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Welcome to Henan Normal University

PKU-CUSTIPEN Nuclear Reaction Workshop on  
"Reactions and Spectroscopy of Unstable Nuclei"

# Isobaric yield ratio difference (IBD) and nuclear density determination

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# Outline

- \* 1. Background and Motivation
- \* 2. IBD Method
- \* 3. SAA model
- \* 4. Results and discussion
- \* 5. Conclusions

# 1. Background and motivation

- \* Measurement of nuclear density and nuclear symmetry energy (NSE) is an important question in nuclear physics.
- \* **NSE depends on nuclear density and temperature.**
- \* Heavy-ion collisions (HIC) can produce nuclear matters from sub-saturation to supra-saturation densities, making HIC be the unique method studying NSE in lab.
- \* **Nuclear density (and NSE) can not be measured directly. It is still an important task to find new probes to nuclear density and NSE.**
  - \* Neutron density
  - \* supra-saturation nuclear matter in compressed zones of HIC.

# 1. Background and motivation

- \* An **isobaric yield ratio difference (IBD)** method is proven to be sensitive to the density difference between nuclei
- \* **Isobaric yield ratio (IYR)** is defined as the ratio between isobars differing two in  $I=N-Z$
- \*  $R=y(A,I+2)/y(A,I)$ ,
  - \*  $y(A,I) = CA^{\tau} \exp\{[F(A,I) + N\mu_n + Z\mu_p]/T\}$
- \*  $R = \exp\{[F(A,I-2) - F(A,I) + \mu_n - \mu_p]/T\}$
- \* The systematic dependence of  $y$  cancels out in  $R$ .

grand-canonical ensembles theory, C. B. Das et al., PRC **64**, 044608 (2001).

Or modified Fisher model, M. Huang et al., PRC81 (2010) 044620; R. W. Minich et al., PLB 118 (1982) 458.

## 2. IBD method

\* In IYR

$$* R = \exp\{[F(A, I+2) - F(A, I) + \mu_n - \mu_p]/T\}$$

$$* \ln R = [\Delta F(A, I+2, I, A) + \Delta\mu_{np}]/T$$

F depends on temperature

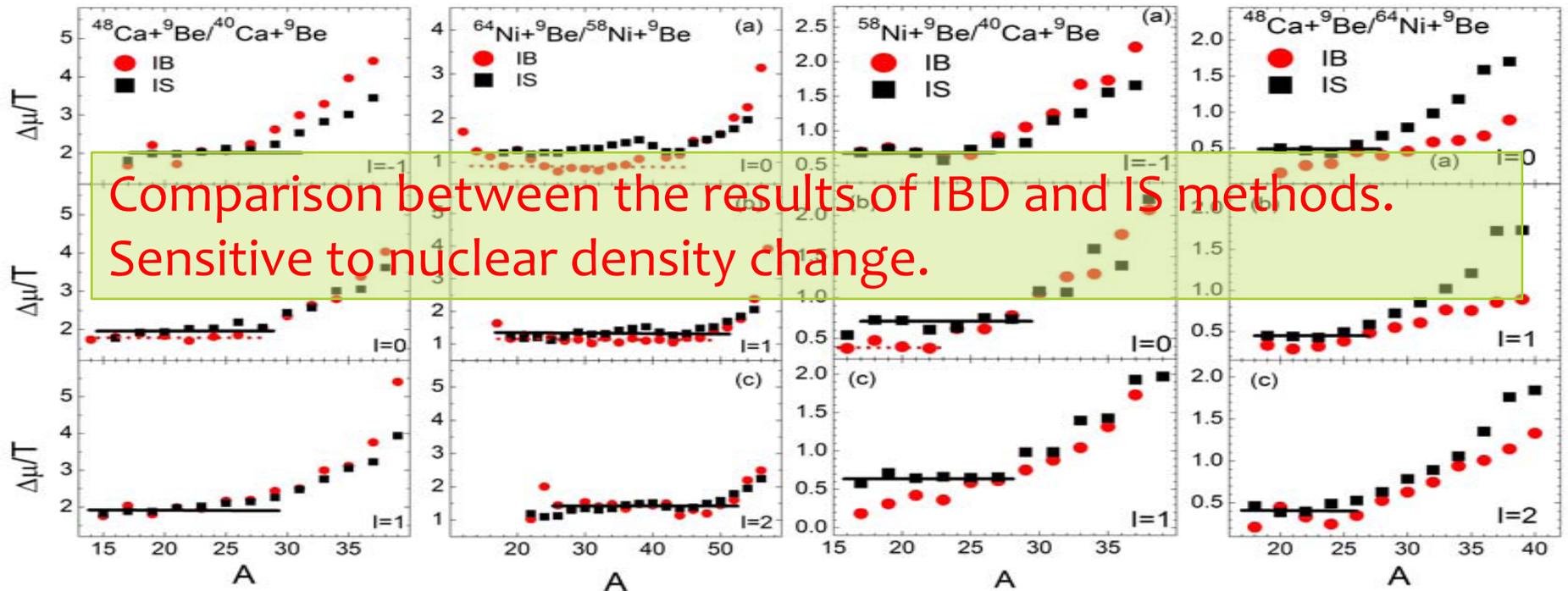
$$* \Delta\mu_{np} = \mu_n - \mu_p$$

\* **Define the difference between IYRs in 2 reactions, namely IBD,**

$$\begin{aligned} * \Delta_{21}\ln R &= \frac{[(\mu_{np})_2 - (\mu_{np})_1]}{T} \\ &= \frac{[\mu_{n2} - \mu_{n1} - (\mu_{p2} - \mu_{p1})]}{T} = \frac{\Delta\mu_{n21} - \Delta\mu_{p21}}{T} \end{aligned}$$

$\Delta F$  cancels out in IBD.  
Assuming T is the same in reactions.

## 2. IBD method



\* Comparing to isoscaling

$$* \alpha = (\mu_{n2} - \mu_{n1})/T = \Delta\mu_{n21}/T;$$

$$* \beta = (\mu_{p2} - \mu_{p1})/T = \Delta\mu_{p21}/T;$$

\* IBD and isoscaling

$$* \Delta_{21} \ln R = \frac{\Delta\mu_{n21} - \Delta\mu_{p21}}{T} = \alpha - \beta$$

## 2. IBD method

### Chemical potential and nuclear density

- \*  $\alpha = \ln \rho_{n2} - \ln \rho_{n1};$

- \*  $\beta = \ln \rho_{p2} - \ln \rho_{p1};$

- \* Denoting the density difference between the reactions.

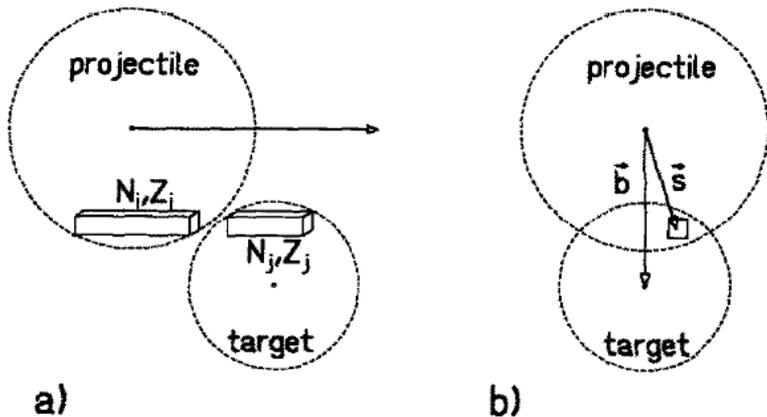
- \* For IBD,

- \* 
$$\begin{aligned} \Delta_{21} \ln R &= \alpha - \beta = \ln \rho_{n2} - \ln \rho_{n1} - (\ln \rho_{p2} - \ln \rho_{p1}) \\ &= \Delta(\ln \rho_n)_{21} - \Delta(\ln \rho_n)_{21} \\ &= \ln \rho_{n2} - \ln \rho_{p1} - (\ln \rho_{n1} - \ln \rho_{p1}) \\ &= \Delta(\ln \rho_{np})_{21} - \Delta(\ln \rho_{np})_{21} \end{aligned}$$

Isoscaling parameters  
and nuclear density.

# 3. SAA model

- \* Statistical abrasion-ablation model
- \* Abrasion-stage (pre-fragment determination)
- \* evaporation-stage (final fragment determination)



- \* Projectile and target nuclei are divided into independent tubes
- \* Neutron and proton densities discriminated (Fang et al.)
- \*  $\rho_n, \rho_p$

# 3. SAA model

- \* pre-fragment determination
- \* Nucleons abraded from the overlapping tubes

$$\langle \Delta A(b) \rangle = \int d^2s \rho_n^P(s) [1 - t_n(s - b)] \\ + \int d^2s \rho_p^P(s) [1 - t_p(s - b)],$$

- \*  $t_n(\mathbf{s}-\mathbf{b})$ ,  $t_p(\mathbf{s}-\mathbf{b})$ : transmission probability for neutrons and protons at  $\mathbf{b}$ ,  
 $t_k(\mathbf{s} - \mathbf{b}) = \exp\{-[\rho_n^T(\mathbf{s} - \mathbf{b})\sigma_{nk} + \rho_p^T(\mathbf{s} - \mathbf{b})\sigma_{pk}]\}$ ,
- \* Cross sections of a prefragment with **N neutrons** and **Z protons** abraded,

$$\sigma(\Delta N, \Delta Z) = \int d^2b P(\Delta N, b) P(\Delta Z, b),$$

Cross section of prefragment is mainly determined by density and nucleus-nucleus reaction cross sections.

# 3. SAA model

- \* Fermi-type density distributions of nucleus

$$\rho_k(r) = \frac{\rho_k^0}{1 + \exp\left(\frac{r - C_k}{t_k f_k / 4.4}\right)}, \quad k = n, p$$

- \*  $t_k$  diffuseness,  $f_k$  introduced to adjust  $t_k$ . The increase of  $f_k$  will push nucleons from core to surface of nucleus.

- A. Fermi-type density distribution, Ozawa, T. Suzuki, I. Tanihata, Nucl. Phys. A **693**, 32 (2001);
- B.  $f_n$  is introduced in C. W. Ma, Y. Fu, D. Q. Fang, Chin. Phys. B **17** (2008) 1216.

# 3. SAA model

- \* Evaporation process—decay of hot prefragment

- \* Excitation energy ( $E^*$ ) of prefragment

$$E^* = 13.3 \langle A(b) \rangle \text{MeV}$$

- \* Excitation energy for per abraded nucleon **13.3** MeV.

- \*  $\langle A(b) \rangle$  abraded nucleons from projectile at  $b$ .

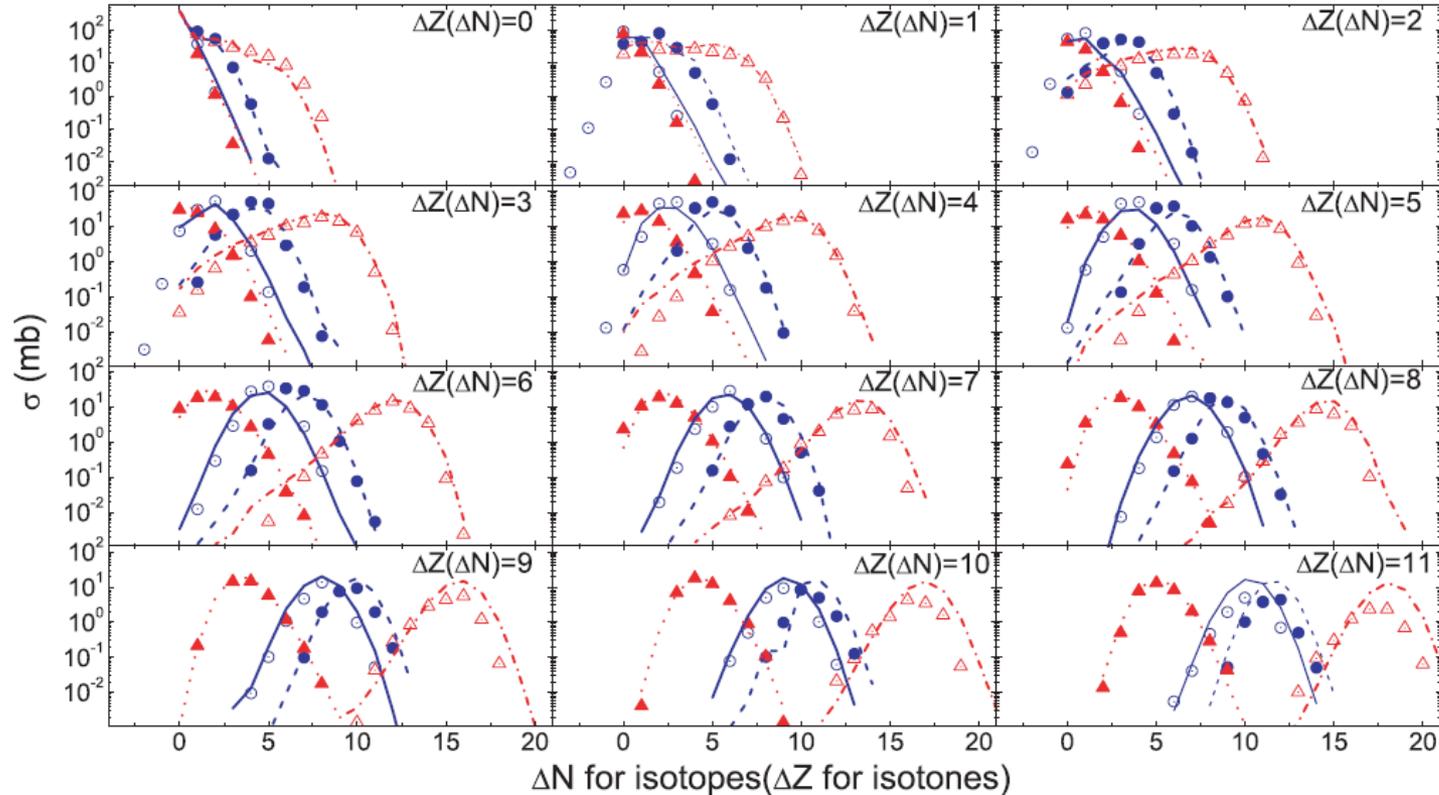
- \* Prefragment ( $N, Z$ ) decays by emitting  $n$ ,  $p$  or  $\alpha$ , until the residue is stable.

- \* The **emitting particle** is selected according to  $\min(s_n, s_p, s_\alpha)$  of prefragment ( $N, Z$ ).

Comparing with GEMINI and SMM, the decay method of SAA is an simple way to determine the final fragment.

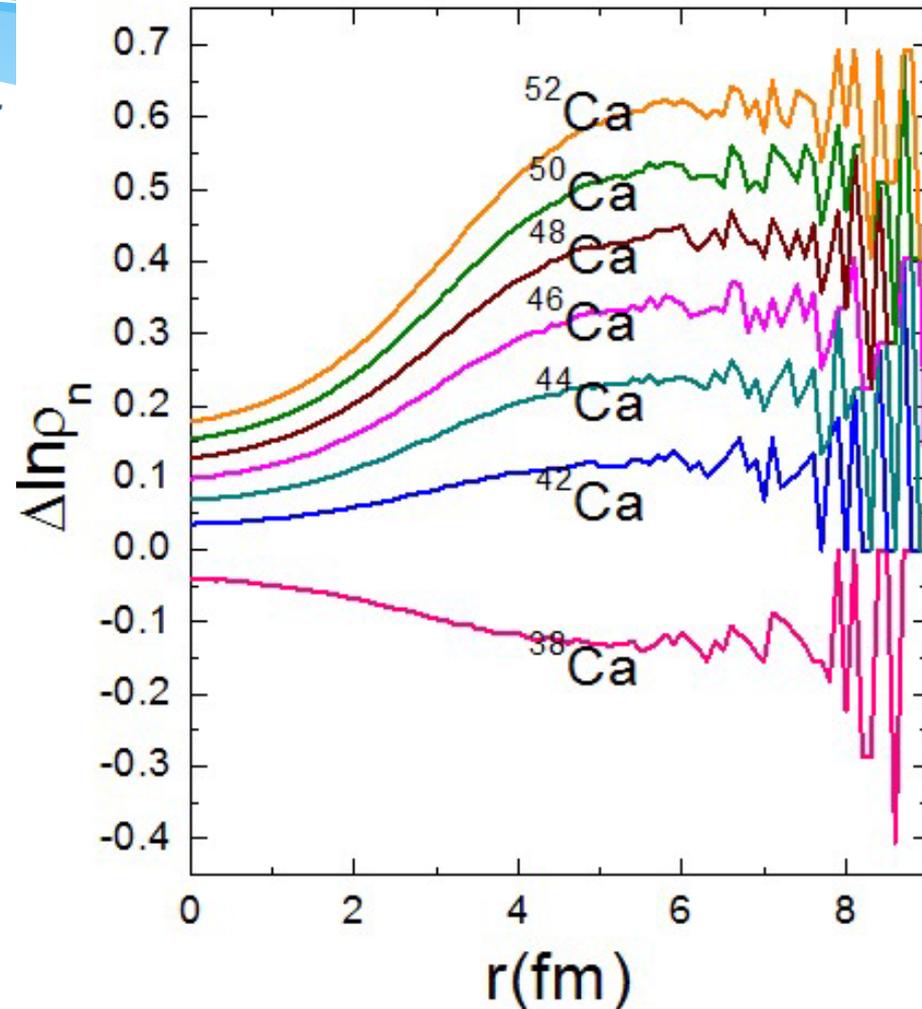
# 3. SAA model

- \* SAA (lines) can well reproduce the measured data (symbols)



# 4. Results and discussion

- \* The calculated 80A MeV Ca +  $^{12}\text{C}$  reactions by using a modified statistical abrasion ablation model
- \* 38, 40, 42, 44, 46, 48, 50, 52Ca as projectiles
- \* Neutron density difference
- \*  $\Delta_{21}\ln R = \Delta(\ln\rho_n)_{21}$



# 4. Results and discussion

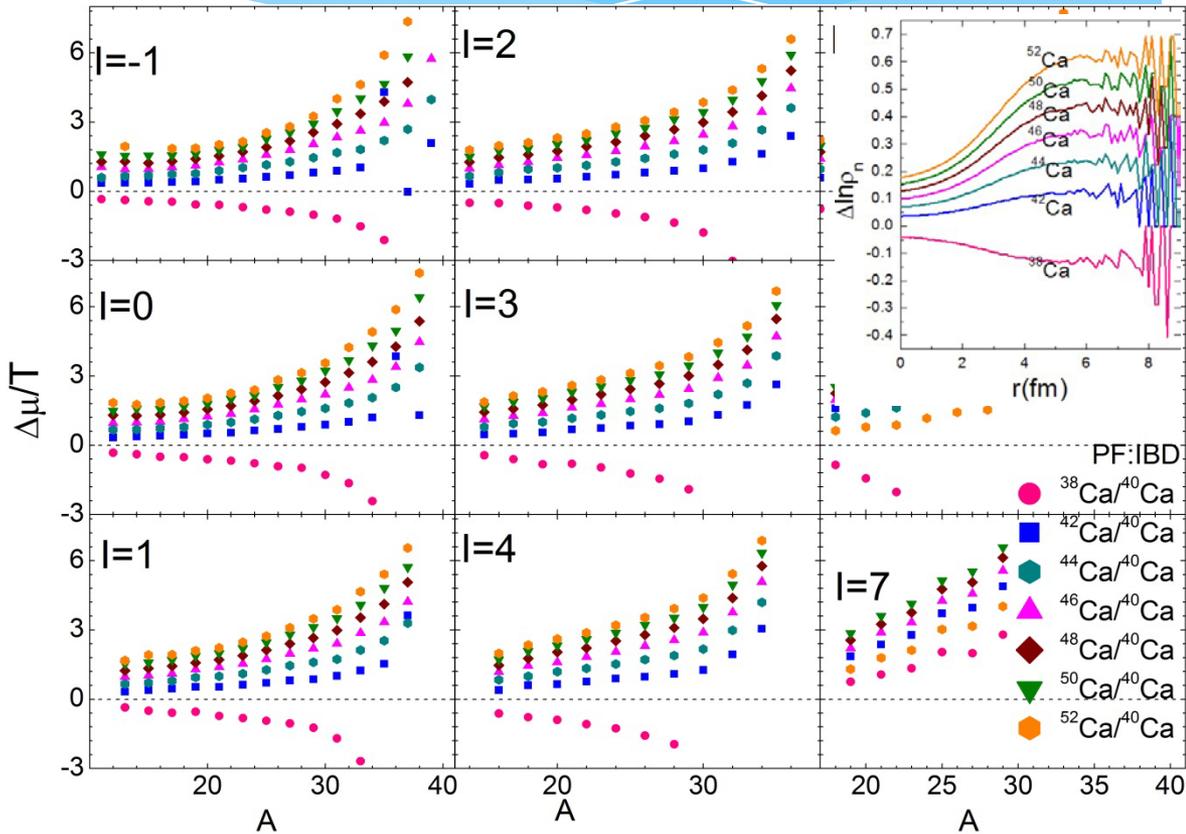
- \* prefragments
- \* IBD-plateaus
- \* Height increases with n/z of projectile

- \*  $\Delta_{21} \ln R$   
 $= \Delta(\ln \rho_n)_{21} - \Delta(\ln \rho_n)_{21}$

- \* Assuming the proton density distributions of  $^X\text{Ca}$  are the same

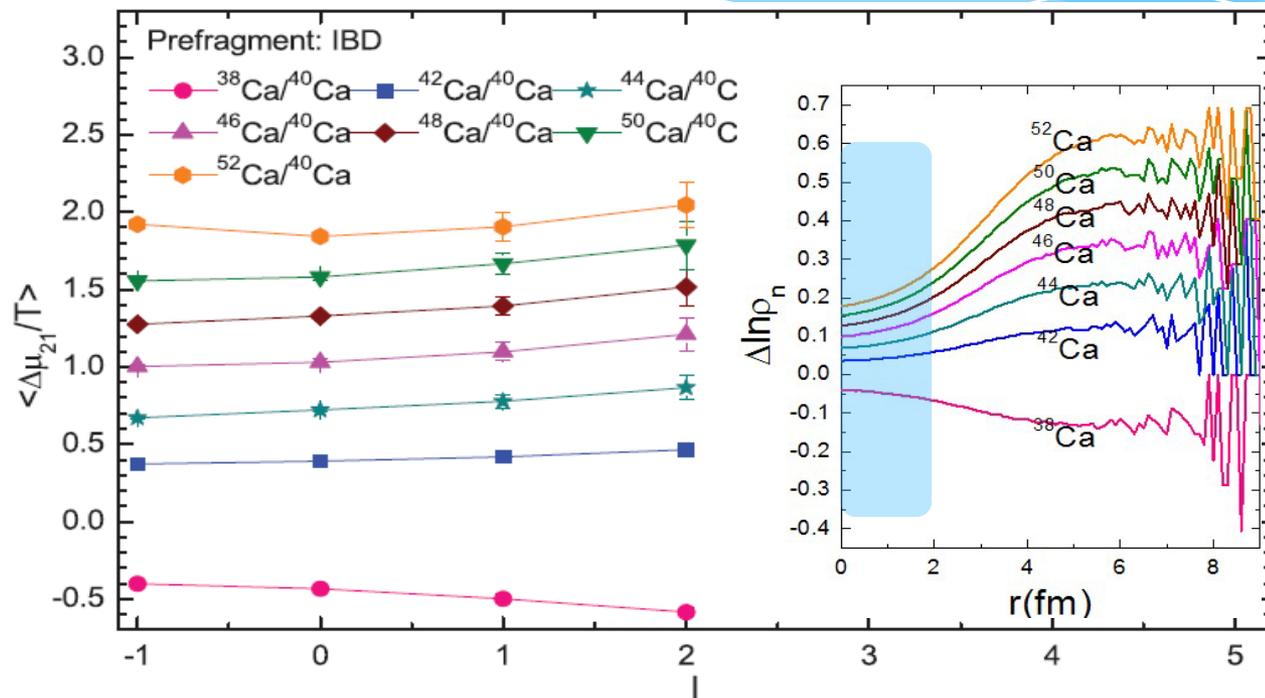
- \*  $\Delta_{21} \ln R = \Delta(\ln \rho_n)_{21}$

- \* H of Plateau sensitive to  $\Delta(\ln \rho_n)_{21}$



Similar trends of  $\Delta\mu_{n21}/T$  and  $\Delta \ln \rho_n$   $r < 6$  fm

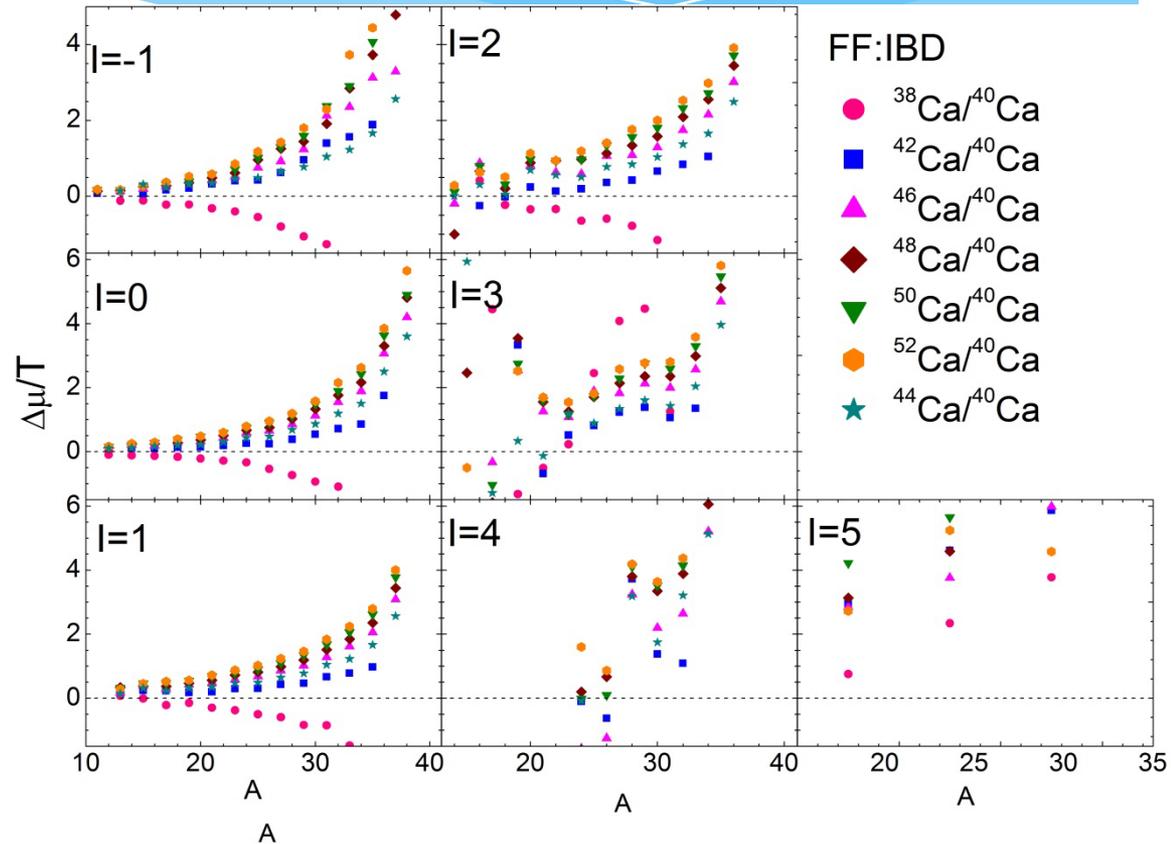
# 4. Results and discussion



- \* Averaged values of plateaus  $\langle \Delta\mu_{n21}/T \rangle$  vs.  $Z$  of fragments
- \*  $\langle \Delta\mu_{n21}/T \rangle$  changes little with  $Z$

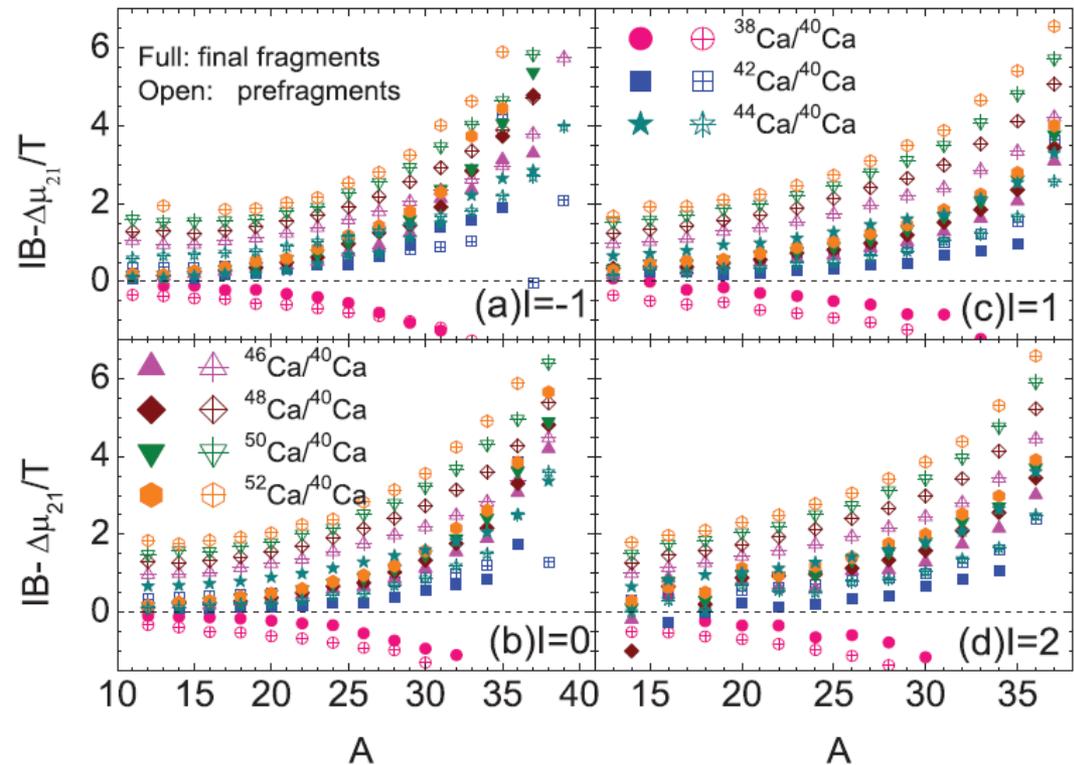
# 4. Results and discussion

- \* Final fragments
- \* IBD-plateaus
- \* Height also increases with  $n/z$  of projectile
- \* H of Plateau less sensitive to  $\Delta(\ln\rho_n)_{21}$
- \* Plateau disappears in neutron-rich fragments



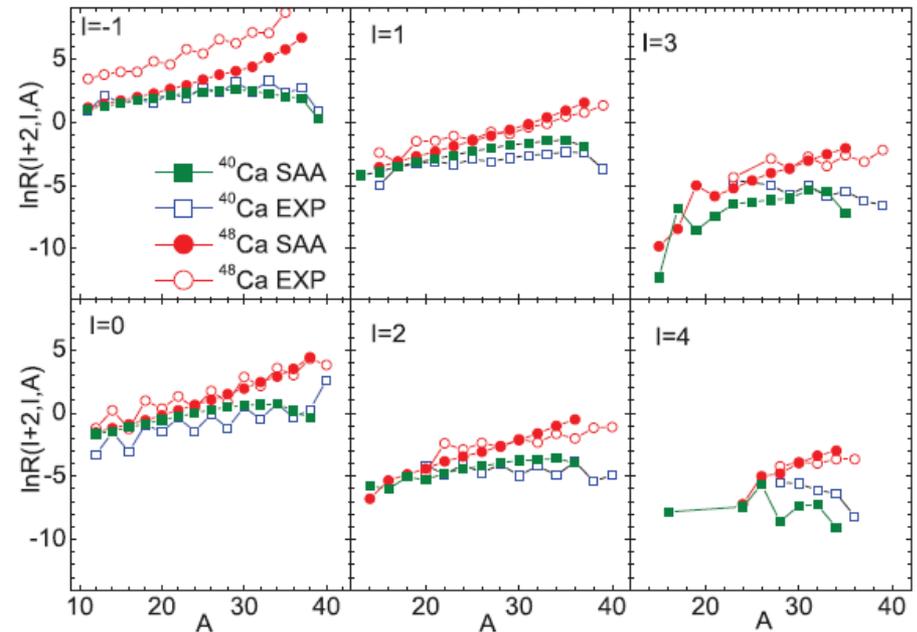
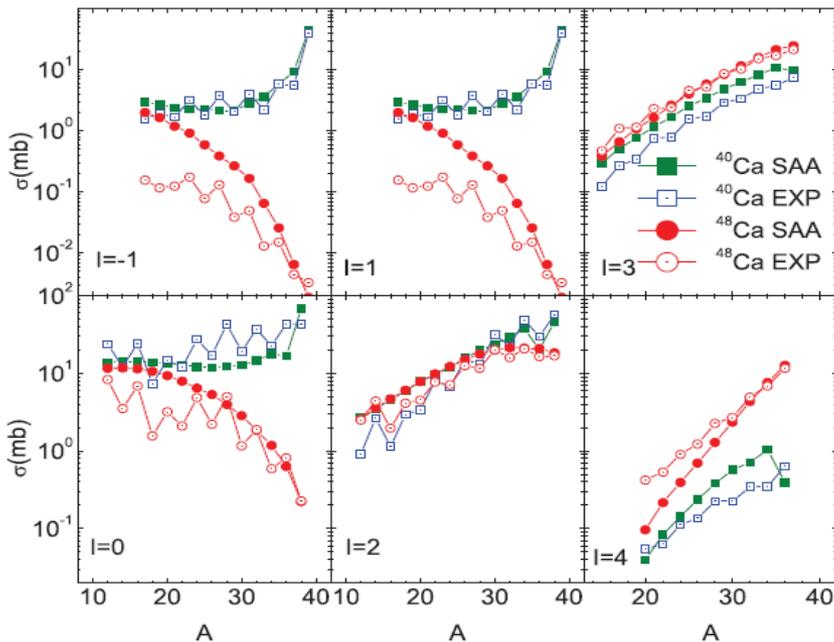
# 4. Results and discussion

- \* Decay effects in IBD
- \* H of final fragments is suppressed, make H less sensitive to the density changes of Ca isotopes
- \* Prefrags. IBD
- \* SAA~1.75
  - \* Final frags. IBD
  - \* SAA ~0.5, exp. ~2



# 4. Results and discussion

- \* SAA well reproduces yields of frag. in  $^{40}\text{Ca}$  reaction, but overestimates yields of frags with small  $A$  in the  $l=-1, 0$  and  $1$  chains in the  $^{48}\text{Ca}+\text{C}$  reaction.
- \* SAA underestimate IYR for  $l=-1$  frags in the  $^{48}\text{Ca}+\text{C}$  reaction.
- \* The decay calculations should account for the difference between IYRs for reactions of neutron-rich projectile nucleus.



# 5. Conclusions

- \* Experimentally, IBD is sensitive to density difference between projectiles.
- \* IBD from SAA prefrags **is sensitive to** the density difference between projectiles. While IBD from SAA final frags **is suppressed and is less sensitive** to the density difference between projectiles.
- \* The decay calculation for small A fragments should be modified.
- \* **More works should be carried out on the IBD probes both theoretically and experimentally.**

More discussion on the IBD method, please refer to:

Ma C W, Wang S S, Zhang Y L, Wei H L, [PRC87, 034618 \(2013\)](#); [JPG 40 \(2013\) 125106](#);  
C. W. Ma, J. Yu, X. M. Bai, Y. L. Zhang, H. L. Wei, S. S. Wang, [PRC 89, 057602 \(2014\)](#).

- \* Group members
- \* Wang Shan-Shan, Zhang Yan-Li, Qiao Chun-Yuan,  
Zhang Hui-Ping, Bai Xiao-Man, Yu Jiao

Thanks for your attention!