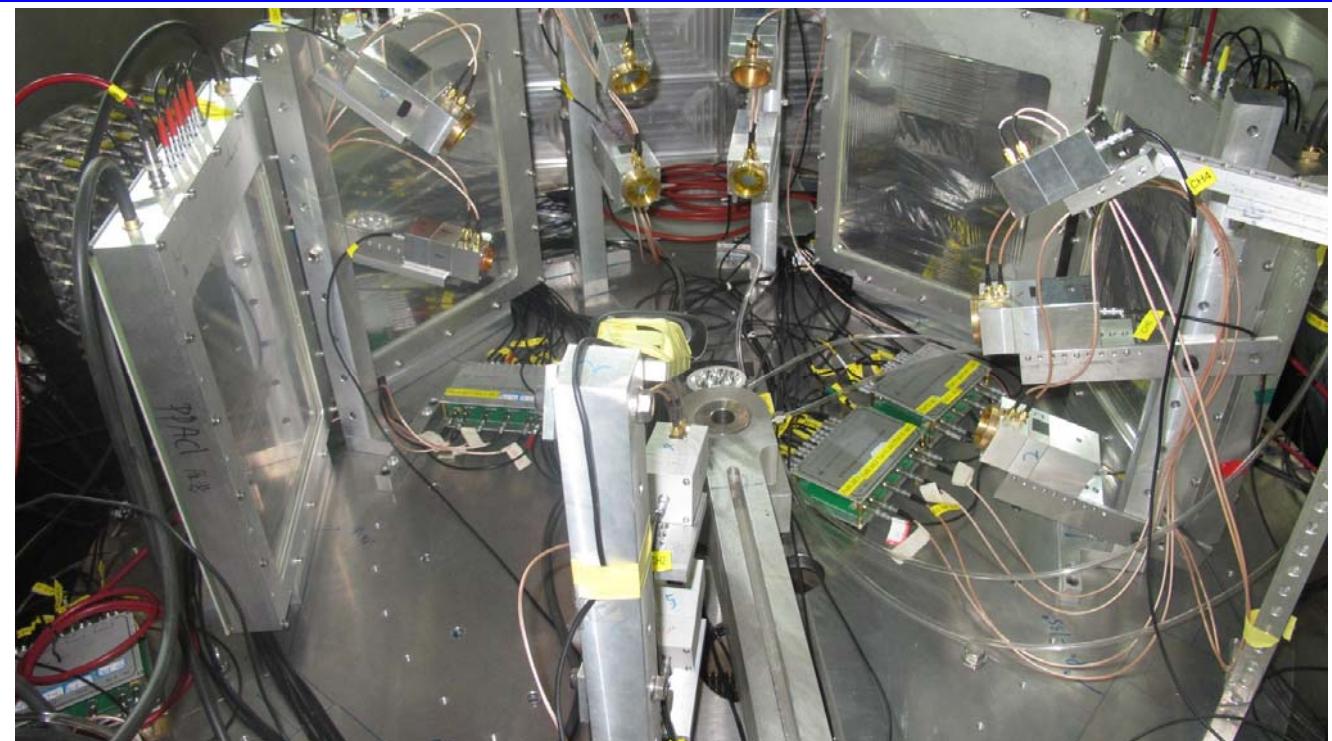
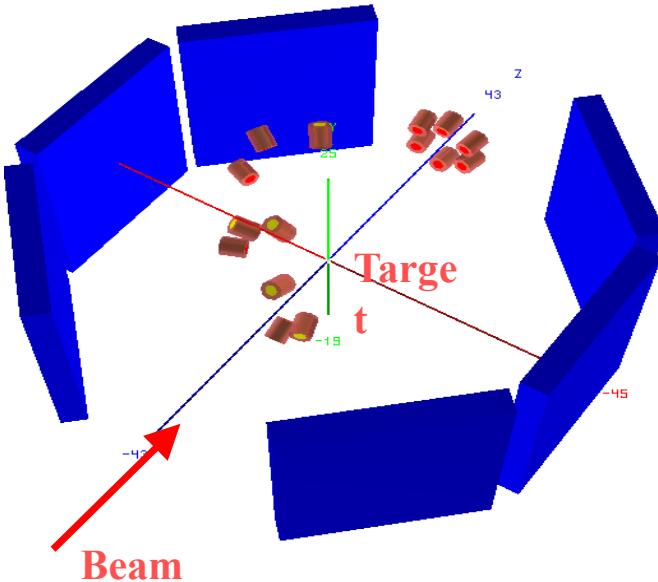
2) The isospin composition N/Z exhibits an obvious dependence on  $E_{\text{sym}}(\rho)$  till very late stage.

3) The effect of the symmetry energy remains equally significant in the fission.

→ **Scission point can be a clock to investigate the effect of  $E_{\text{sym}}(\rho)$ .**

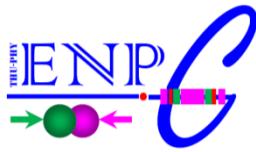


# Further improved experiment

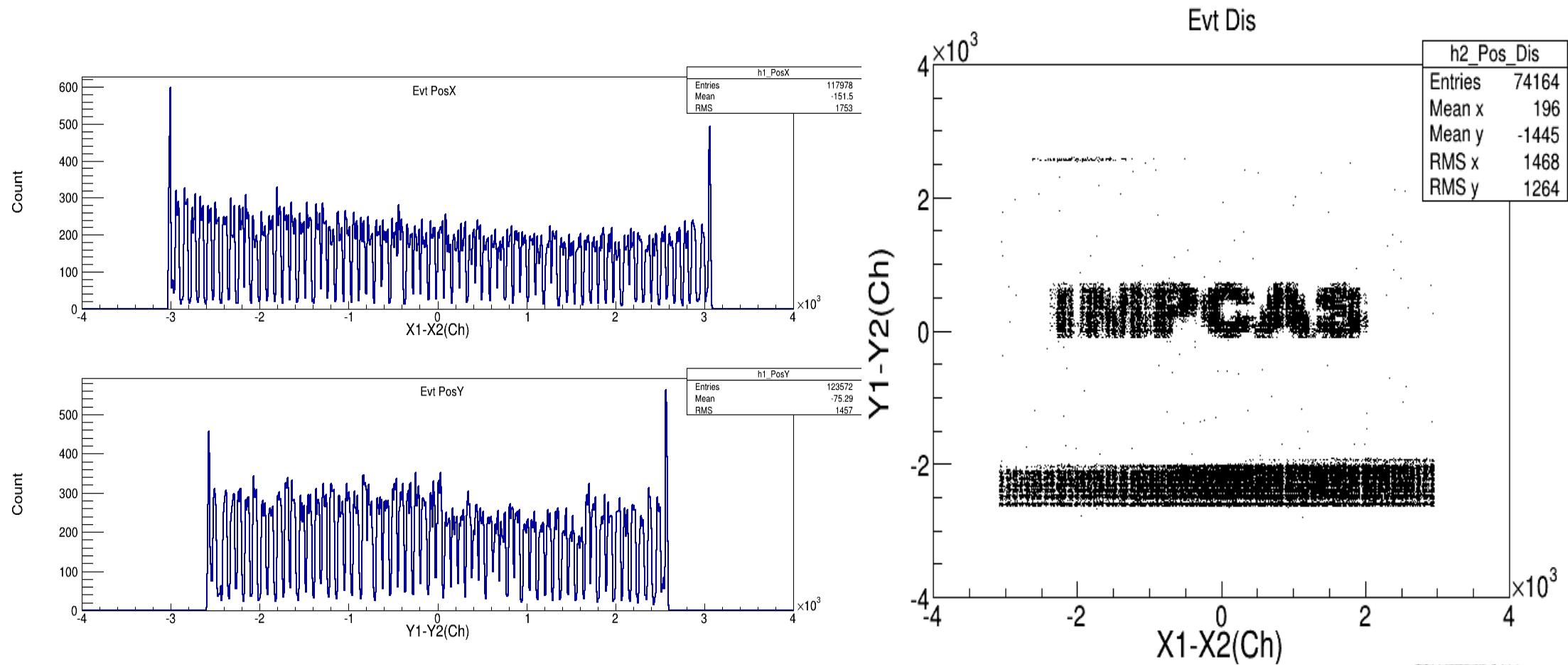


- **Complete in June 2014.**

1. Improved PID by using H.Q. telescopes
2. Lower energy threshold
3. More Detectors(> 5 positions)

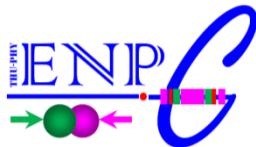


# PPAC Performance

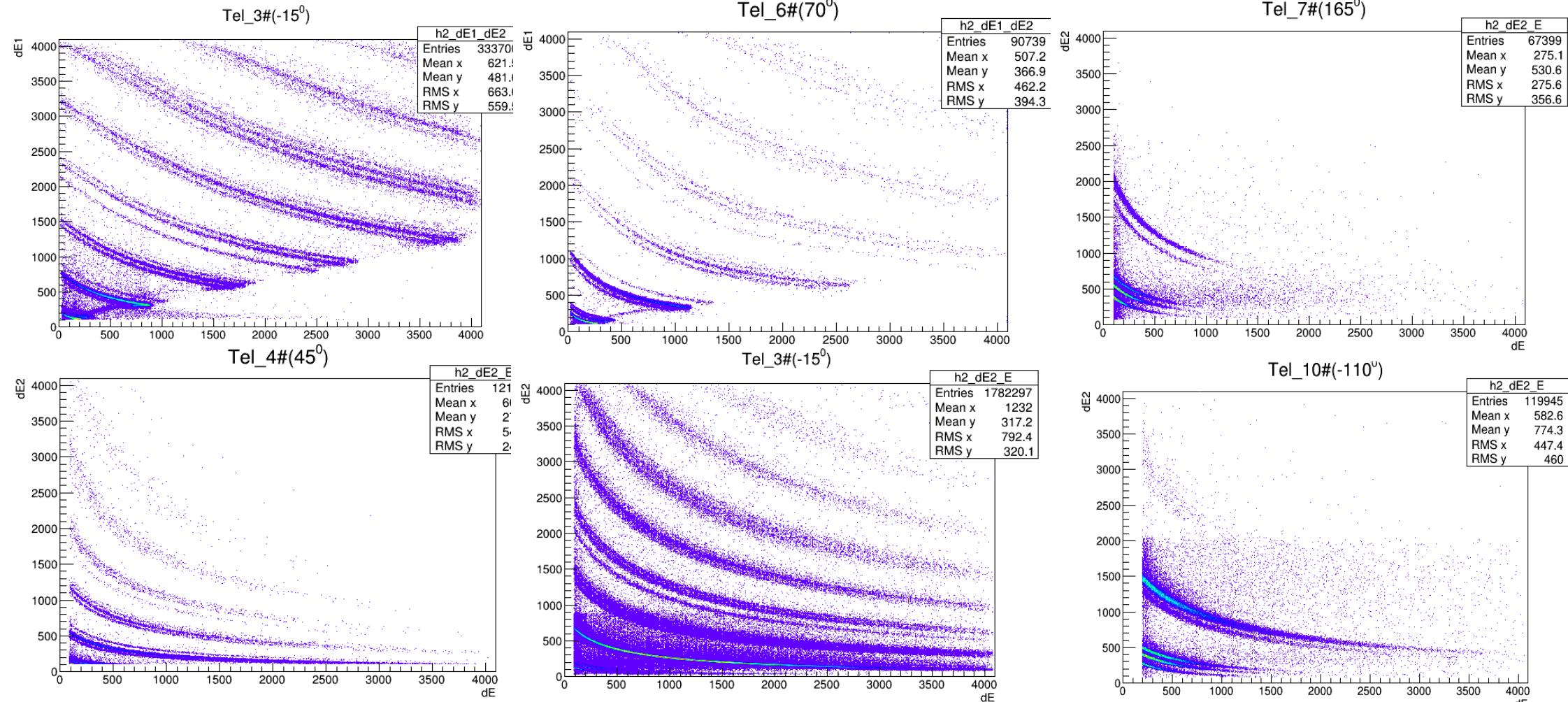


- Good Position Resolution and high fission fragment efficiency

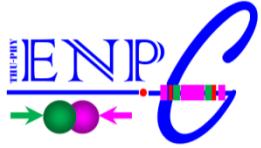




# Telescope Performance



- Isotope identification achieved in most of the telescopes → More angles

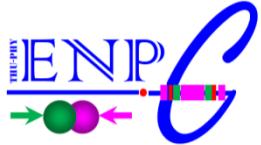


# Summary

- In 35 MeV/u  $^{40}\text{Ar}+^{197}\text{Au}$  collisions:
  - LCPs are measured in coincidence with fission events
  - Smaller angle products, with more contribution from dynamic emissions, are more neutron rich. A hierarchy from t to d and p are observed for the dynamic emissions, later emissions exhibit the inverse trend.
  - Effect of the symmetry energy persists to very late stage. Process with long time scale is sensitive to the underlying effect of the symmetry potential. The time dependent N/Z of the light charged particles can be used as a new probe to  $E_{\text{sym}}(\rho)$
  - Further experimental studies are of interest.

Please refer to R. Wang et al, *Phys. Rev. C* **89**, 064613 (2014)





# Acknowledgements

## Collaborators

THU: R. S. Wang, Y. Zhang, H. Yi, L. M. Lv,  
Y. Huang, W. J. Cheng, H. J. Li

IMP: G. M. Jin, L. M. Duan, R. J. Hu, H. R. Yang,  
Y. P. Zhang, J. S. Wang, P. Ma, Y. J. Zhou,  
Y. Y. Yang, S. L. Jin.....

CIAE: [Y. X. Zhang, Q. H. Wu](#)

ATC: [J. L. Tian](#)

MSU: B. Tsang

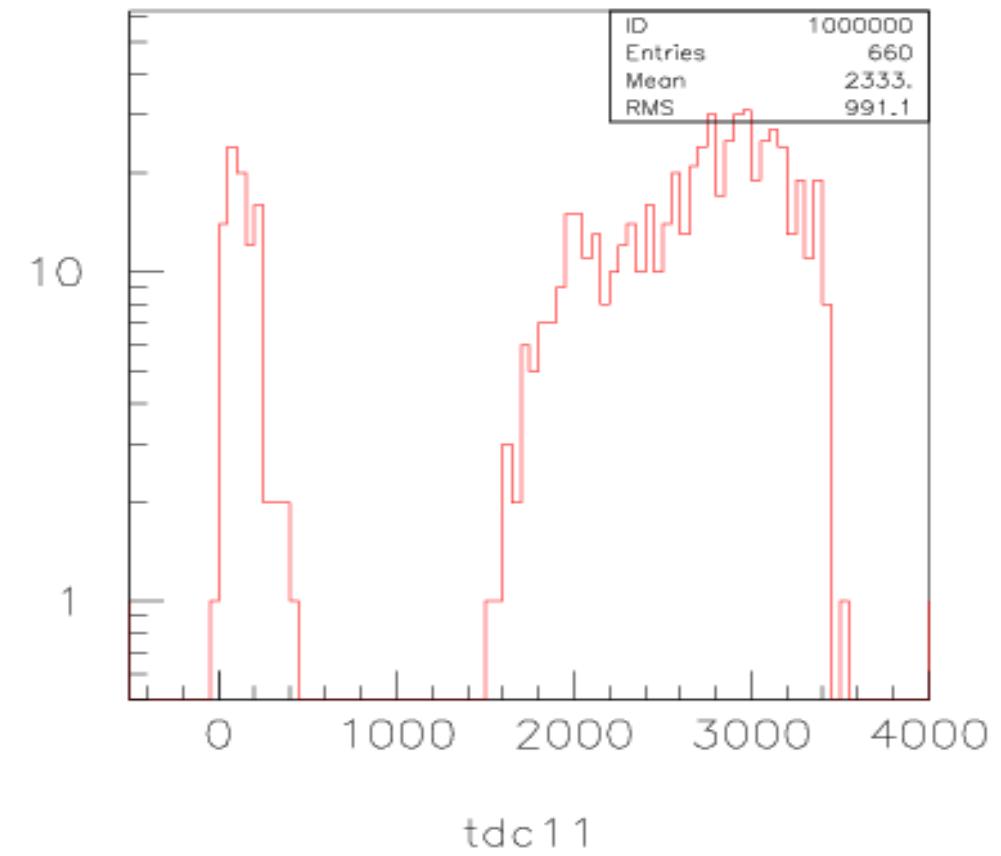
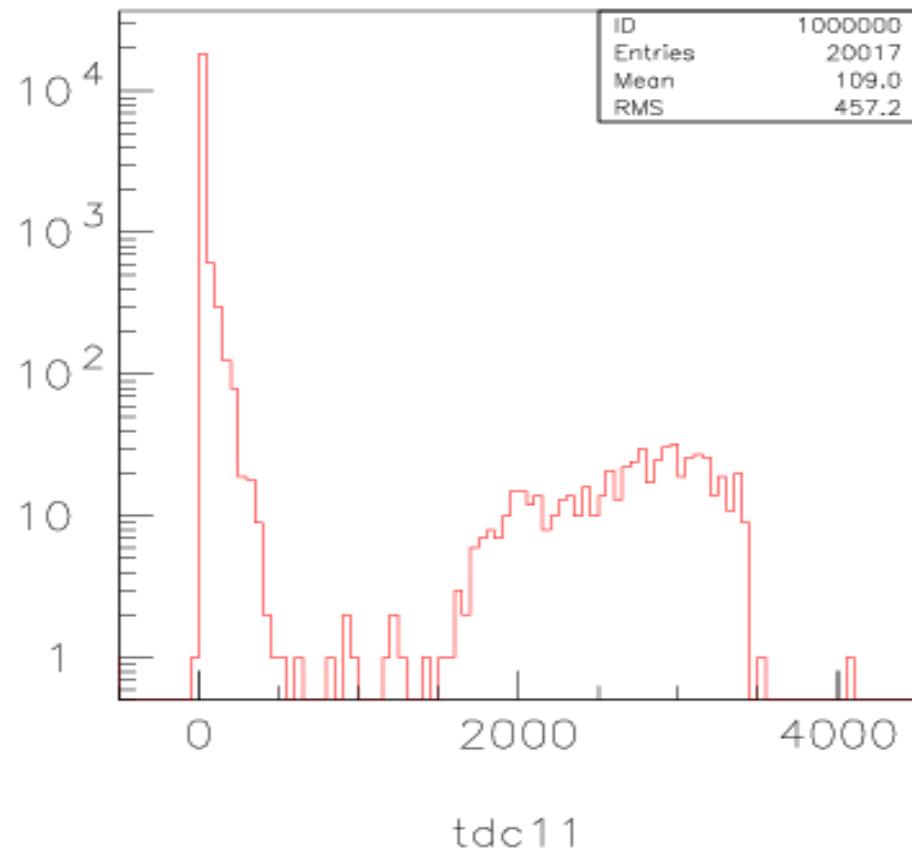


**Funding:** NSFC, Tsinghua University Initiative Scientific Research Program

Thank You for your attention!

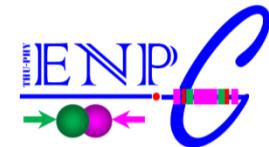


# PPAC Performance II

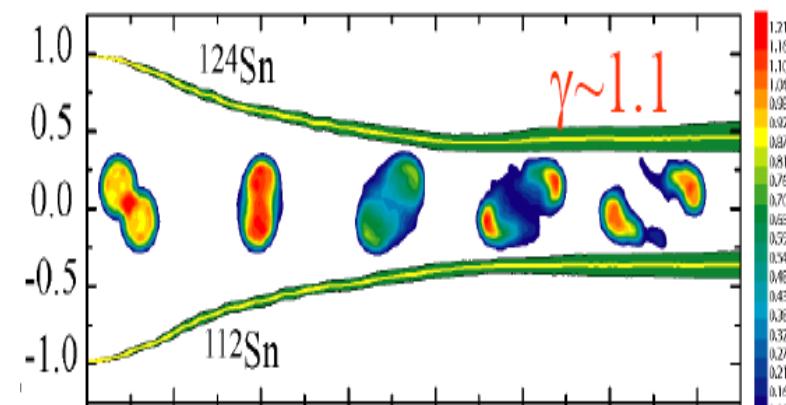


- Identify of fission fragments against light charged particles

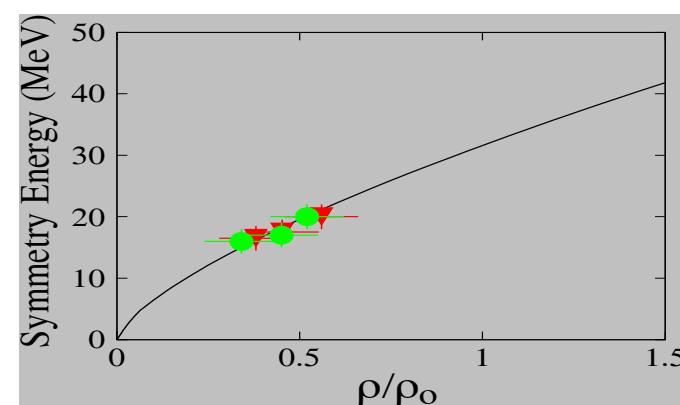
# Some example probes of $E_{\text{sym}}(\rho)$ at $\rho < \rho_0$



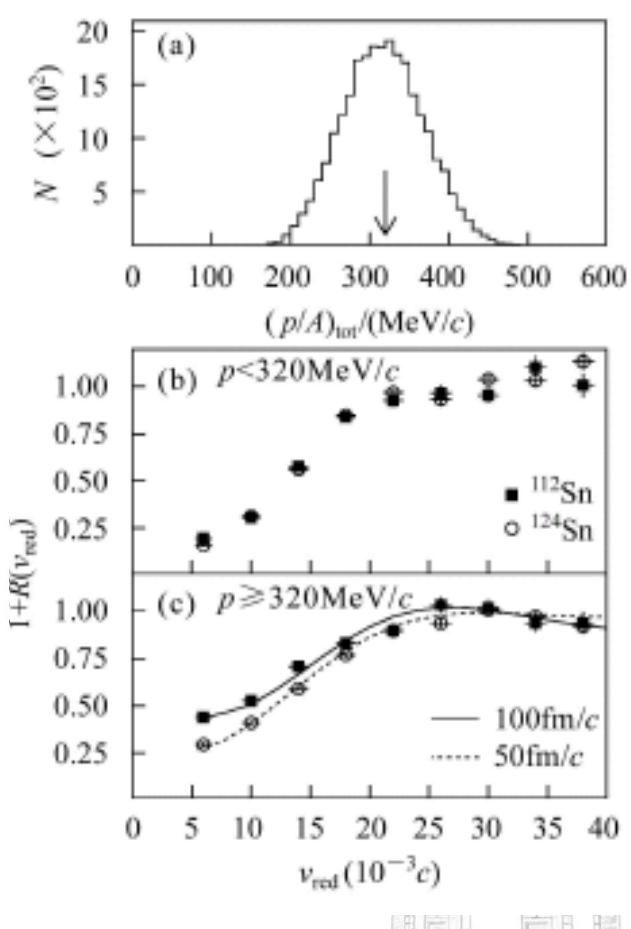
## Isospin diffusion



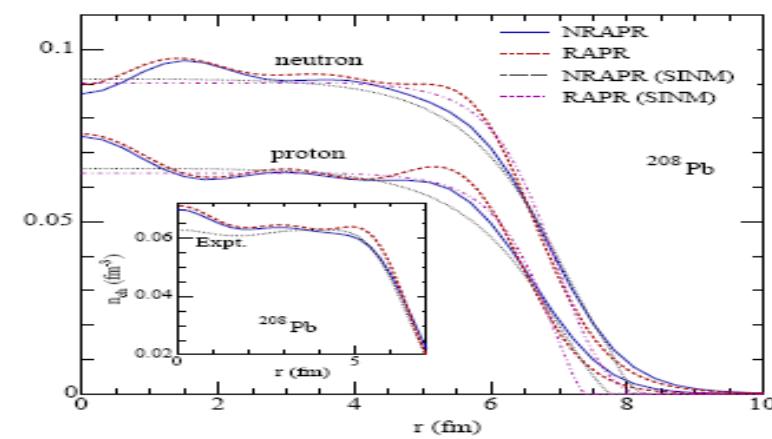
## Isoscaling



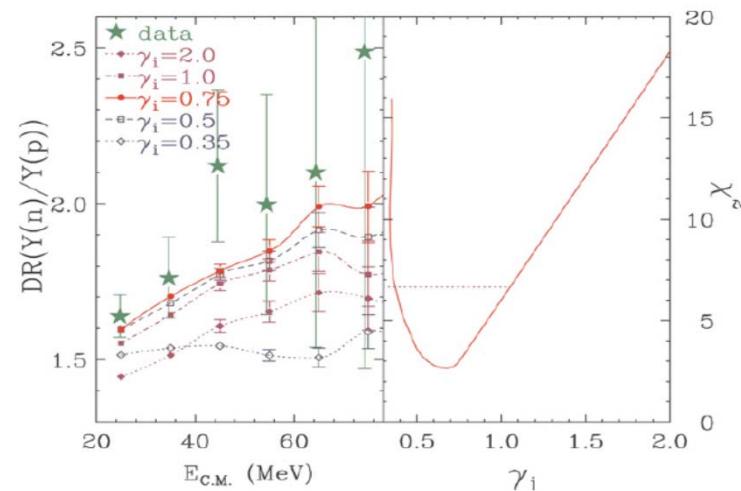
## Correlation Function



## Neutron Skin in $^{208}\text{Pb}$ or RI

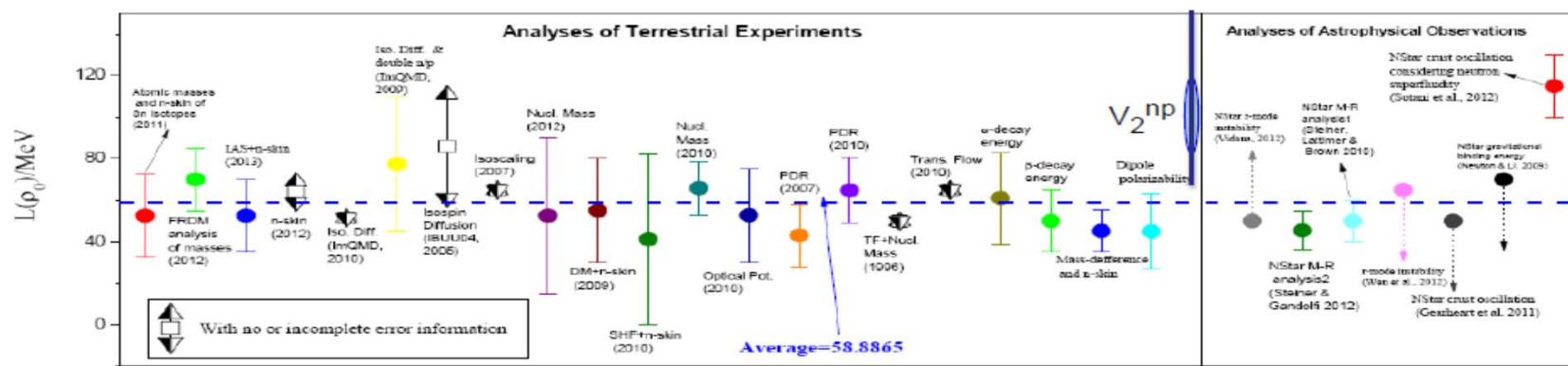
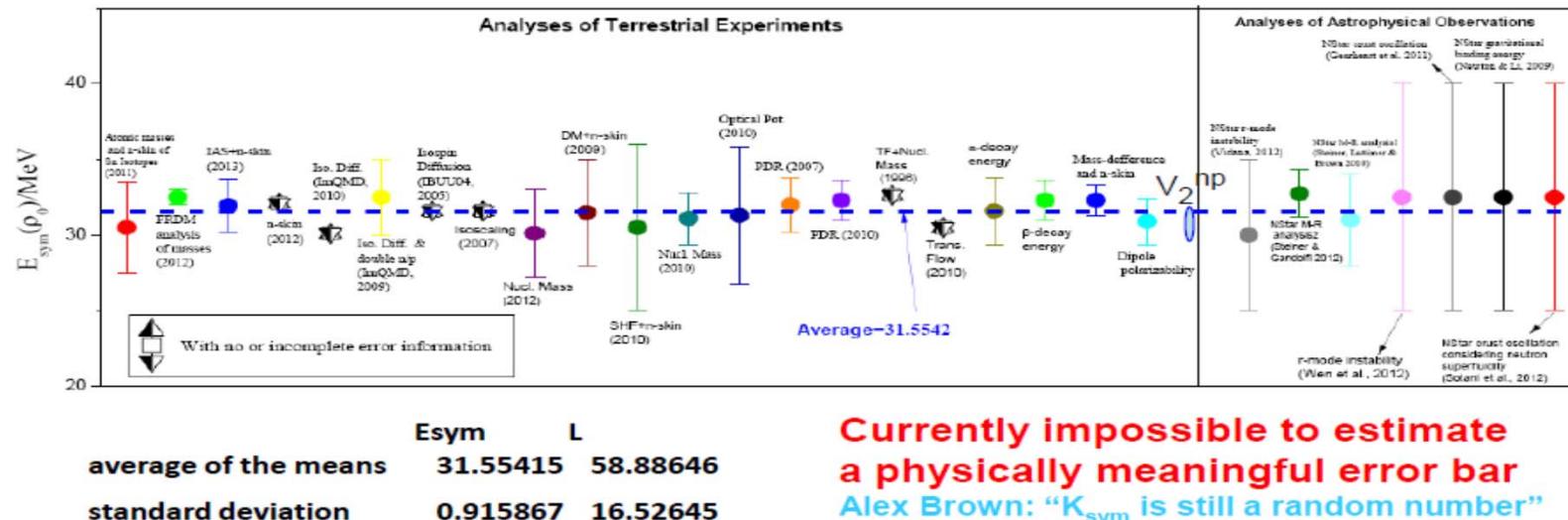


## Fast nucleon emission



# Current constraints on $E_{\text{sym}}(\rho)$ at $\rho < \rho_0$

Nusym13 constraints on  $E_{\text{sym}}(\rho_0)$  and  $L$  based on 29 analyses of some data



- L.W. Chen, arXiv:1212.0284
- B.A. Li, L.W. Chen, F.J. Fattoyev, W.G. Newton, and C. Xu, arXiv:1212.1178