



# How alpha-Cluster Configuration Affects Giant Dipole Resonance

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PKU-CUSTIPEN Nuclear Reaction Workshop "Reactions and Spectroscopy of Unstable Nuclei"

# Outline:

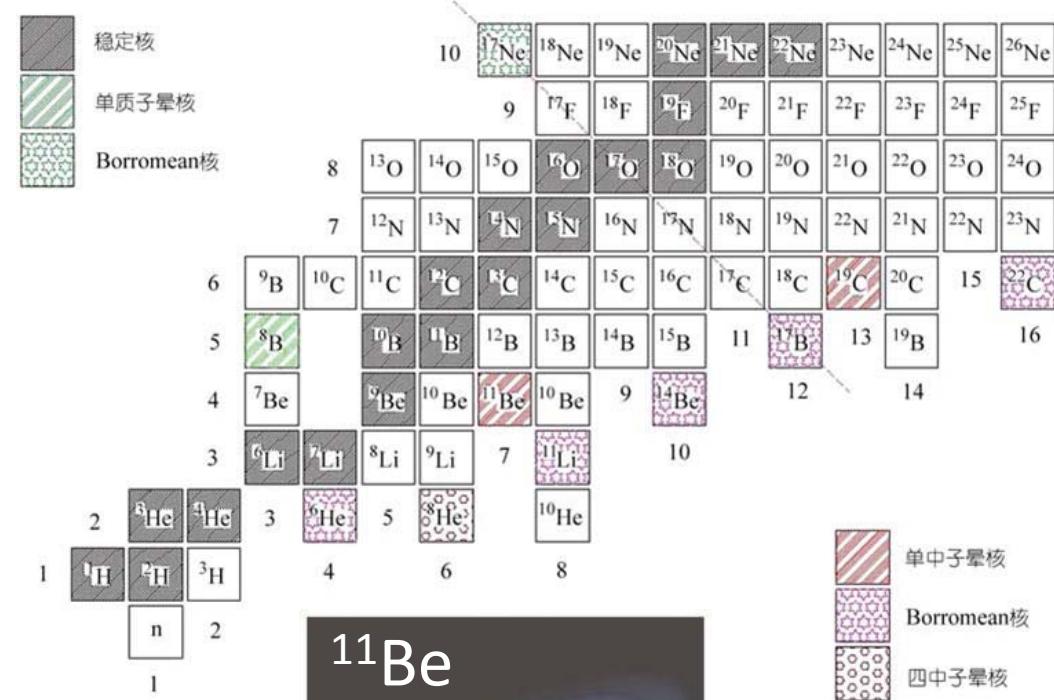
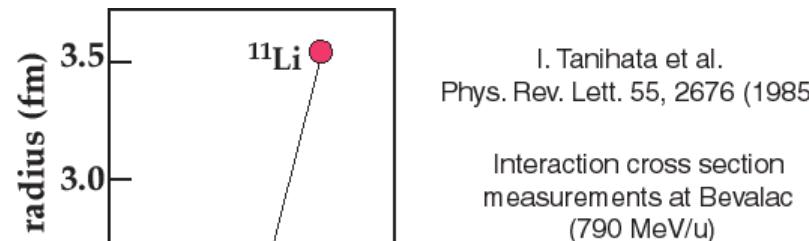
- Background & method introduction
  - ✓ Nuclear cluster in light nuclei
  - ✓ Nuclear collective motion
  - ✓ Microscopic dynamical model
- GDR algorithm & verification
- Results and discussion
  - ✓ Density distribution of cluster nuclei and wave packets
  - ✓ GDR of  ${}^8\text{Be}$ ,  ${}^{12}\text{C}$  &  ${}^{16}\text{O}$  with different  $\alpha$  configurations
- Summary

# □ Background & method introduction

-- cluster in light nuclei

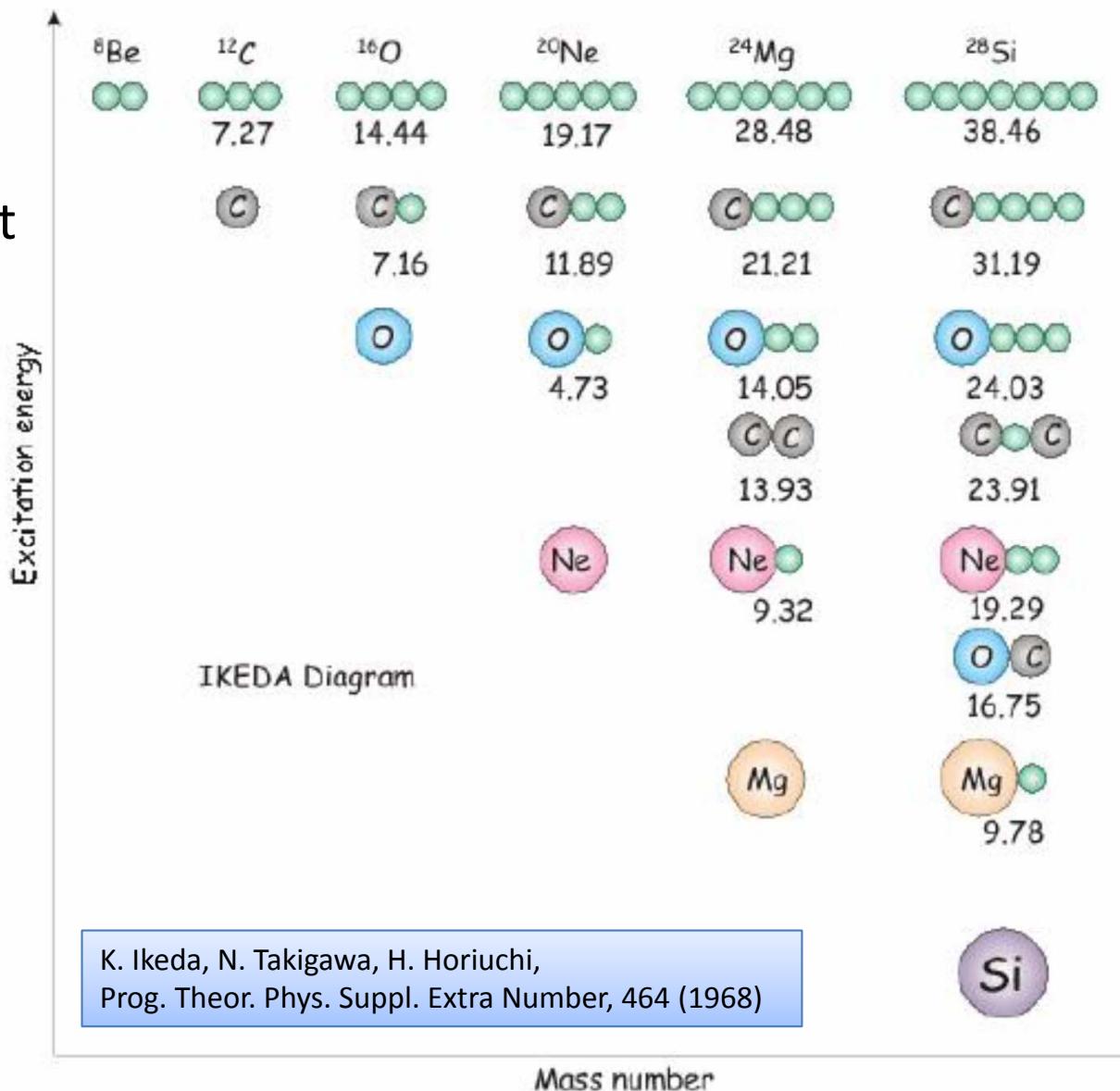
**Cluster completes with mean field in the region of light nuclei**

✓ Far from  $\beta$  stability line, the cluster phenomenon appears as halo



- ✓ Cluster is predicted to appear near cluster decay threshold in  $\alpha$ -conjugate nuclei

The  $\alpha$  cluster is the most prominent case since the high binding energy of  $\alpha$  and the strong  $\alpha$ - $\alpha$  correlation



## ✓ The $\alpha$ cluster configuration in $^{12}\text{C}$

- Non-localized, condensed-like wave function, gas of  $\alpha$  cluster in **Hoyle state**

THSR (Tohsaki-Horiuchi-Schuck-Ropke) wave function:

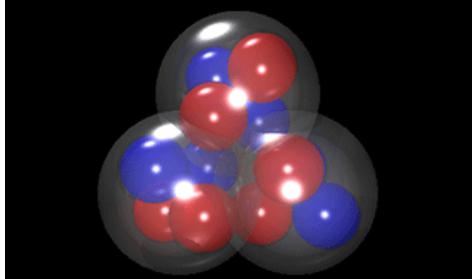
A. Tohsaki et al., *Phys. Rev. Lett.* 87, 192501 (2001)

T. Suhara et al., *Phys. Rev. Lett.* 112, 062501 (2014)

- AB initio calculation based on effective field theory obtains that **Hoyle state** is more like a linear chain of three alpha clusters

E. Epelbaum et al., *Phys. Rev. Lett.* 106, 192501 (2011)

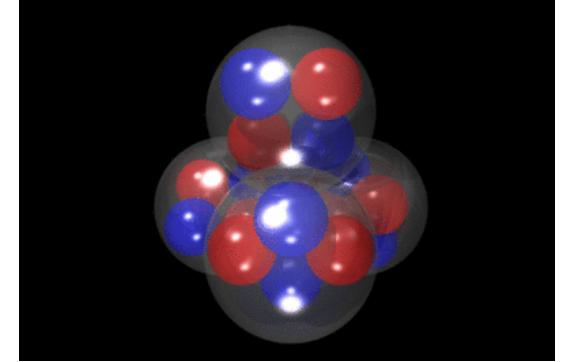
- However, the recent data supports the triangle  $\alpha$  configuration of  $^{12}\text{C}$  **Hoyle state**



D. Marin-Lámbarri, R. Bijker, M. Freer et al. **Evidence for Triangular D<sub>3</sub>h Symmetry in  $^{12}\text{C}$ .** *Phys. Rev. Lett.* 113, 012502 (2014)

## ✓ The $\alpha$ cluster configuration in $^{16}\text{O}$

- Many different calculations support the tetrahedral structure in  $^{16}\text{O}$  ground state, which challenges the traditional shell model picture.



Algebraic model: [Bijker, Iachello, Evidence for Tetrahedral Symmetry in  \$^{16}\text{O}\$ . \*Phys. Rev. Lett.\* 112, 152501 \(2014\)](#)

Effective field theory: [E. Epelbaum, H. Krebs, T. A. Lähde, D. Lee, U.-G. Meißner, and G. Rupak, \*Phys. Rev. Lett.\* 112, 102501 \(2014\)](#)

Covariant density functional theory: [L. Liu and P. W. Zhao, \*Chin. Phys. C\* 36, 818 \(2012\)](#)

- The excited  $^{16}\text{O}$  may evolve into square, or linear chain, or non-localized gas configuration

Effective field theory: [E. Epelbaum, H. Krebs, Timo A. Lähde, Dean Lee, Ulf-G. Meißner, and G. Rupak, \*Phys. Rev. Lett.\* 112, 102501 \(2014\)](#)

Covariant density functional theory: [L. Liu and P. W. Zhao, \*Chin. Phys. C\* 36, 818 \(2012\)](#)

THSR wave function: [T. Suhara et al., \*Phys. Rev. Lett.\* 112, 062501 \(2014\)](#)

## Two important points need to be explored:

- From the experimental point of view, the probe is needed to diagnose the different configurations
- What are the aspects of the collective dynamics of excited  $\alpha$  clustering systems and the underlying mechanism?

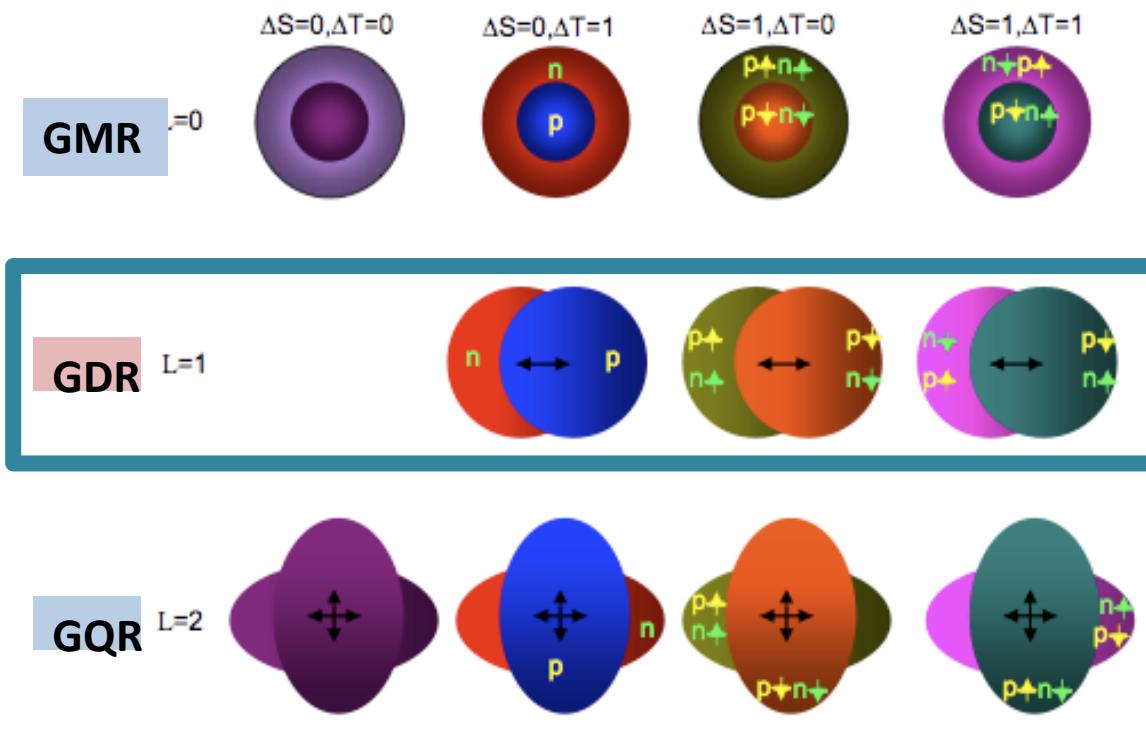
Giant Resonance  $\longleftrightarrow$   $\alpha$  Cluster Configuration

- ❖ Centroid energy of GR can provide direct information about nuclear size and the nuclear equation of state
- ❖ Width of GR closely relates with nuclear deformation, temperature, and angular momentum

# □ Background & method introduction

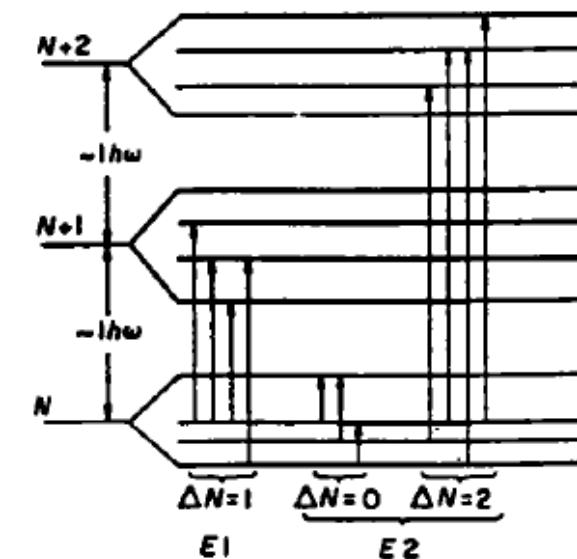
## -- Giant Resonance

Giant resonances are typical collective excitations in nuclei



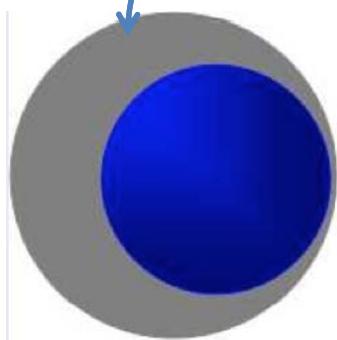
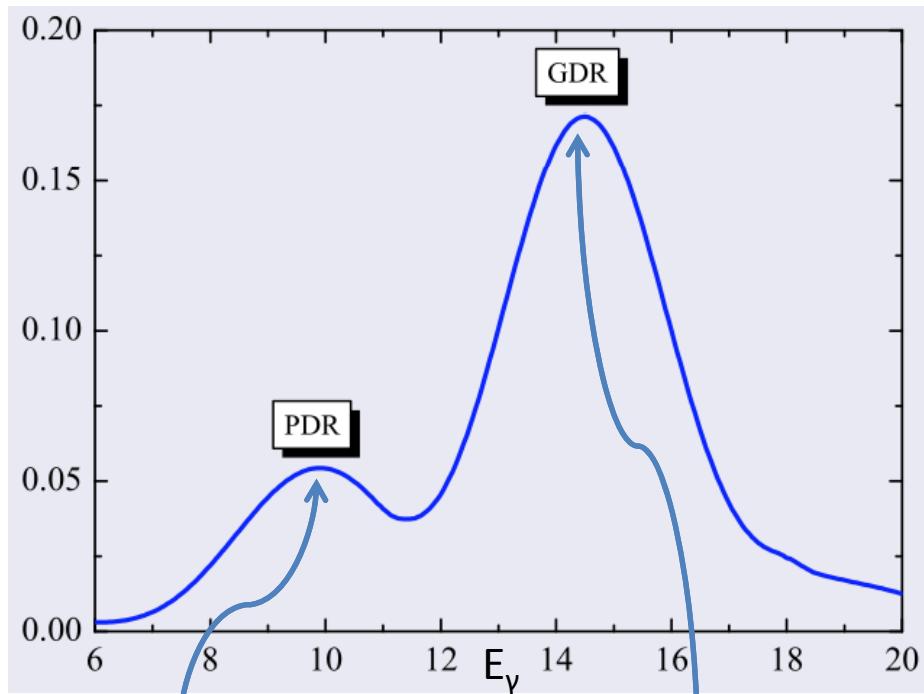
Different collective excitation modes

Macroscopic description

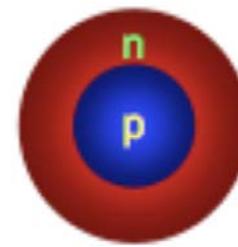
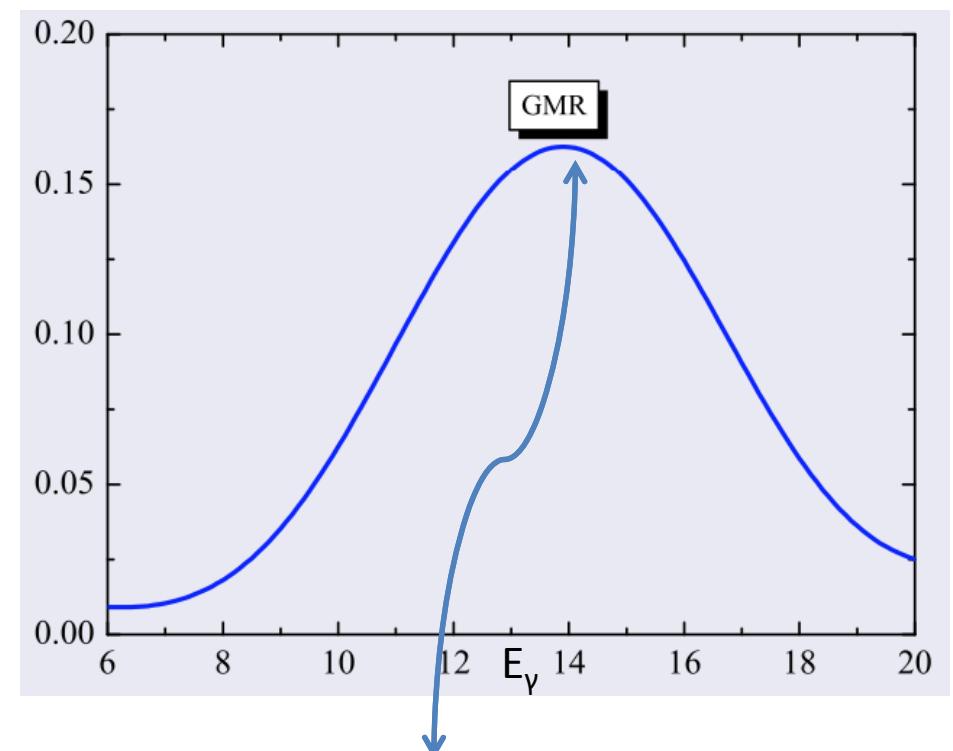


Microscopic description

There are three main excitation modes: GDR, PDR, GMR



PDR  
Valence neutron  $\leftrightarrow$  Core



GDR

Proton  $\leftrightarrow$  Neutron

## □ Background & method introduction

### -- microscopic dynamical model

#### The EQMD model

T. Maruyama, et al., Phys Rev C 53, 297(1996)

R. Wada et al., Phys. Lett. B 422, 6 (1998).

Compared with other Molecular Dynamics (MD) models: QMD, IQMD, AMD, CoMD , ImQMD, IDQMD and LQMD has the following features:

- 1) Dynamical wave packet width in wave function (as in FMD).

Taking into account the kinetic energy term of the momentum variance of wave packets to the Hamiltonian

$$\Psi = \prod_i \phi_i(\mathbf{r}_i)$$
$$\phi_i(r_i) = \left( \frac{\nu_i + \nu_i^*}{2\pi} \right)^{3/4} \exp \left[ -\frac{\nu_i}{2} (\mathbf{r}_i - \mathbf{R}_i)^2 + \frac{i}{\hbar} \mathbf{P}_i \cdot \mathbf{r}_i \right]$$
$$\nu_i \equiv \frac{1}{\lambda_i} + i\delta_i$$

$$H = \left\langle \Psi \left| \sum_i -\frac{\hbar^2}{2m} \nabla_i^2 - \hat{T}_{c.m.} + \hat{H}_{int} \right| \Psi \right\rangle$$
$$= \sum_i \left[ \frac{P_i^2}{2m} + \frac{3\hbar^2(1 + \lambda_i^2 \delta_i^2)}{4m\lambda_i} \right] - T_{c.m.} + H_{int}$$

The equation of motion of nucleon

$$\delta \int_{t_1}^{t_2} \zeta dt = 0$$

$$\zeta \left( \{ R_i, P_i, \lambda_i, \delta_i, \dot{R}_i, \dot{P}_i, \dot{\lambda}_i, \dot{\delta}_i \} \right) \equiv \left\langle \Psi \left| i\hbar \frac{d}{dt} - \hat{H} \right| \Psi \right\rangle$$

$$\dot{R}_i = \frac{\partial H}{\partial P_i} + m_k \frac{\partial H}{\partial R_i} \quad \dot{P}_i = - \frac{\partial H}{\partial R_i} + m_p \frac{\partial H}{\partial P_i}$$

$$\frac{3\hbar}{4} \dot{l}_i = - \frac{\partial H}{\partial d_i} + m_l \frac{\partial H}{\partial l_i} \quad \frac{3\hbar}{4} \dot{d}_i = \frac{\partial H}{\partial l_i} + m_d \frac{\partial H}{\partial d_i}$$

The effective potential considered:

$$H_{\text{int}} = H_{\text{Skyrme}} + H_{\text{Coulomb}} + H_{\text{Symmetry}} + H_{\text{Pauli}}$$

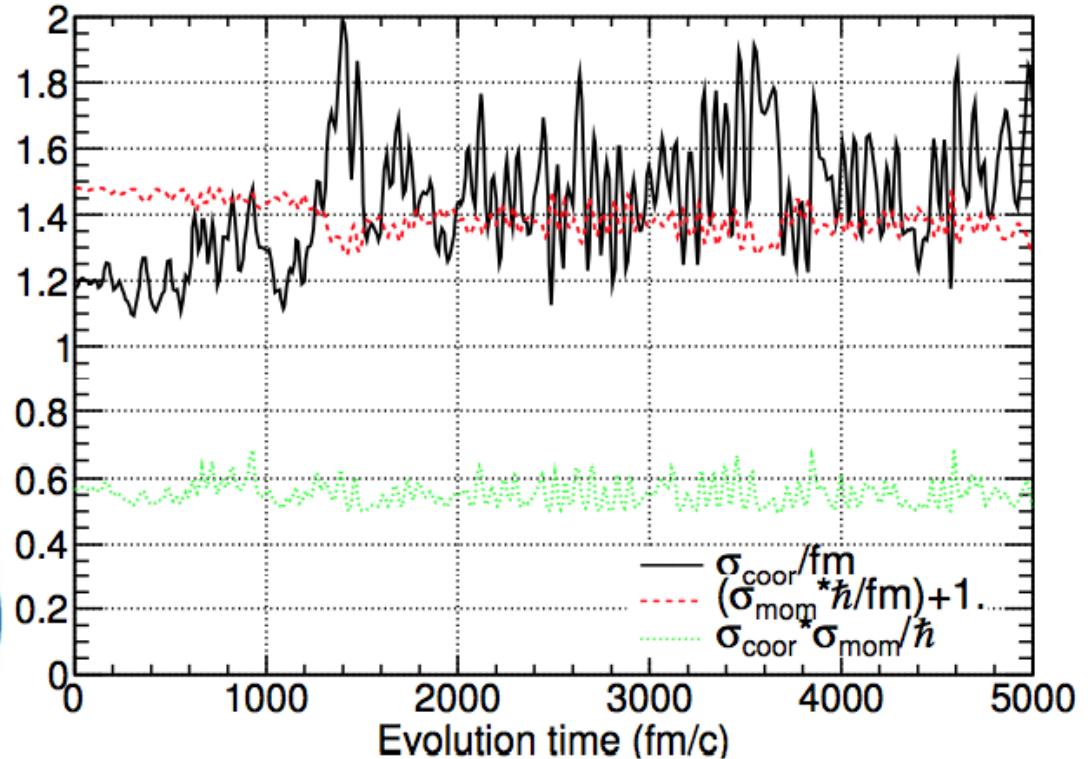
$$H_{\text{Skyrme}} = \frac{\alpha}{2\rho_0} \int \rho^2(r) d^3r + \frac{\beta}{(\gamma+1)\rho_0^\gamma} \int \rho^{\gamma+1}(r) d^3r$$

$$H_{\text{Symmetry}} = \frac{c_s}{2\rho_0} \sum_{i,j \neq 0} \int [2\delta(T_i T_j) - 1] \rho_i(r) \rho_j(r) d^3r$$

$$\sigma_x = \sqrt{\frac{1}{2} \lambda_i}$$

$$\sigma_k = \sqrt{\frac{1}{2} \frac{1 + \lambda_i^2 \delta_i^2}{\lambda_i}}$$

$$\sigma_x^2 \sigma_k^2 = \frac{1}{4} (1 + \lambda_i^2 \delta_i^2) = \frac{1}{4} \left( 1 + \frac{a_I(t)^2}{a_R(t)^2} \right)$$



2) Including Pauli potential into effective interaction to approximate the nature of fermion many-body system: a phenomenological repulsive potential which inhibits nucleons of the same spin S and isospin T to come close to each other in the phase space.

$$H_{Pauli} = \frac{c_p}{2} \sum_i (f_i - f_0)^\mu \theta(f_i - f_0) \quad f_i \equiv \sum_j \delta(S_i, S_j) \delta(T_i, T_j) \left| \langle \phi_i | \phi_j \rangle \right|^2$$

3) The initialization of ground nuclei: fraction cooling

## Advantages:

- ✓ QMD based many-body model, mature and powerful
- ✓ Full microscopic, without assuming cluster in advance
- ✓ Without assuming reaction mechanism in advance
- ✓ Dynamical evolution -> links with observables directly
- ✓ Compared with TDHF cal., this method can be used at higher energy, many-body correlations, more realistic linkage with observables

## Disadvantages:

- ✓ Semi-classical
- ✓ No anti-symmetrized

## Unique Advantages of EQMD compared with other version QMD:

- ✓ Energy conservation more better duration evolution thanks to strict threefold loop computation for three body interaction
- ✓ Stable enough ground state to study low energy region reaction process, without spurious particle emission
- ✓ Dynamical wave packet evolution, reasonable fluctuation and dissipation

## GDR algorithm & verification

-- How to extract giant resonance from QMD

### Fourier transformation

V. Baran et al, Nucl. Phys.A 679,373(2001)

✓  $DR(t) = \frac{NZ}{A} (R_p - R_n)$

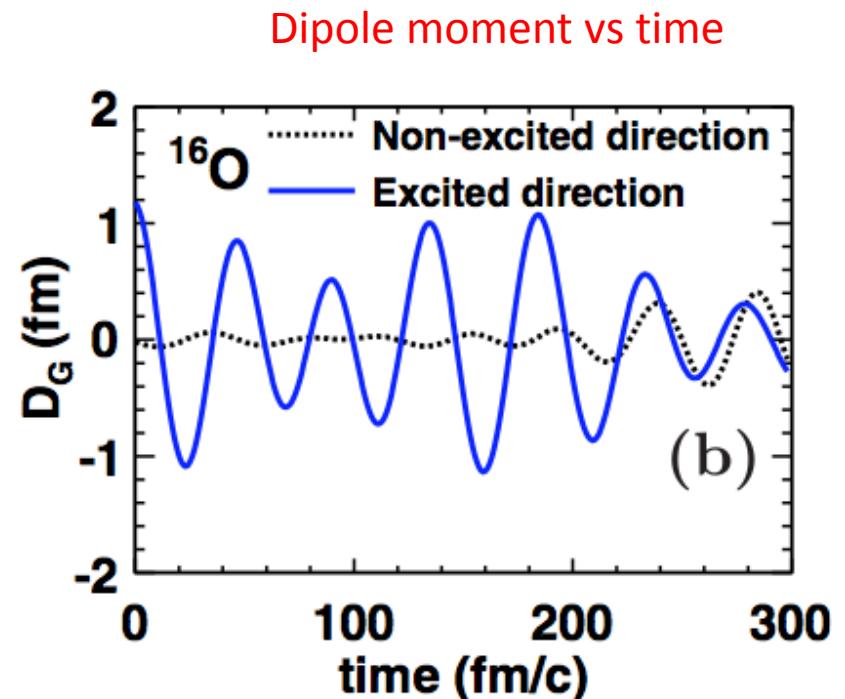
$R_p(R_n)$  is center of mass for protons (neutrons)

✓  $\bar{V} \equiv \overline{\frac{dDR(t)}{dt}},$

✓  $\frac{dV}{dt}(E) = \int_0^\infty \frac{d^2 DR(t)}{dt^2} e^{i\left(\frac{Et}{\hbar c}\right)} dt$

✓  $\frac{dP}{dE} = \frac{2}{3\pi E\hbar c} \left| \frac{dV}{dt}(E) \right|^2$

$dP/dE$  is GDR strength

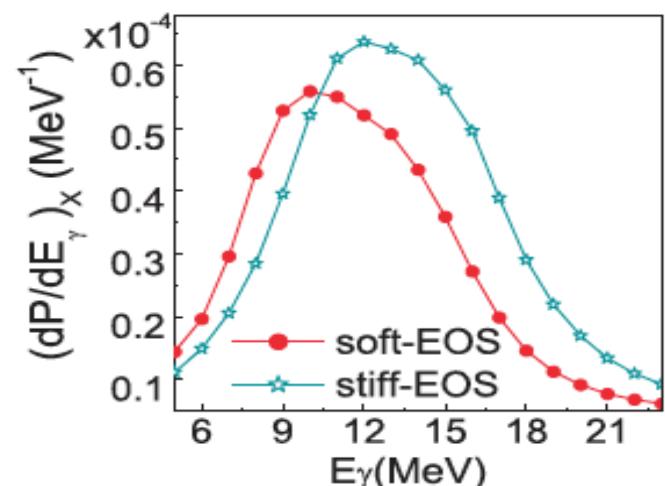
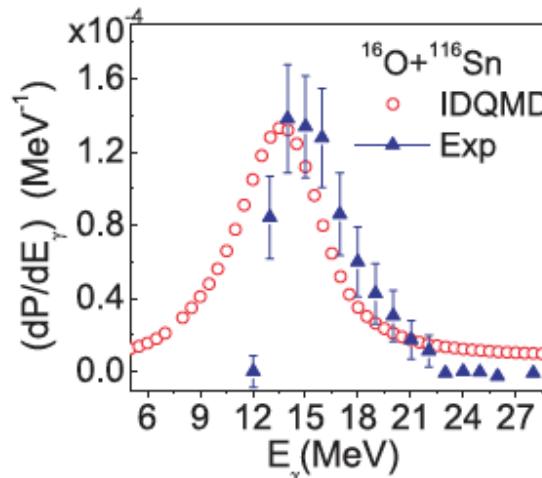
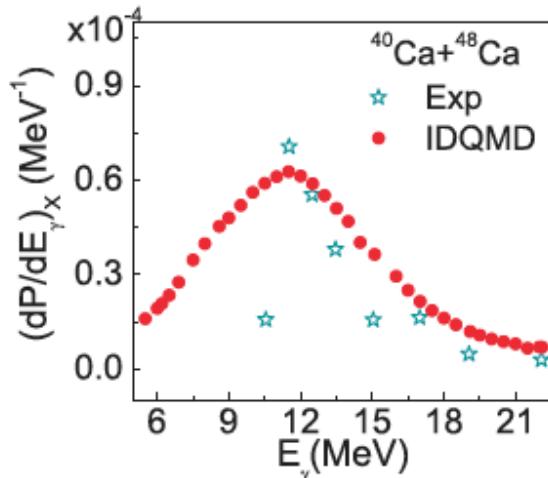
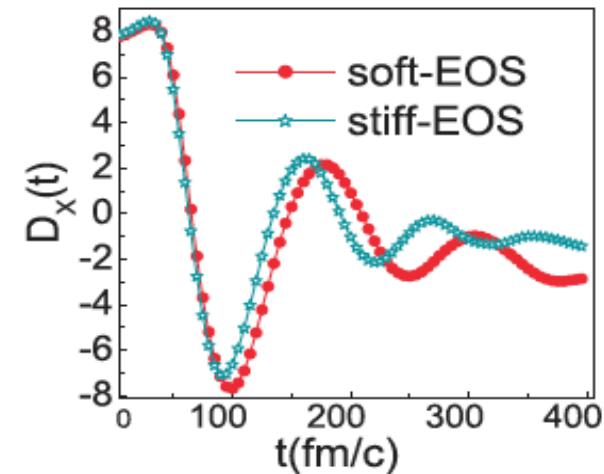
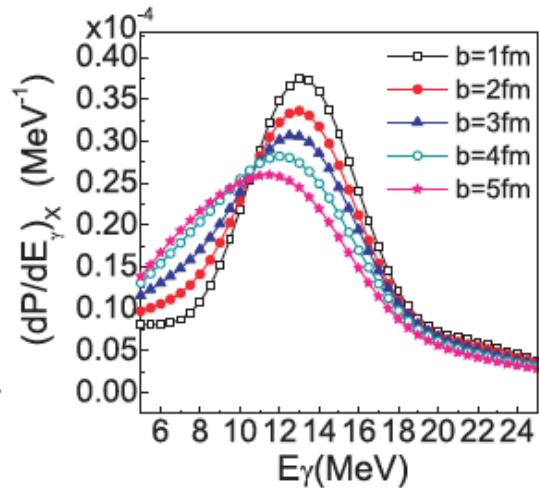
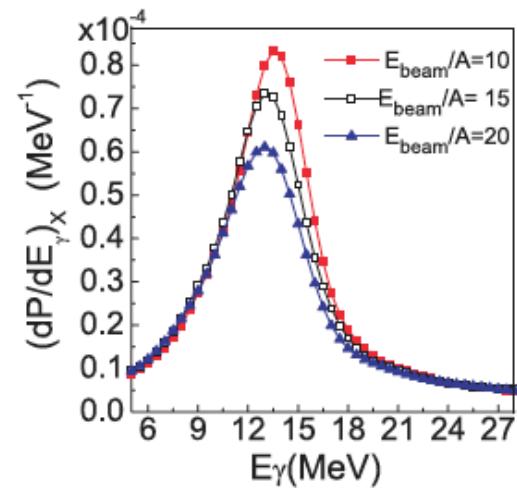


This approach has been successfully applied in GDR, PDR, GMR calculations by IQMD & BUU model based on the fact that the quasiperiodic motion of nucleons in GR represents a known classical limit of quantum mechanics, which has been confirmed by TDHF calculations long before [A. S. Umar Phys. Rev. C 32, 172 (1985)].

### Our recent works:

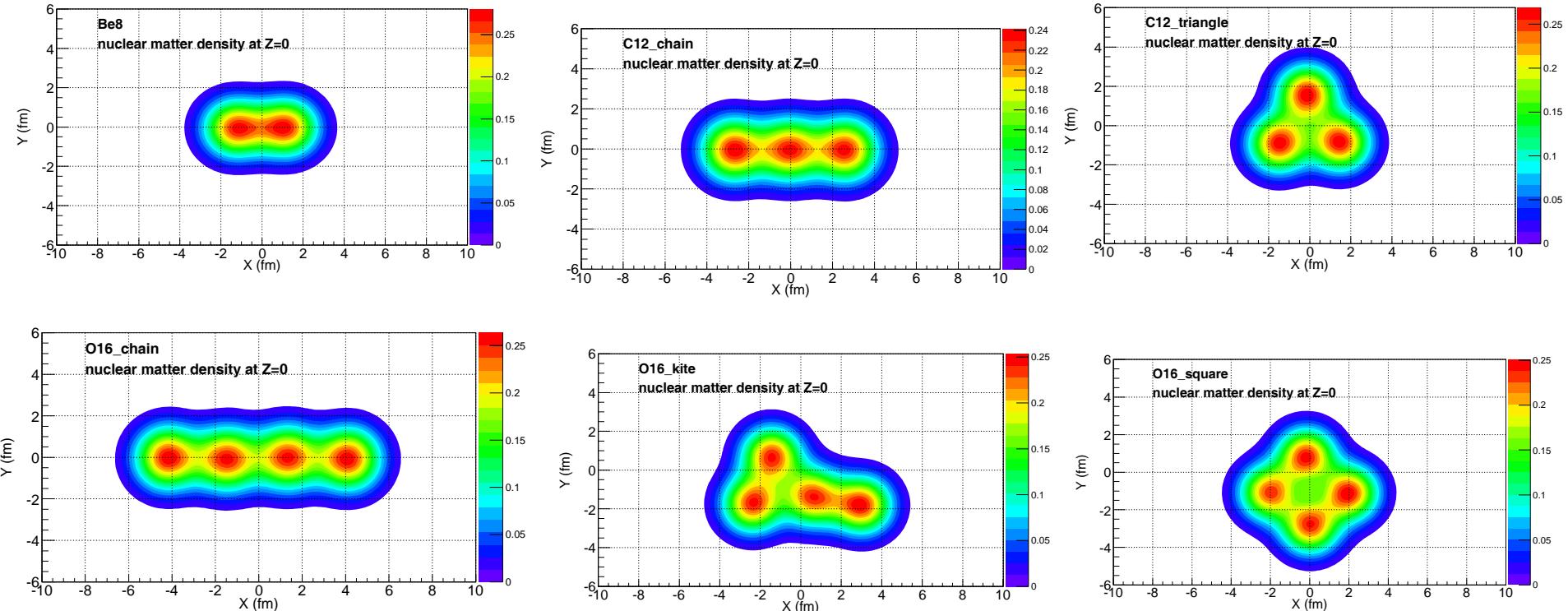
- H. L. Wu, W. D. Tian and YGM et al., “Dynamical dipole \gamma radiation in heavy ion collisions on the basis of a quantum molecular dynamics model”, [Phys. Rev. C 81](#), 047602 (2010)
- C. Tao and YGM et al., “Pygmy and giant dipole resonances by Coulomb excitation using a quantum molecular dynamics model”, [Phys. Rev. C 87](#), 014621 (2013)
- C. Tao and YGM et al., “Isoscalar giant monopole resonance in Sn isotopes using a quantum molecular dynamics model ”, [Phys. Rev. C 88](#), 064615 (2013)
- S. Q. Ye, X. Z. Cai and YGM et al., “Symmetry-energy dependence of the dynamical dipole mode in the Boltzmann-Uehling- Uhlenbeck model”, [Phys. Rev. C 88](#), 047602 (2013)

## Dynamical dipole $\gamma$ radiation in heavy-ion collisions on the basis of a quantum molecular dynamics model



## □ Results & discussion

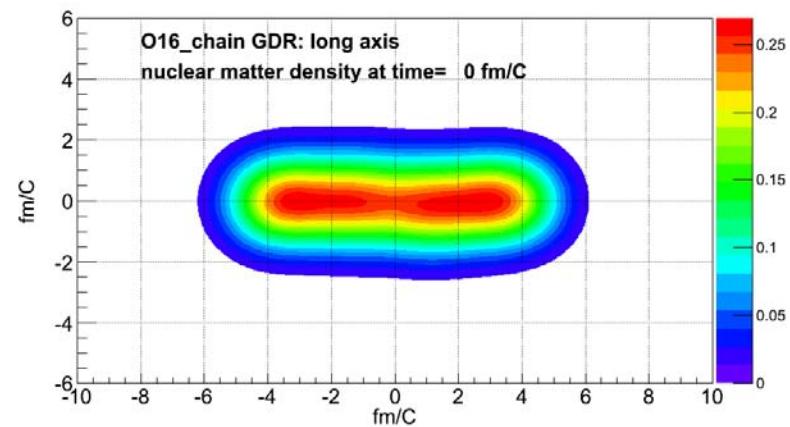
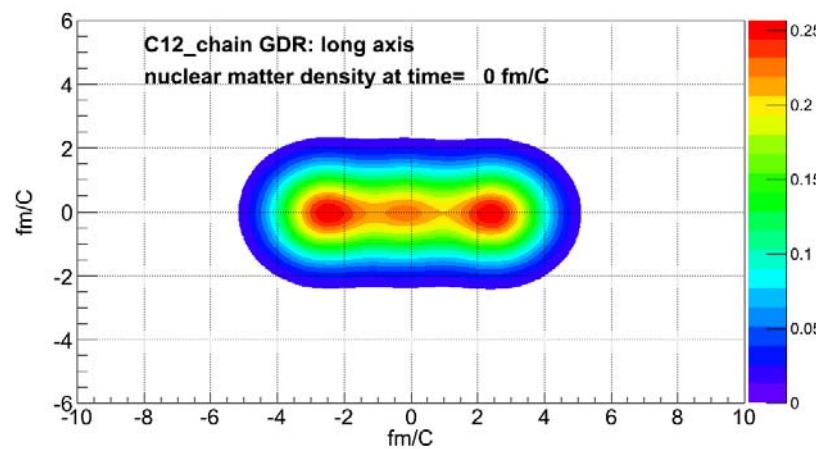
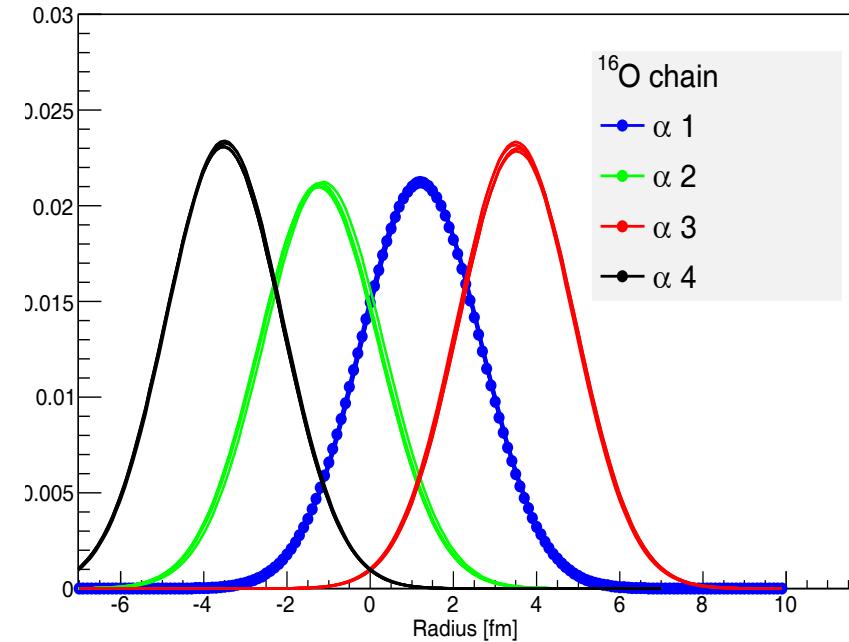
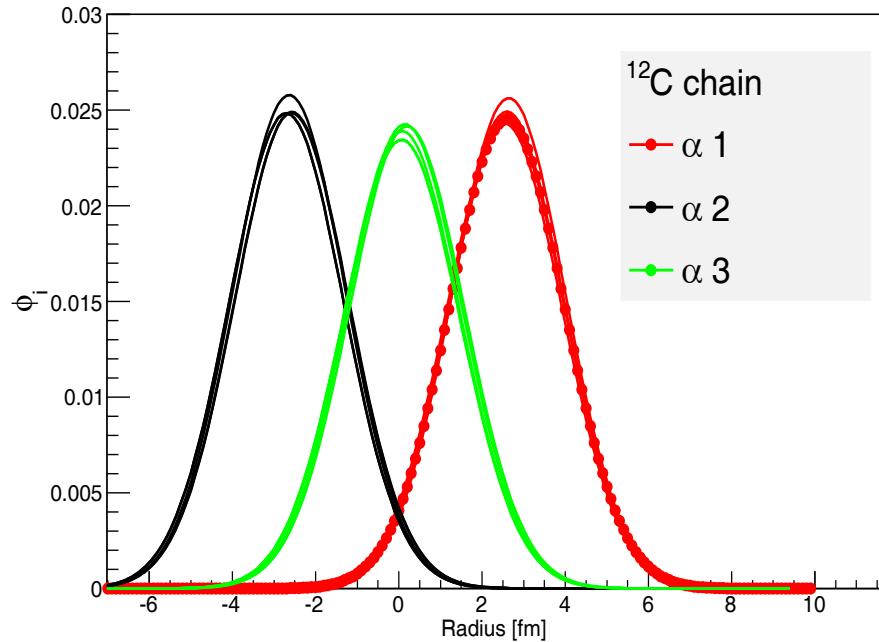
### -- Density distribution of clustering nuclei and wave packets



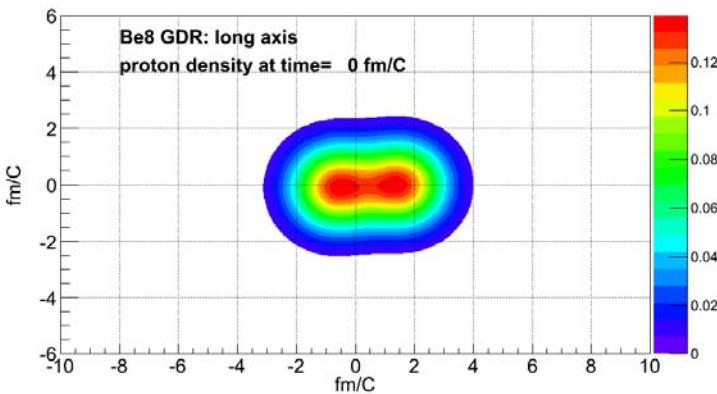
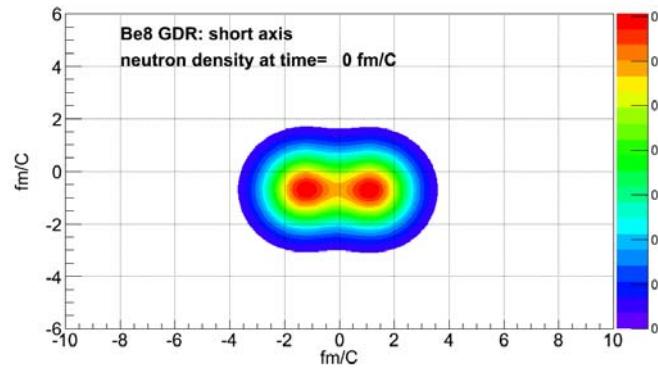
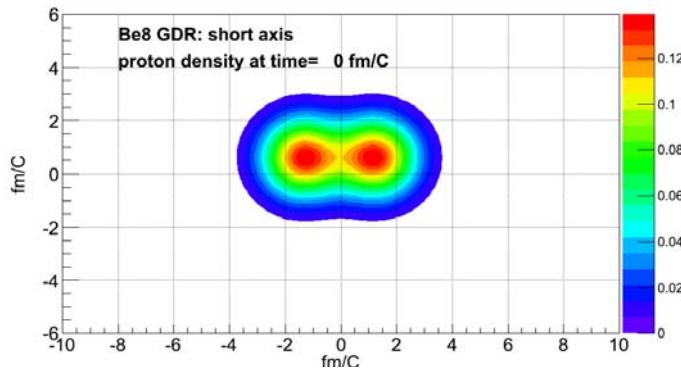
Binding energy of nuclei with cluster configuration

Nuclei	$^6\text{Be}$	$^{12}\text{C}$ chain	$^{12}\text{C}$ triangle	$^{16}\text{O}$ chain	$^{16}\text{O}$ kite	$^{16}\text{O}$ square
Binding energy (AMeV)	7.19	7.21	7.26	7.22	7.18	7.26

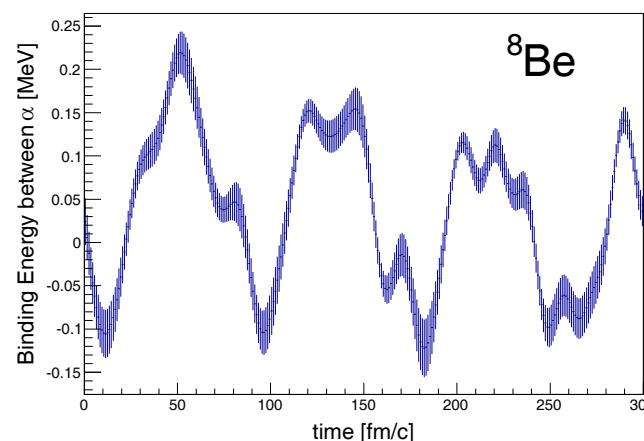
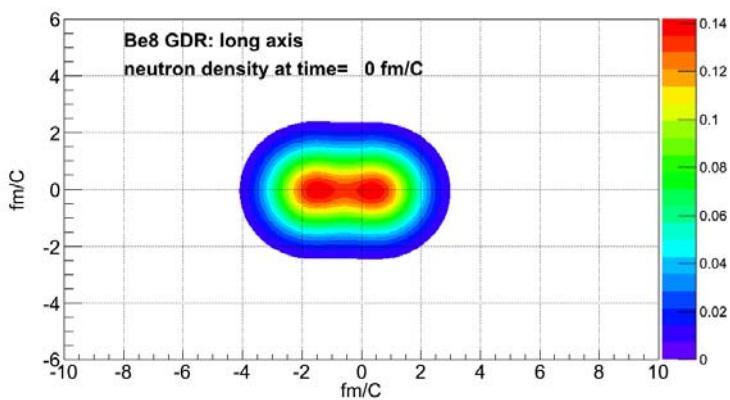
# Density of each nucleon in nuclei with alpha cluster configuration



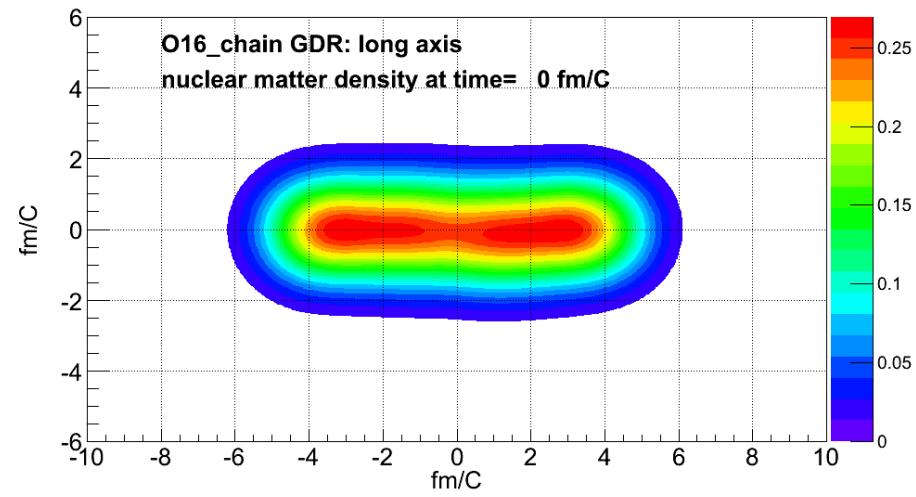
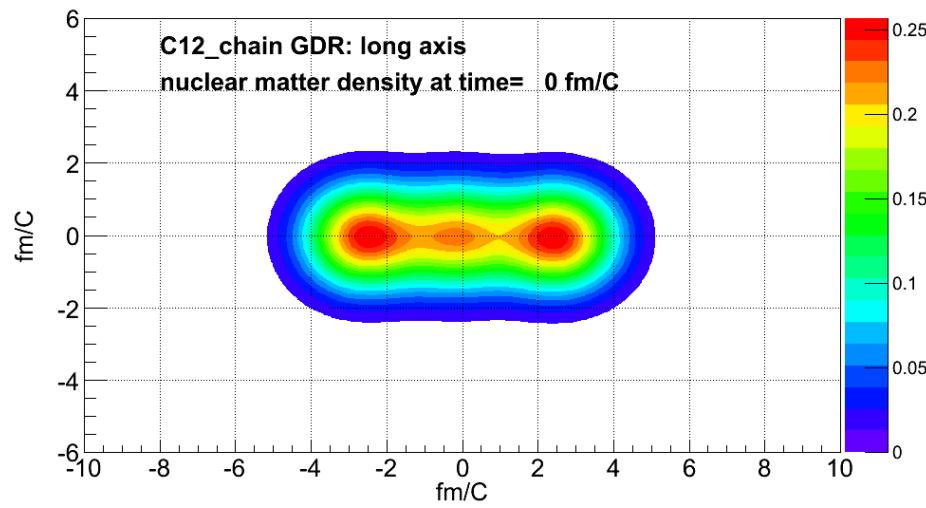
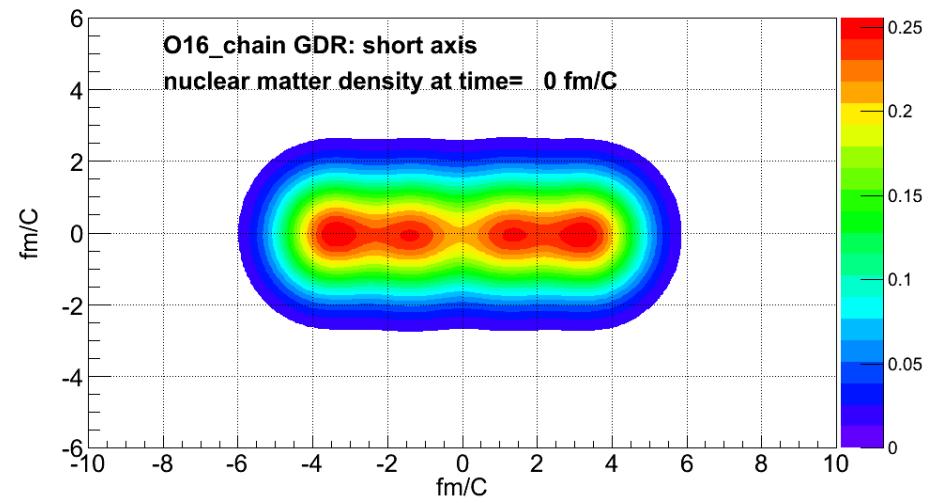
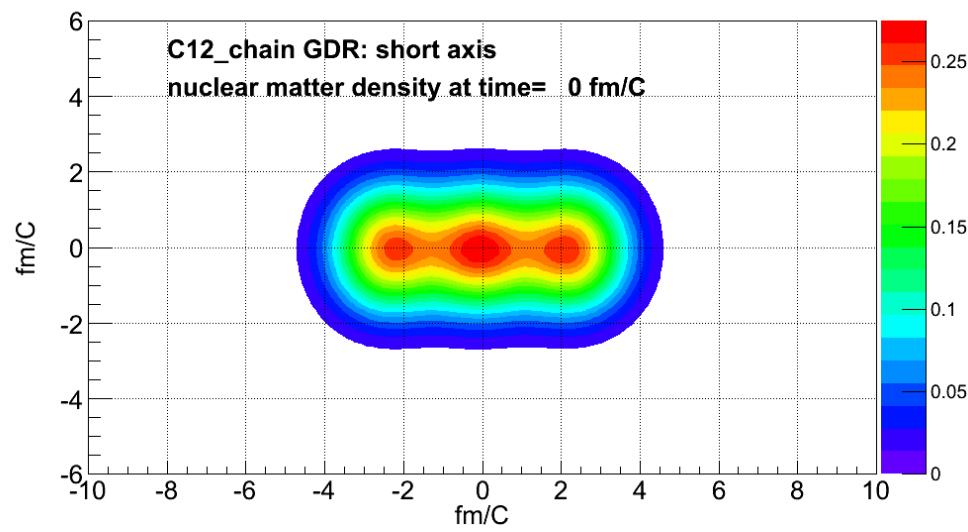
## ◆ Dynamical evolution of density current



The  $\alpha$  cluster is very different from free  $\alpha$  particle



Binding energy evolution between two alphas in  $^{8}\text{Be}$

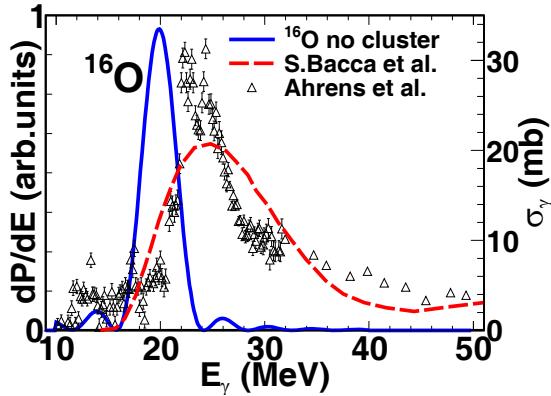


## □ Results & discussion

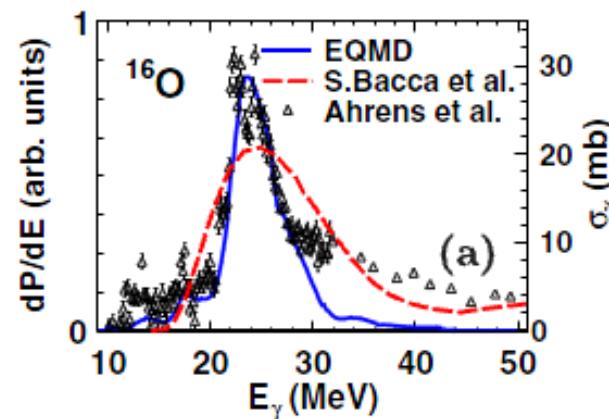
-- GDR of  $^{8}\text{Be}$ ,  $^{12}\text{C}$  &  $^{16}\text{O}$  with different  $\alpha$  configurations

W. He, YGM, X. Cao, X. Cai, G. Zhang, *Phys. Rev. Lett.* **113**, 032506 (2014)

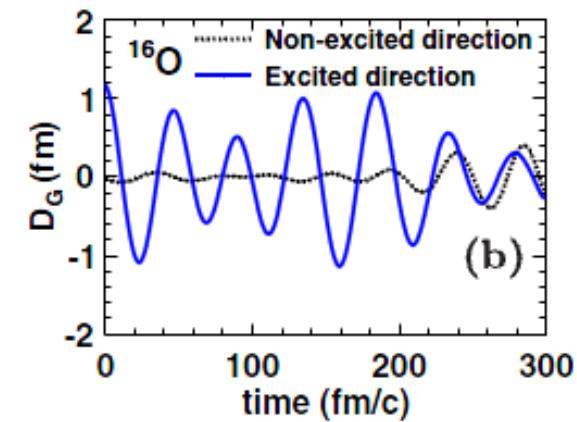
◆ EQMD calculation supports  $^{16}\text{O}$  ground state with tetrahedron



$^{16}\text{O}$  ground state without cluster

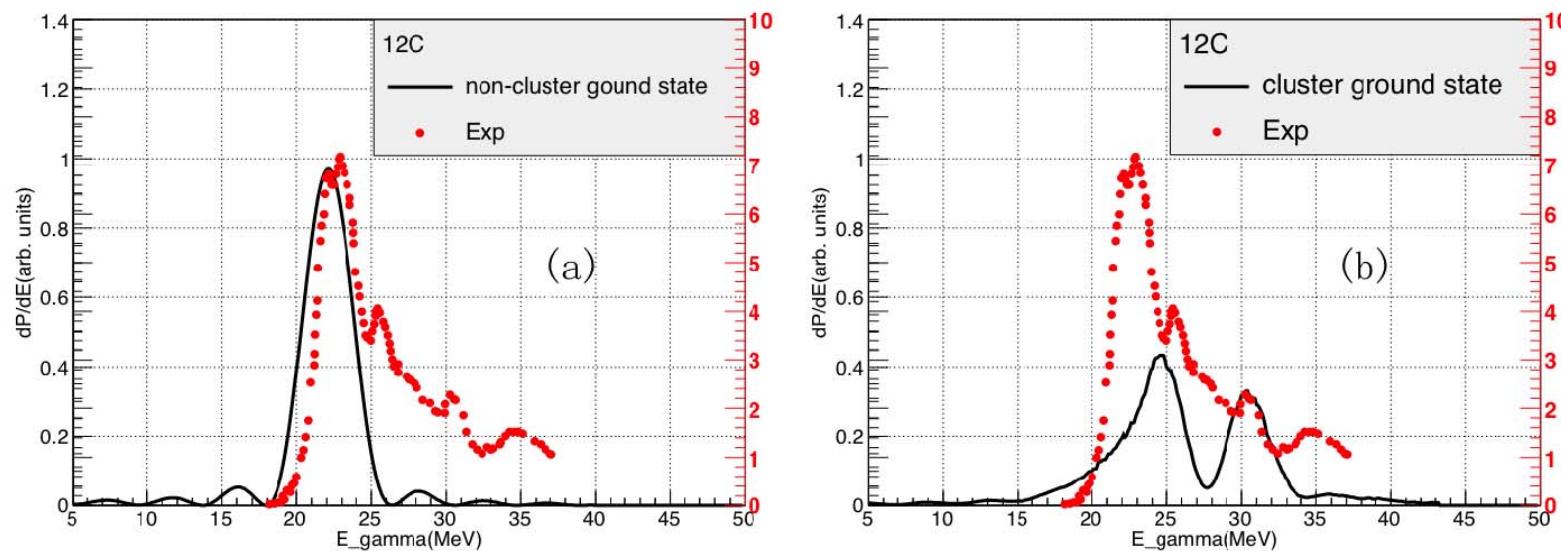


$^{16}\text{O}$  ground state with tetrahedron



Dipole evolution of  $^{16}\text{O}$

◆ EQMD calculation indicates the ground of  $^{12}\text{C}$  is a multiconfiguration mixing of shell-model-like and cluster-like configurations,  
 which is consistent with the prediction of AMD  
 [Y. Kanada-En'yo, Phys. Rev. Lett 81, 5291 (1998)] and FMD  
 [M. Chernykh, H. Feldmeier et al., Phys. Rev. Lett. 98, 032501 (2007)]



$^{12}\text{C}$  GDR without (left panel) and with (right panel)  
 cluster configuration with data.

# Giant Dipole Resonance as a Fingerprint of $\alpha$ Clustering Configurations in $^{12}\text{C}$ and $^{16}\text{O}$

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Correspondence between GDR and  
 $\alpha$  cluster configurations

- ✓ GDR spectrum is highly fragmented into several apparent peaks due to the  $\alpha$  structure
- ✓ The different  $\alpha$  cluster configurations in  $^{12}\text{C}$  and  $^{16}\text{O}$  have corresponding characteristic spectra of GDR
- ✓ The number and centroid energies of peaks in the GDR spectra can be reasonably explained by the geometrical and dynamical symmetries of  $\alpha$  clustering configurations

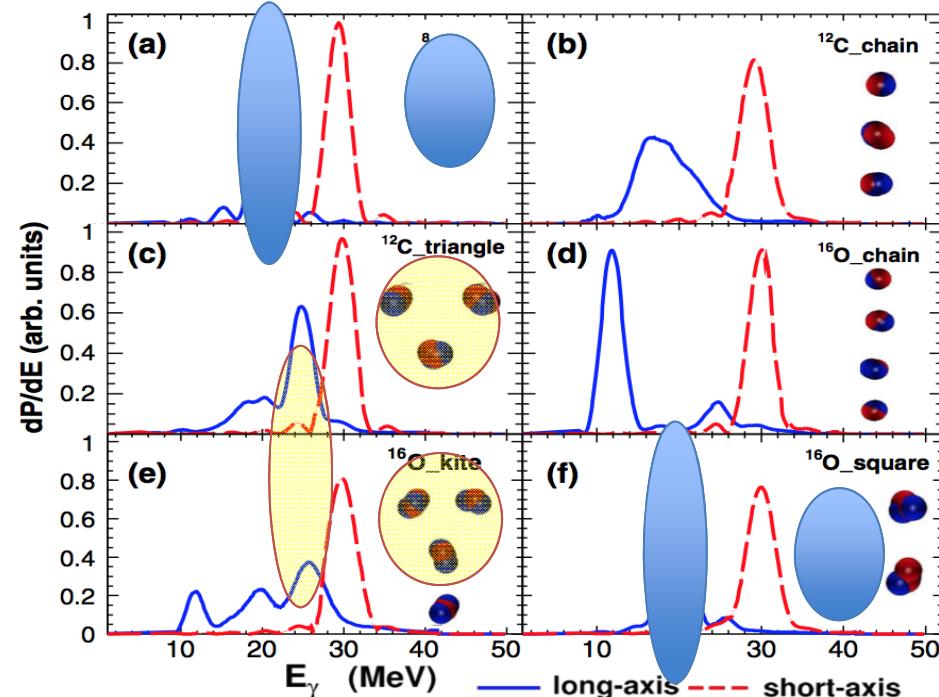


FIG. 2 (color online).  $^8\text{Be}$ ,  $^{12}\text{C}$ , and  $^{16}\text{O}$  GDR spectra with different cluster configurations. The corresponding  $\alpha$  cluster configuration in the present EQMD model calculation is drawn in each panel, in which blue and red balls indicate protons and neutrons, respectively. The dynamical dipole evolution of  $^8\text{Be}$ ,  $^{12}\text{C}$ , and  $^{16}\text{O}$  with linear-chain configurations are shown in [51].

◆ Hints from an experimental point of view

--- sensitive probe

- ✓ The measurement of the GDR peak located around 30 MeV is a feasible way to confirm the existence of an  $\alpha$  clustering state
- ✓ Analysis of other low- lying peaks can be used to diagnose the different configurations formed by  $\alpha$  clusters
- ✓ The similar GDRs of  $^8\text{Be}$  and triangle  $^{12}\text{C}$  appear as substructures in the GDRs of square  $^{16}\text{O}$  and kite  $^{16}\text{O}$ , respectively, which will help to recognize the  $\alpha$  configuration in  $^{16}\text{O}$

## □ Summary & outlook

- ✓ The semi-classical QMD-like model is suitable to study GR
- ✓ The GDR of excited state with  $\alpha$  cluster is studied by EQMD
  - ✧ GDR as an effective probe of  $\alpha$  configuration
    - Peak near 30 MeV
    - Substructure in  $^{12}\text{C}$  and  $^{16}\text{O}$
  - ✧ The density evolution shows the complicated underlying dynamics of  $\alpha$  cluster in nuclei
- ✓ Possible experimental chance on HLyS (Triangle Univ.) and SLEGS (SINAP)

Thanks for discussions with P. Schuck, T. Maruyama, J. Natowitz, S. Shlomo, R. Wada

*Thanks very much for your attention!*

# Backup slides



## Signatures of $\alpha$ Clustering in Light Nuclei from Relativistic Nuclear Collisions

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<sup>2</sup>*H. Niewodniczański Institute of Nuclear Physics PAN, 31-342 Cracow, Poland*

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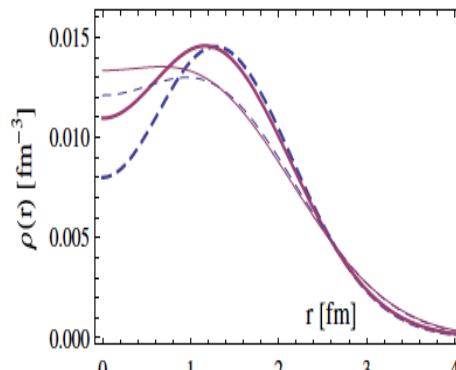
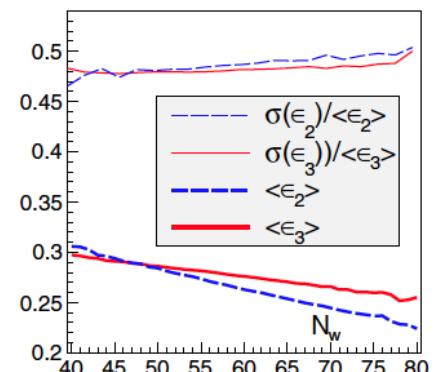
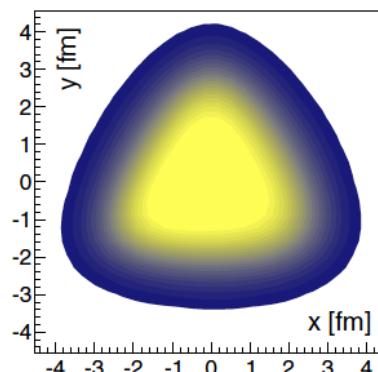
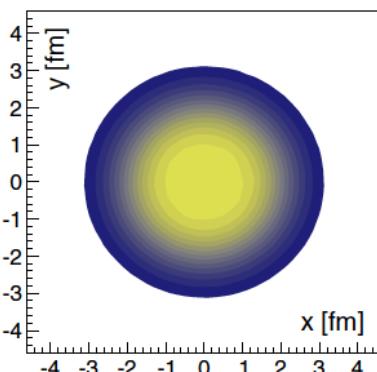
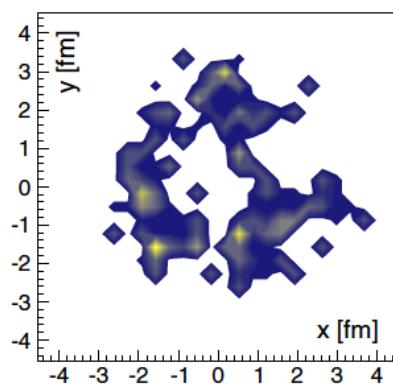
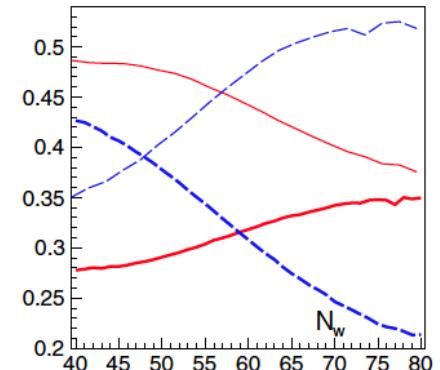
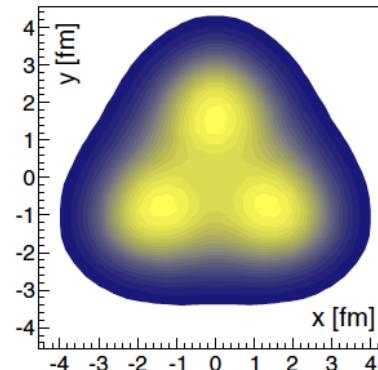
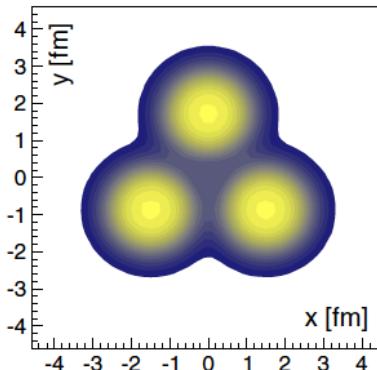
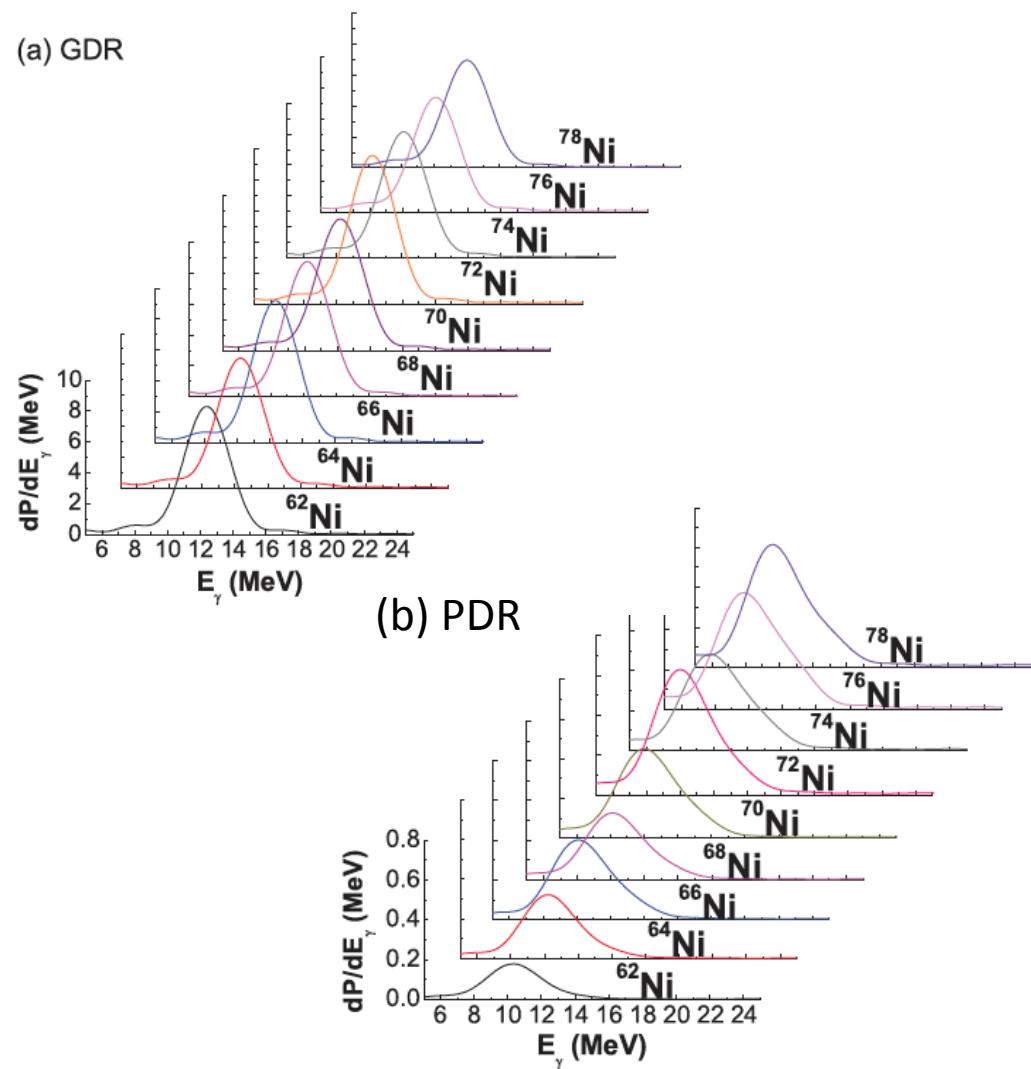
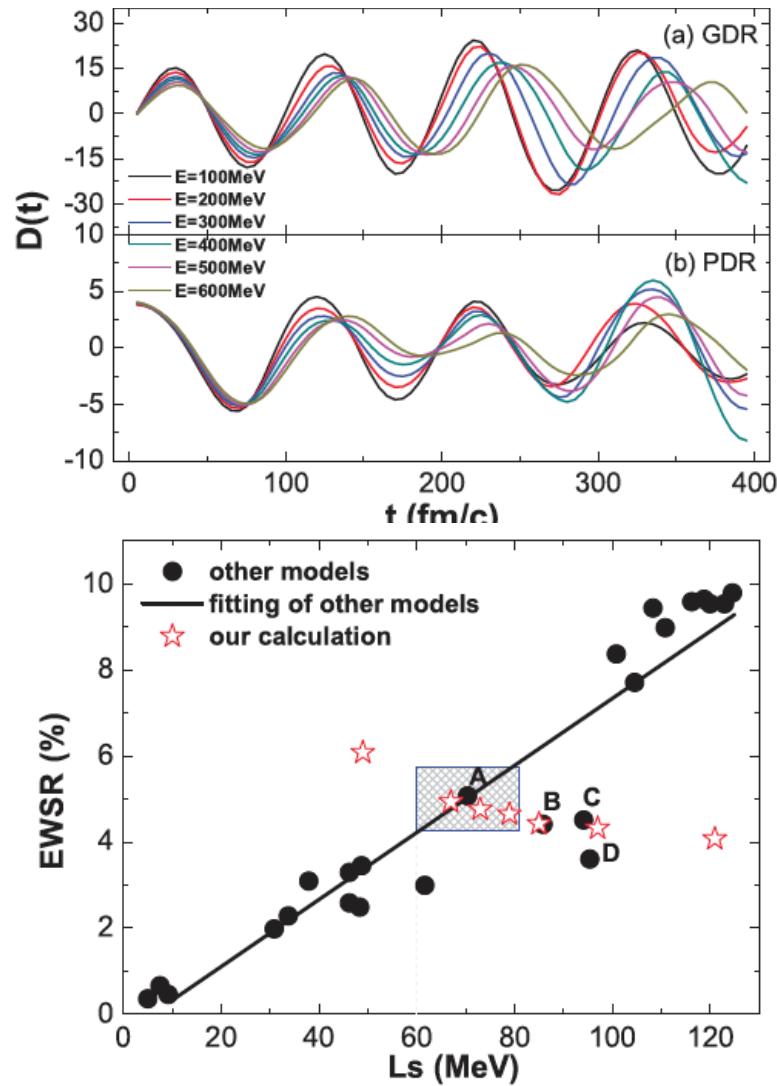


FIG. 1. (Color online) (color online). The electric charge density (thin lines) and the corresponding distribution of the centers of nucleons (thick lines) in  $^{12}\text{C}$  for the data and BEC calculations (dashed lines), and for the FMD calculations (solid lines), plotted against the radius.



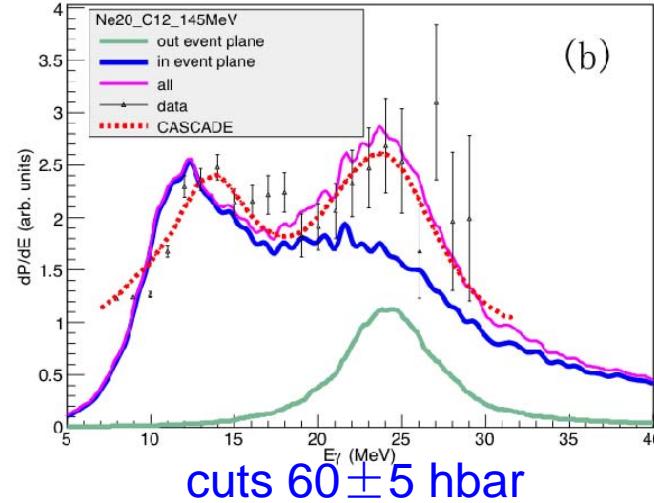
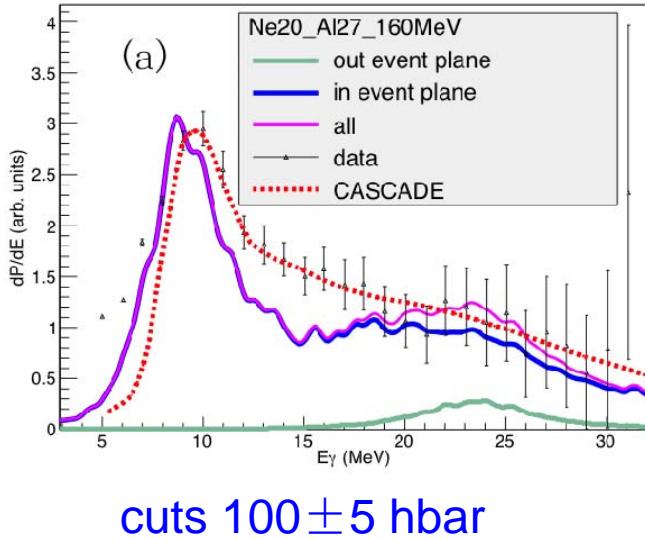
# Pygmy and giant dipole resonances by Coulomb excitation using a quantum molecular dynamics model



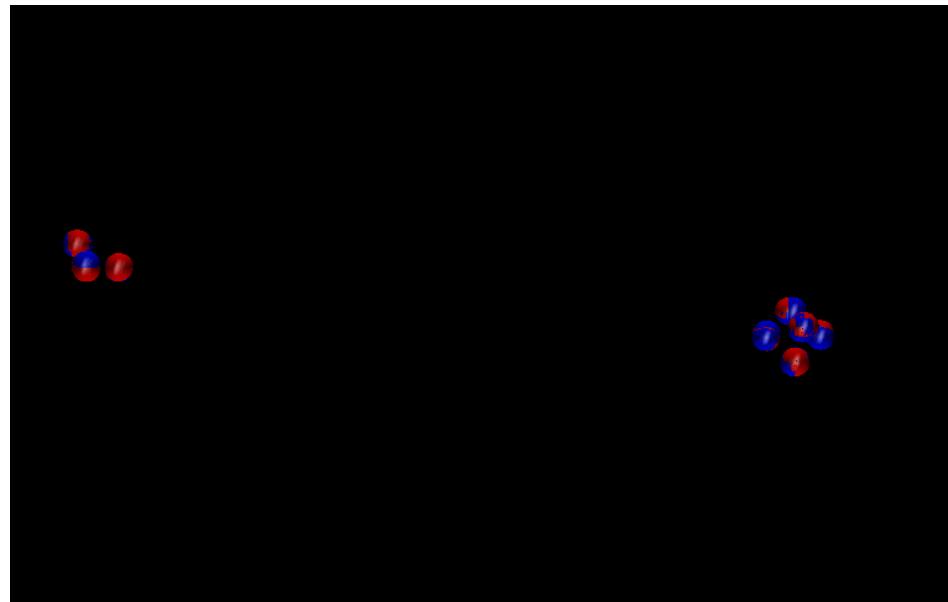
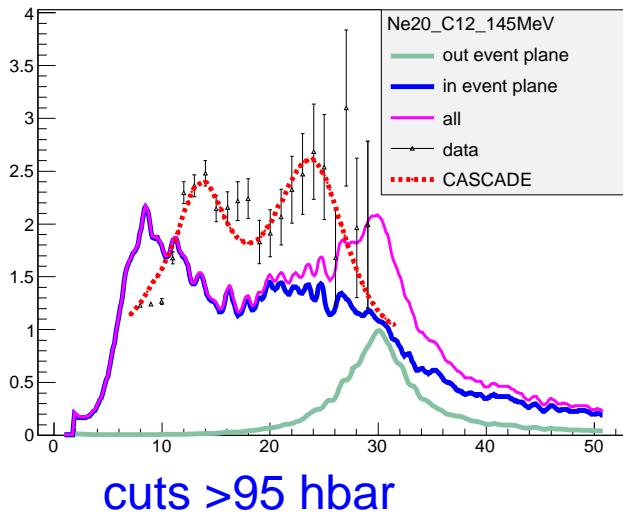
## □ GDR algorithm & verification

-- verification the reliability of EQMD in GDR calculations

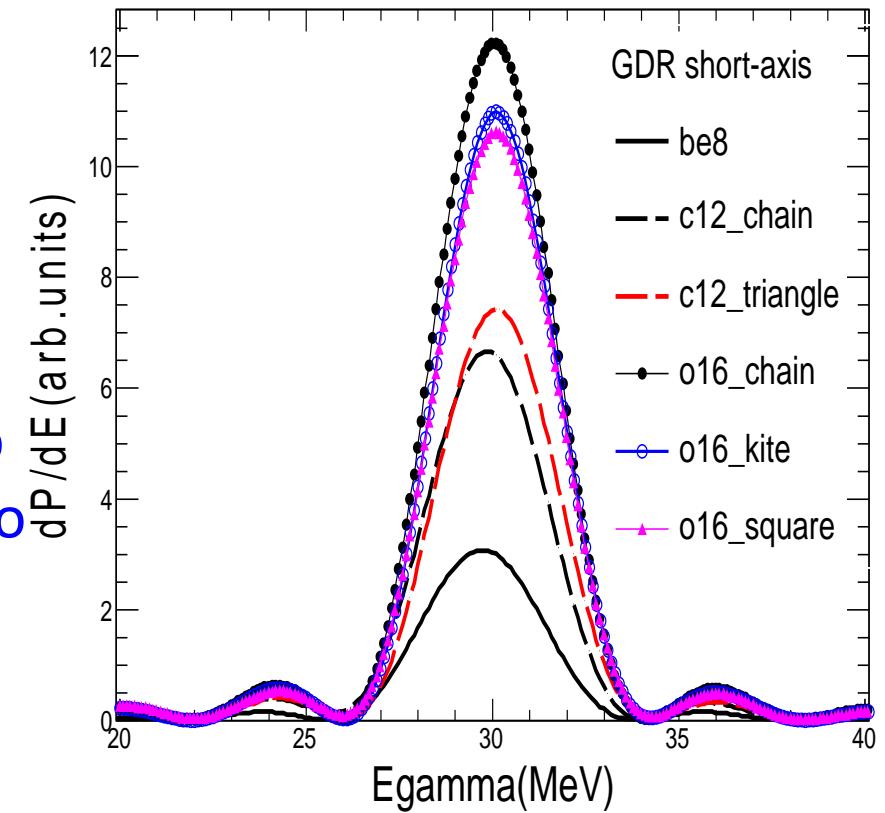
### GDR in fusion reaction

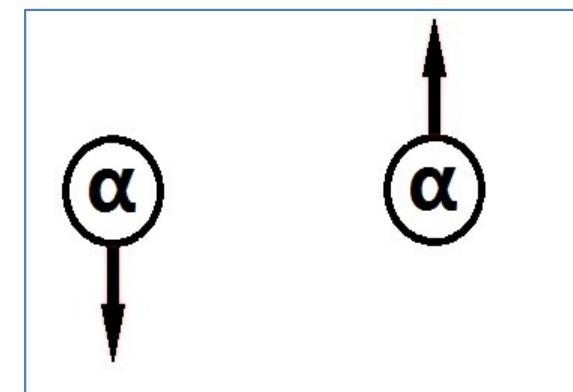
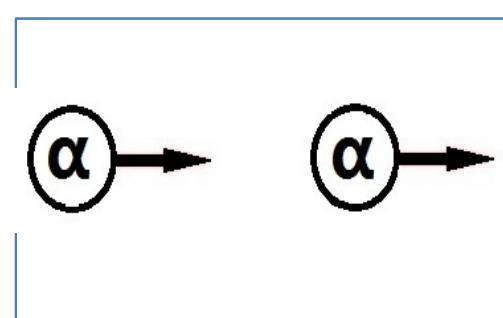
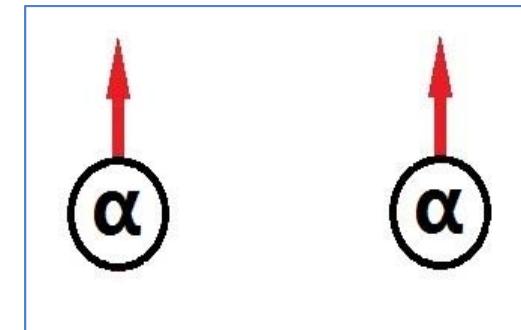
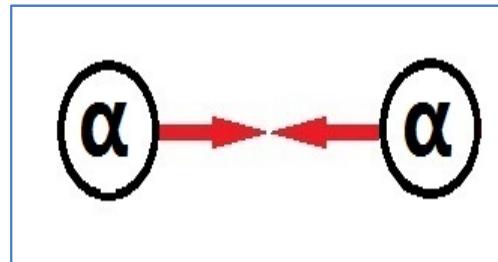
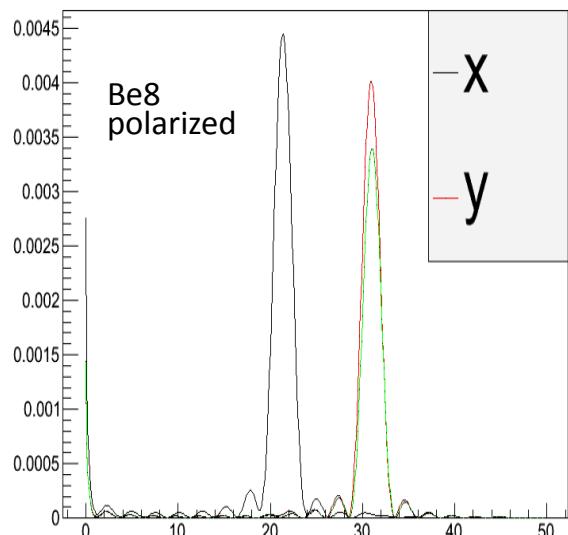


the data is from D. Pandit et al, Phys. Rev. C 81, 061302 (2010)



The strength perpendicular has strong correlation with the number of alphas: more alphas, more big strength. The relationship is not a simple linear relation due to the interaction among alphas, which can be seen clearly in next several slides.



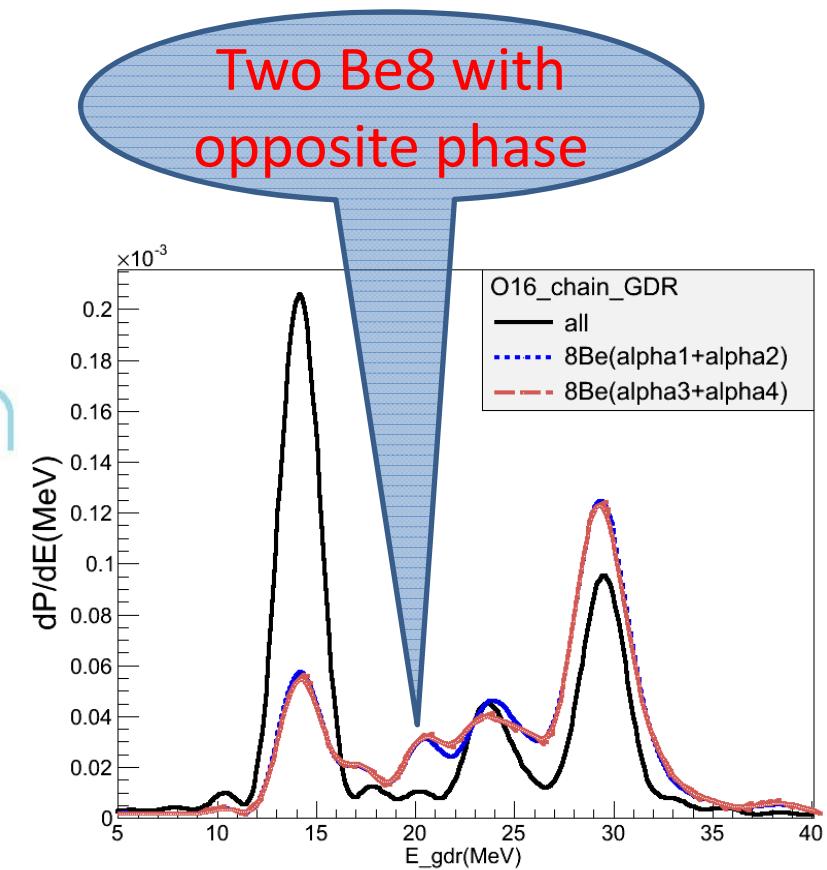
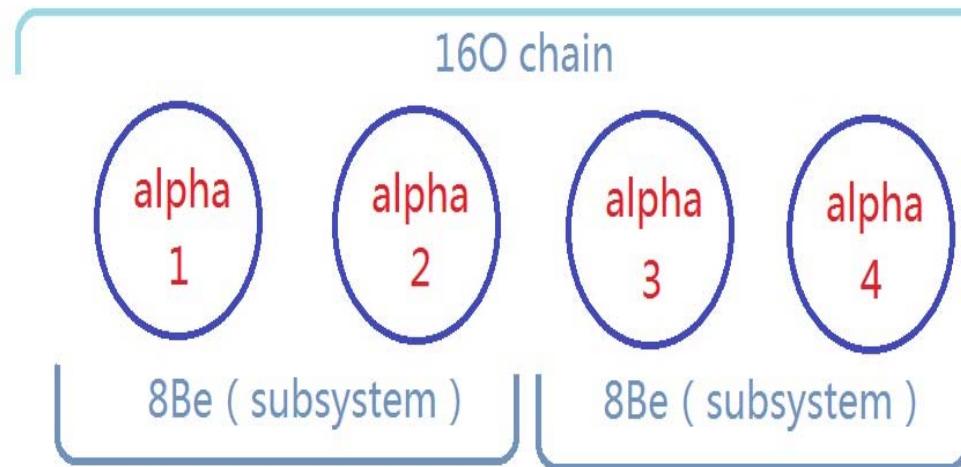


This figure shows dipole moment rather than motion in two direction.

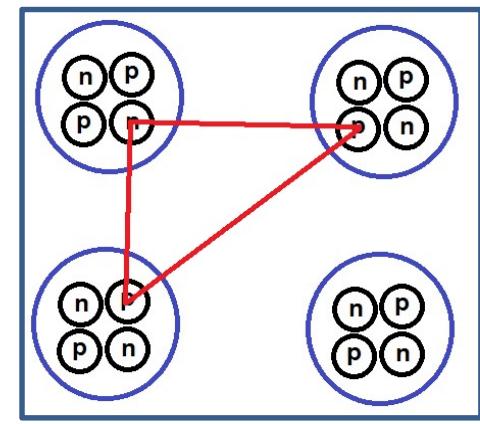
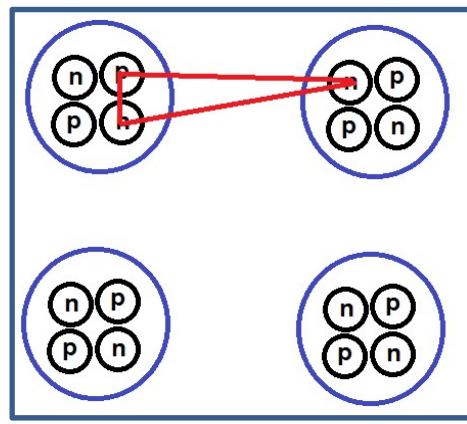
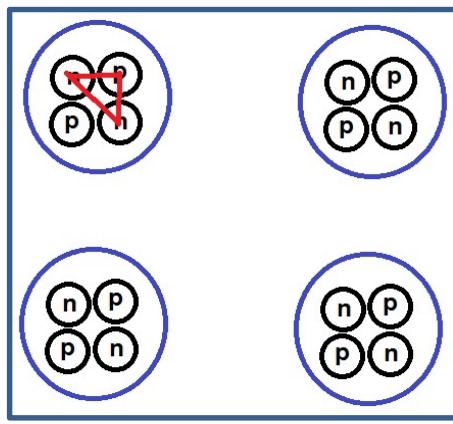
The **red arrow** shows high frequency component  
The black arrow shows low frequency component

The substructure of Be8 in O16 GDR is shown in the following figures. In right figure, the blue dotted and red dashed line represent two substructures.

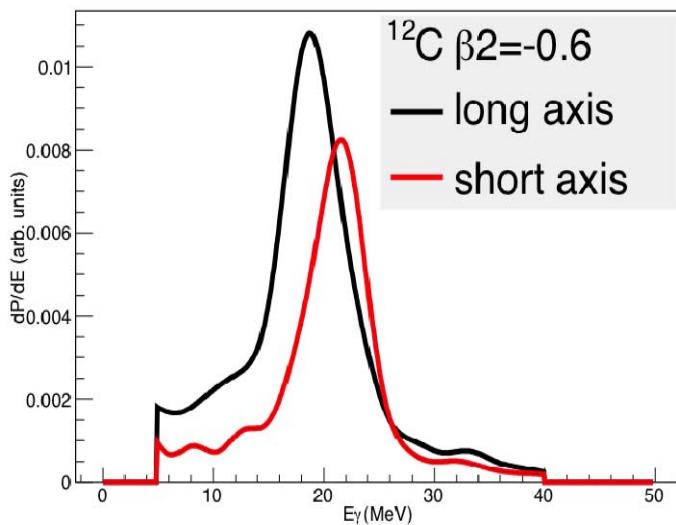
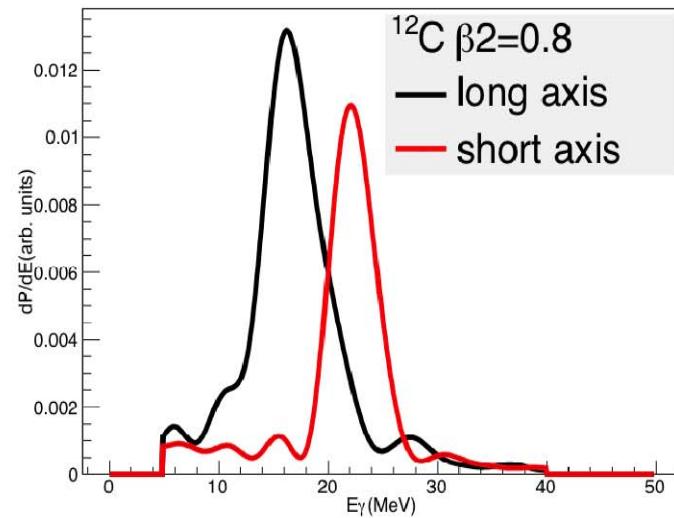
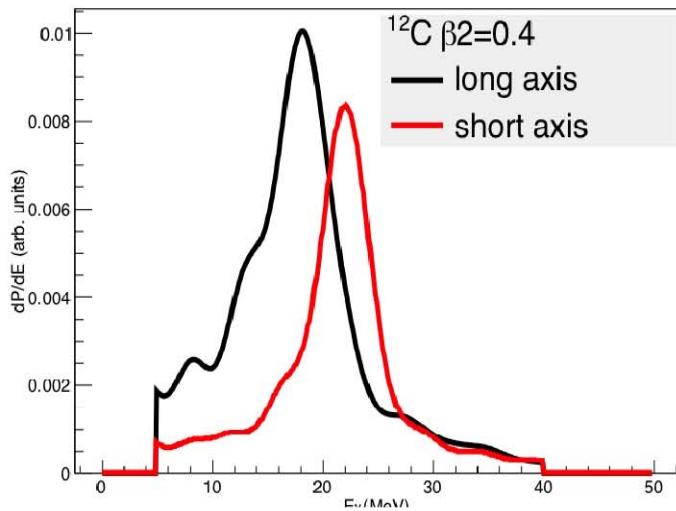
The peaks near 20MeV in GDR from two Be8 counteract because of the opposite phase.



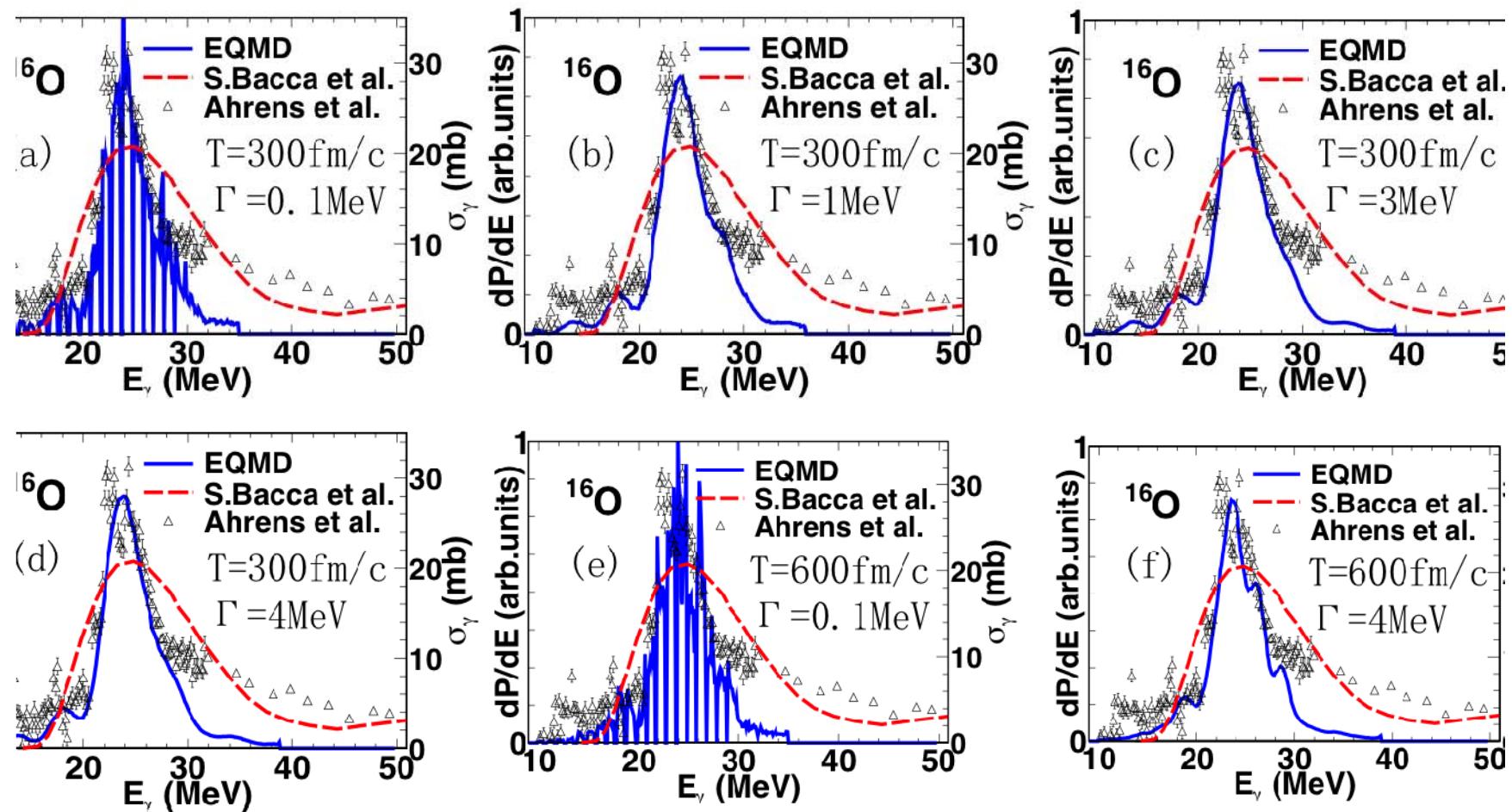
Three body force has three cases in cluster nuclei made of alphas as shown in following three figures. 25 MeV peak in GDR is affected by the third case. The third case manifests as effective three alpha force among alphas. This effective three alpha force favors triangle configuration.



# The GDR of $^{12}\text{C}$ with prolate and oblate deformations.



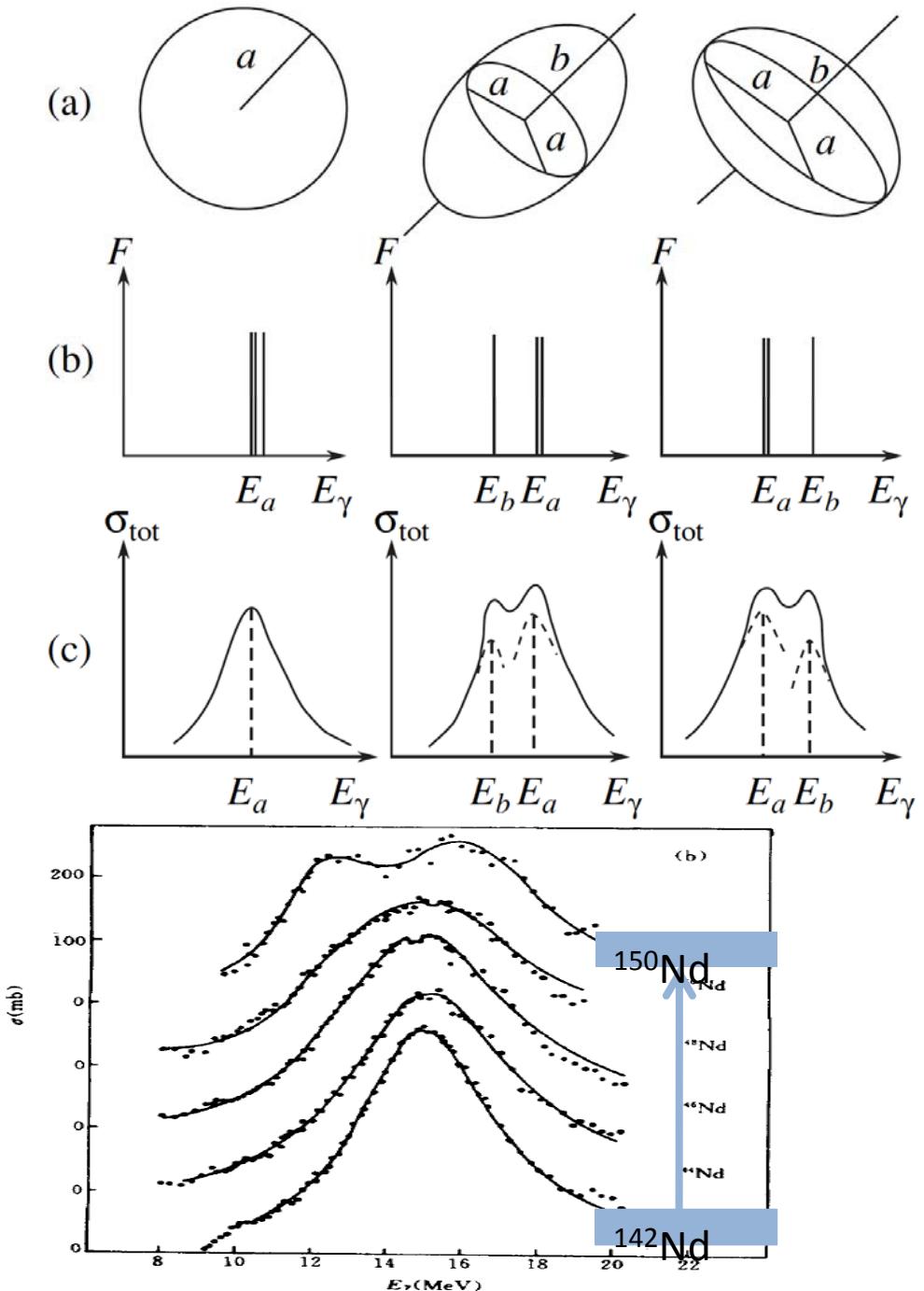
# The dependence $^{16}\text{O}$ GDR width on smoothing factor $\Gamma$ and integration time



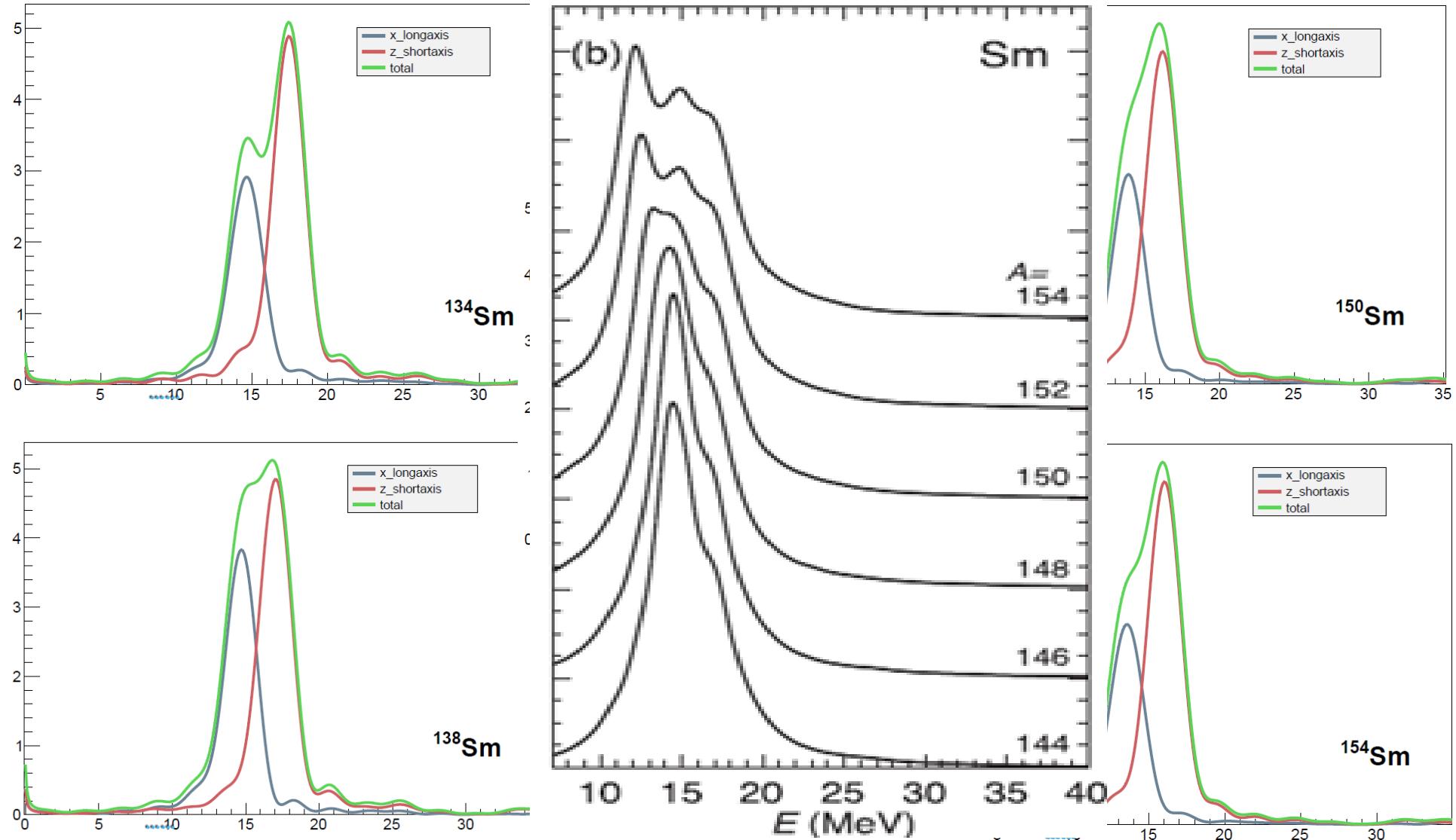
# Background

◆ 球形核沿三个轴的振动频率是相同的，因此共振为单峰。而旋转椭球形核沿长轴与短轴的振动频率会有差异，前者频率低于后者，因此共振呈双峰结构；而且对于长椭球变形核的低频振动强度应为高频成分的二分之一，反之则为扁椭球变形核。因此共振峰能反映核的形状。

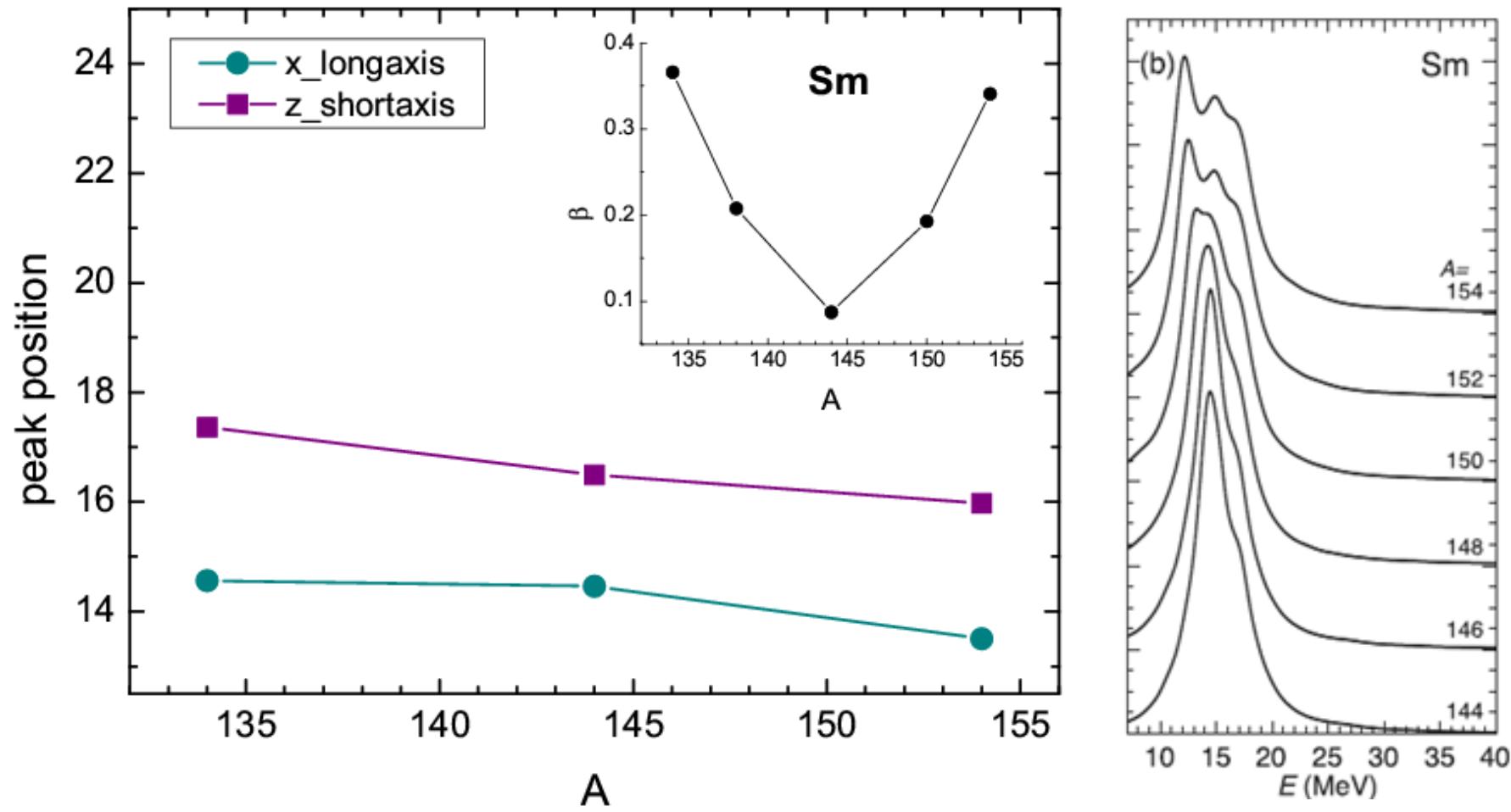
◆ 形变核有两个共振峰，被解释为原子核吸收E1辐射后引起中子流与质子流相对于共有的质心的振动，为电偶极振动，其恢复力是对称能。



# GDR in deformation nuclei



# GDR in deformation nuclei



# Background

## ■ QMD、AMD、FMD

- QMD不适用于研究低能核反应（例融合、裂变、深度非弹性碰撞）
- AMD和FMD计算重系统时，要花费大量的CPU时间

## ■ EQMD模型的改进之处

- 有效相互作用中引入Pauli势，体现核子的费米属性
- 把波包变化动能项考虑到系统的Hamiltonian中
- 核子波函数中引入复数变量的波包宽度，波包宽度的演化用变分原理处理

# Background

系统总的波函数

$$\Psi = \prod_i \phi_i(\mathbf{r}_i)$$

其中， $\phi_i(\mathbf{r}_i) = \left( \frac{\nu_i + \nu_i^*}{2\pi} \right)^{3/4} \exp \left[ -\frac{\nu_i}{2} (\mathbf{r}_i - \mathbf{R}_i)^2 + \frac{i}{\hbar} \mathbf{P}_i \cdot \mathbf{r}_i \right]$

$$\nu_i \equiv \frac{1}{\lambda_i} + i\delta_i$$

高斯波包宽度

其中 $\lambda_i$ 和 $\delta_i$ 分别代表核子坐标和动量空间宽度， $\mathbf{R}_i$ 、 $\mathbf{P}_i$ 、 $\lambda_i$ 和 $\delta_i$ 随时间的演化由时间依赖的变分原理得到。

四种相互作用

$$H_{\text{int}} = H_{\text{Skyrme}} + H_{\text{Coulomb}} + H_{\text{symmetry}} + H_{\text{Pauli}}$$

T.Maruyama et al. Phys. Rev. C 53, 297 (1996)