



Experimental studies on isospin chronology and the asymmetric nuclear EOS in heavy ion collisions

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TSINGHUA UNIVERSITY DEPARTMENT OF PHYSICS

Content

- 1. Introduction: Isospin transport in HIC and Isospin Chronology (5)**
- 2. Hanbury-Brown and Twiss Method (5)**
- 3. Isospin effect on HBT correlations in Heavy Ion Reactions (5)**
- 4. Summary (2')**



Symmetry Energy

$$B(Z, A) = B_v + B_s + B_c + B_a + B_p$$

$$= a_v A - a_s A^{2/3} - a_c Z^2 A^{-1/3} - \boxed{a_a (A/2 - Z)^2 A^{-1}} + a_p \delta A^{-1/2}$$

Symmetry Term

$$E(\rho, \delta) = E_0(\rho) + \delta^2 E_{\text{sym}}(\rho) = a_v + \frac{\kappa}{18} \varepsilon^2 + \frac{J}{162} \varepsilon^3 + \dots + \delta^2 \left(E_{\text{sym}} + \frac{L}{3} \varepsilon + \dots \right)$$

κ : Compressibility

$E_{\text{sym}}(\rho)$



(Neutron Star and NS Merge)

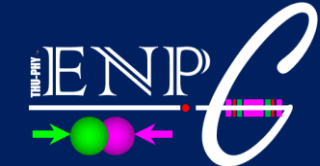


(Static or Resonant Properties of Nuclei)



(Heavy Ion Collisions)



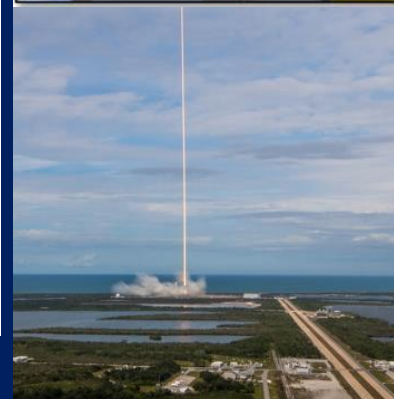
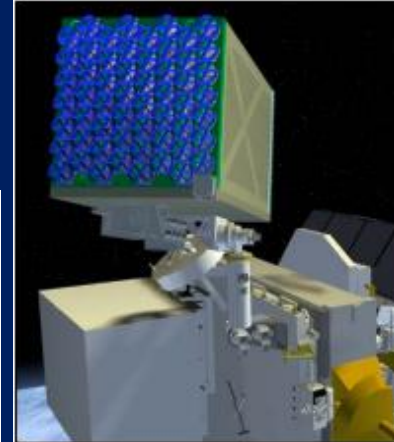
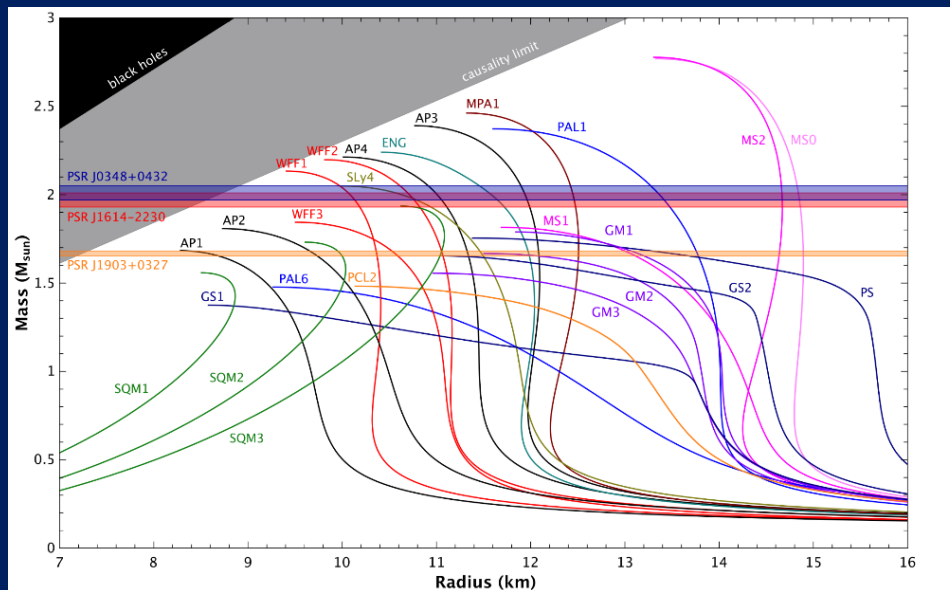


$E_{\text{sym}}(\rho)$ becomes a frontier in major Labs

Neutron Star Observatory:

The Neutron Star Interior Composition Explorer (NICER)

To Constrain EOS of nuclear matter through precise M and R measurements of several neutron stars.



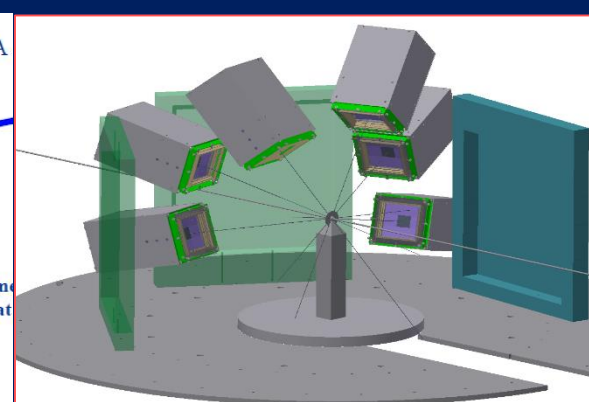
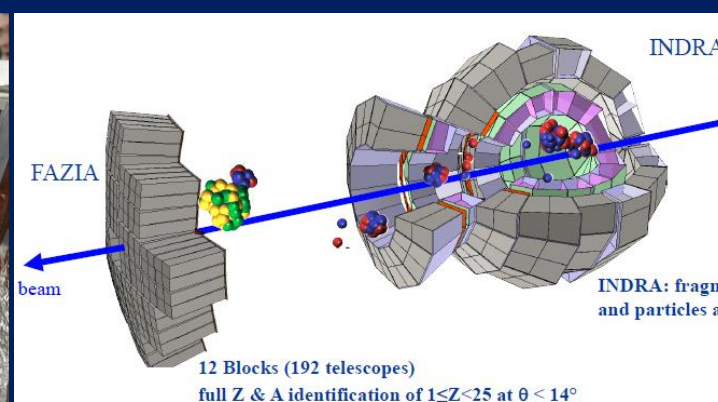
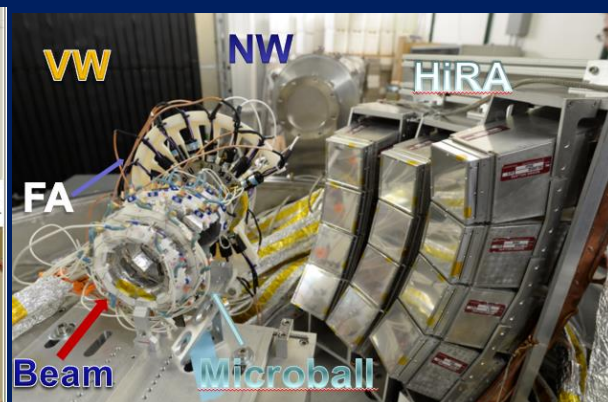
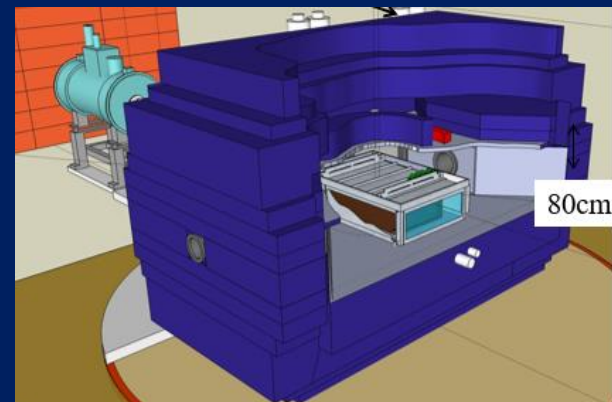
HI accelerator and RIB facilities:

SAMURAI-TPC@RIKEN

HIRA@NSCL, MSU

INDRA@GANIL

RIBLL @ HIRFL



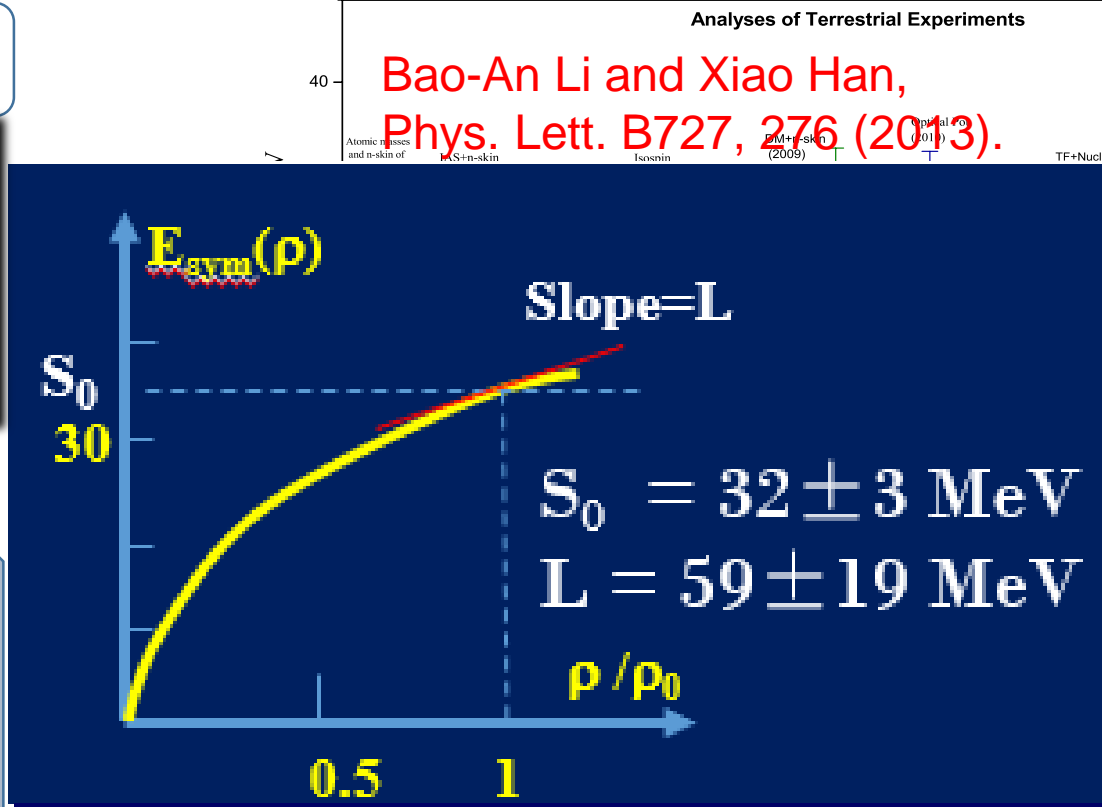
Isospin transport and the constraint of $E_{\text{sym}}(\rho)$

At sub-saturation densities



List extends:

- Isospin diffusion (MSU ...)
- Isospin scalaring and isospin fractionaiton (MSU...)
- n/p ratio of fast and pre-equilibrium nucleons (MSU ...)
- N/Z of the emitted fragments (LNS, TAMU, MSU, HIRFL ...)
- GMR strength (ND ...)
- HBT correlation function (KVI, MSU, HIRFL ...)
-



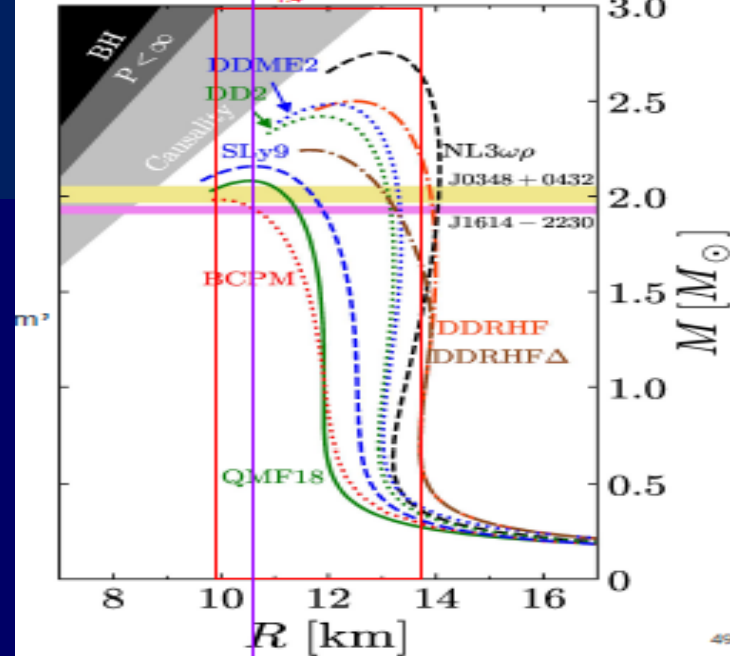
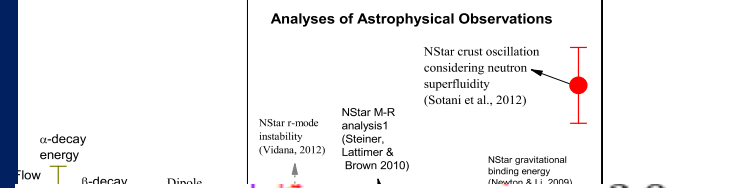
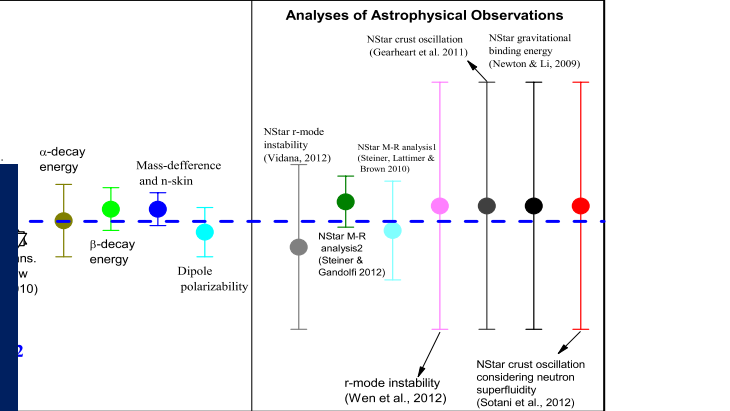
Globe Optical Potential Fit: $L=53 \pm 23 \text{ MeV}$
C. Xu et al, PRC 82, 054607 (2010)

Proton Emission: $L = 52 \pm 7 \text{ MeV}$
N. Wan et al., PRC 94, 044322 (2016)

GW170817 QMF18: $L=40 \text{ MeV}$

Ang Li et al., APJ, 862,98 (2018)

H. Sagawa's talk: $L=42 \pm 14$



Symmetry Energy and isospin transport in HIC

Two mechanisms governs the transport of IDOF in nuclear collisions:

1. Isospin Diffusion :

$$j_{np} = j_n^I - j_p^I = -(D_n^I - D_p^I) \nabla I$$

$$D_n^I - D_p^I \propto 4\rho E_{sym}(\rho)$$

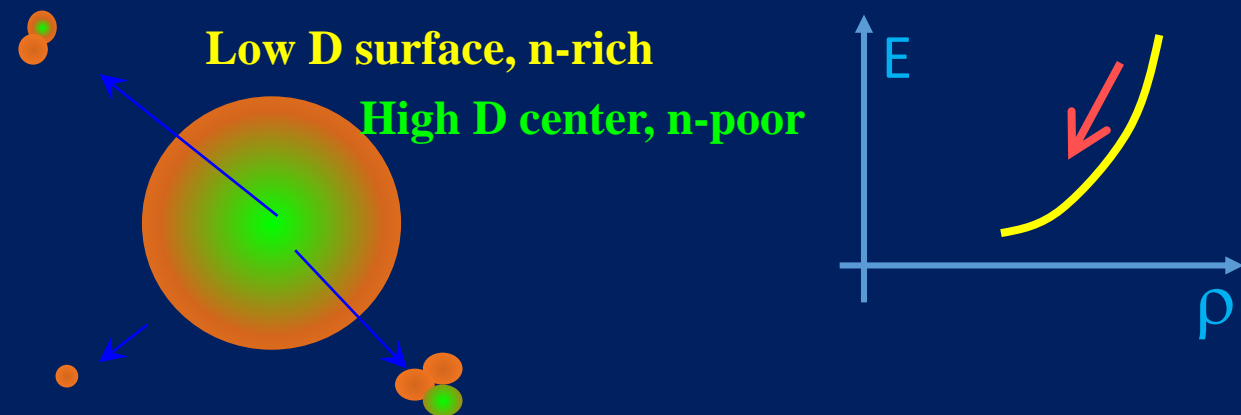


Likely terminated when P-T separated.

2. Isospin Drift :

$$j_{np} = j_n^\rho - j_p^\rho = (D_n^\rho - D_p^\rho) \nabla \rho$$

$$D_n^\rho - D_p^\rho \propto 4I \frac{\partial E_{sym}(\rho)}{\partial \rho}$$



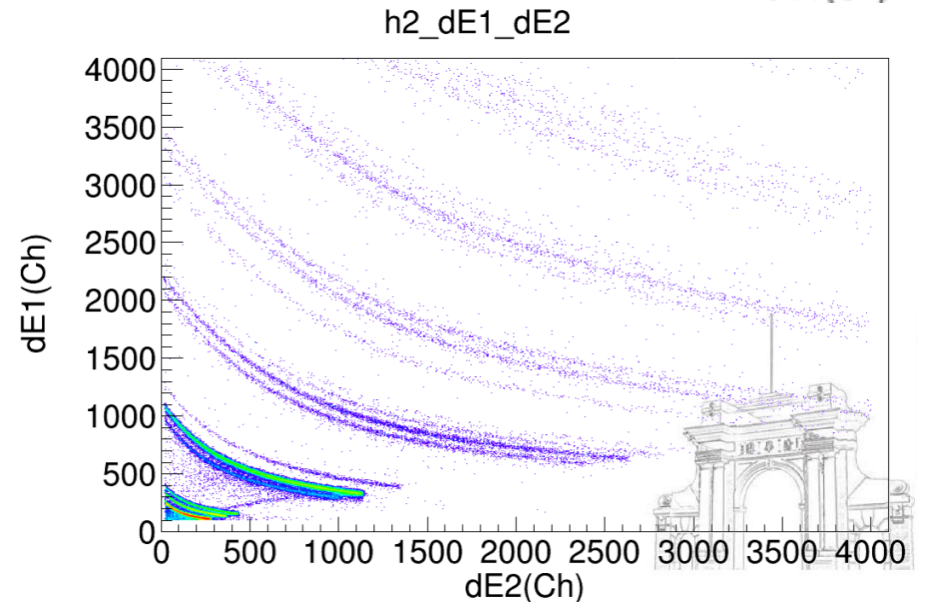
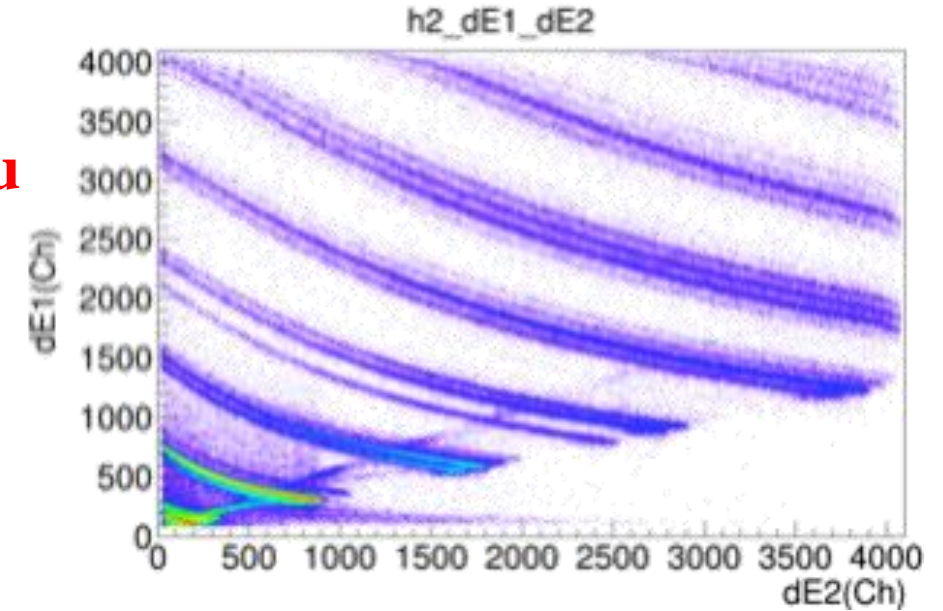
Likely persists for long time.

Long time isospin drift and the constraint of $E_{\text{sym}}(\rho)$



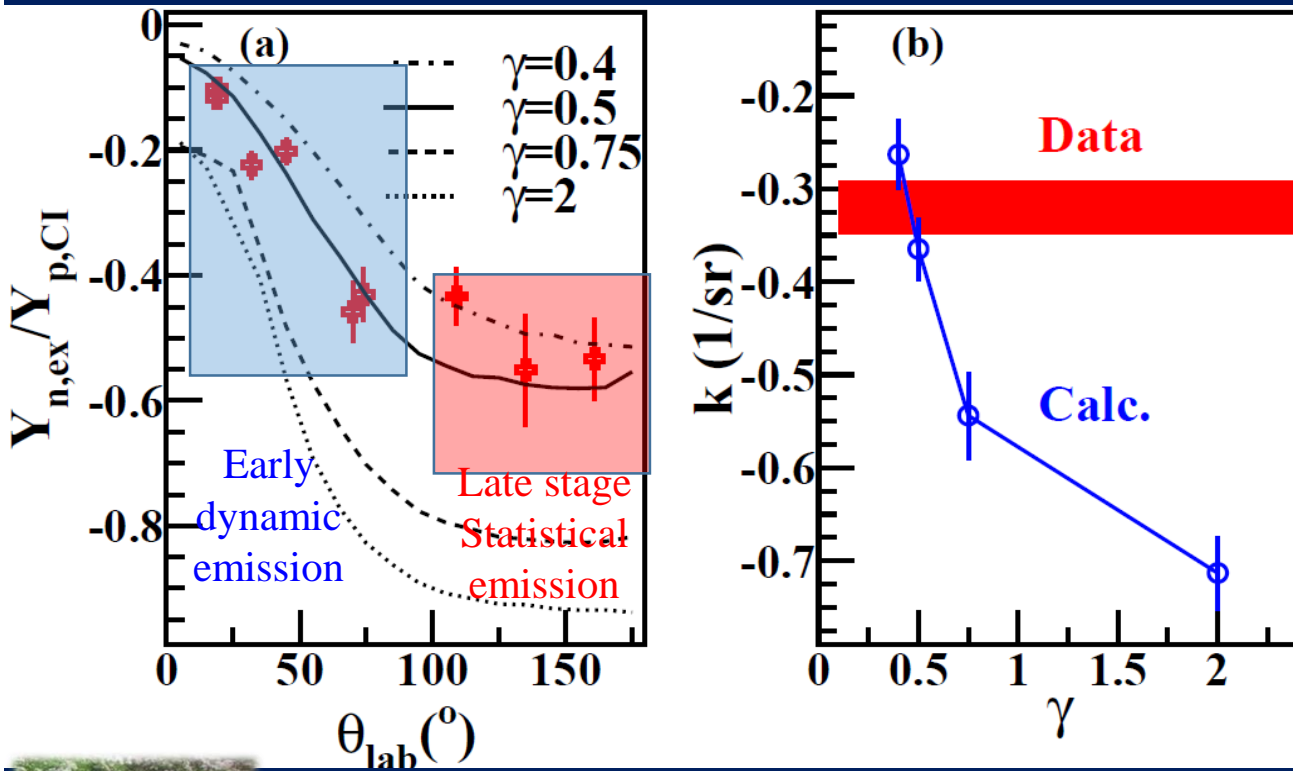
**30 MeV/u Ar+Au @
RIBLL, HIRFL, Lanzhou**

Telescope	Silicon1 (μm)	Silicon2 (μm)	CsI(cm)	Position (θ, φ)
Telescope1#	150	200	2*2*3	(37,69)
Telescope2#	75	200	2*2*3	(19,39)
Telescope3#	75	200	2*2*3	(19,39)
Telescope4#	50	200	2*2*3	(45,170)
Telescope5#	30	200	2*2*3	(74,39)
Telescope6#	50	300	1.5*1.5*2	(70,13)
Telescope7#	25	300	1.5*1.5*2	(161,37)
Telescope10#	30	200	2*2*3	(109,196)
Telescope11#	50	300	1.5*1.5*2	(135,110)



Constraint of the $E_{\text{sym}}(\rho)$ with IMQMD+GEMINI

$$\frac{Y_{n,\text{ex}}}{Y_{p,\text{CI}}} = \frac{\sum y_i (N_i - Z_i)}{\sum y_i Z_i} \quad \frac{Y_{n,\text{ex}}}{Y_{p,\text{CI}}} = k\theta_{\text{lab}} + b$$



1) In the wide angular range, the neutron richness decreases with angle in lab.
 → Isospin drift is long time process, persisting from early dynamic emission to late statistical emission

2) $E_{\text{sym}}(\rho)$: $\gamma = 0.46 \pm 0.025$ (STDEV)
 $L = 47 \pm 14$ MeV (CL=95%)
 with S_0 fixed at 28.3 MeV.

Globe Optical Potential Fit: $L = 52.7 \pm 22.5$ MeV PRC (2010)
 Proton Emission: $L = 51.8 \pm 7.2$ MeV, PRC(2016)
 GW170817 QMF18: $L = 40$ MeV APJ, (2018)
 IAS- ΔR_{np} , $L = 42 \pm 14$ MeV H. Sagawa's talk



Y. Zhang, ... ZGX, PRC 95, 041602(R) (2017)

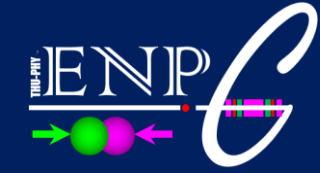
RAPID COMMUNICATIONS

PHYSICAL REVIEW C 95, 041602(R) (2017)

Long-time drift of the isospin degree of freedom in heavy ion collisions

Yan Zhang (张嫣),¹ Junlong Tian (田俊龙),^{2,*} Wenjing Cheng (程文静),¹ Fenhai Guan (关分海),¹ Yan Huang (黄彦),¹

- How long is long?
- How short is short?
- How do we measure?



Content

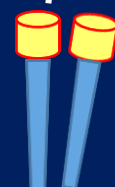
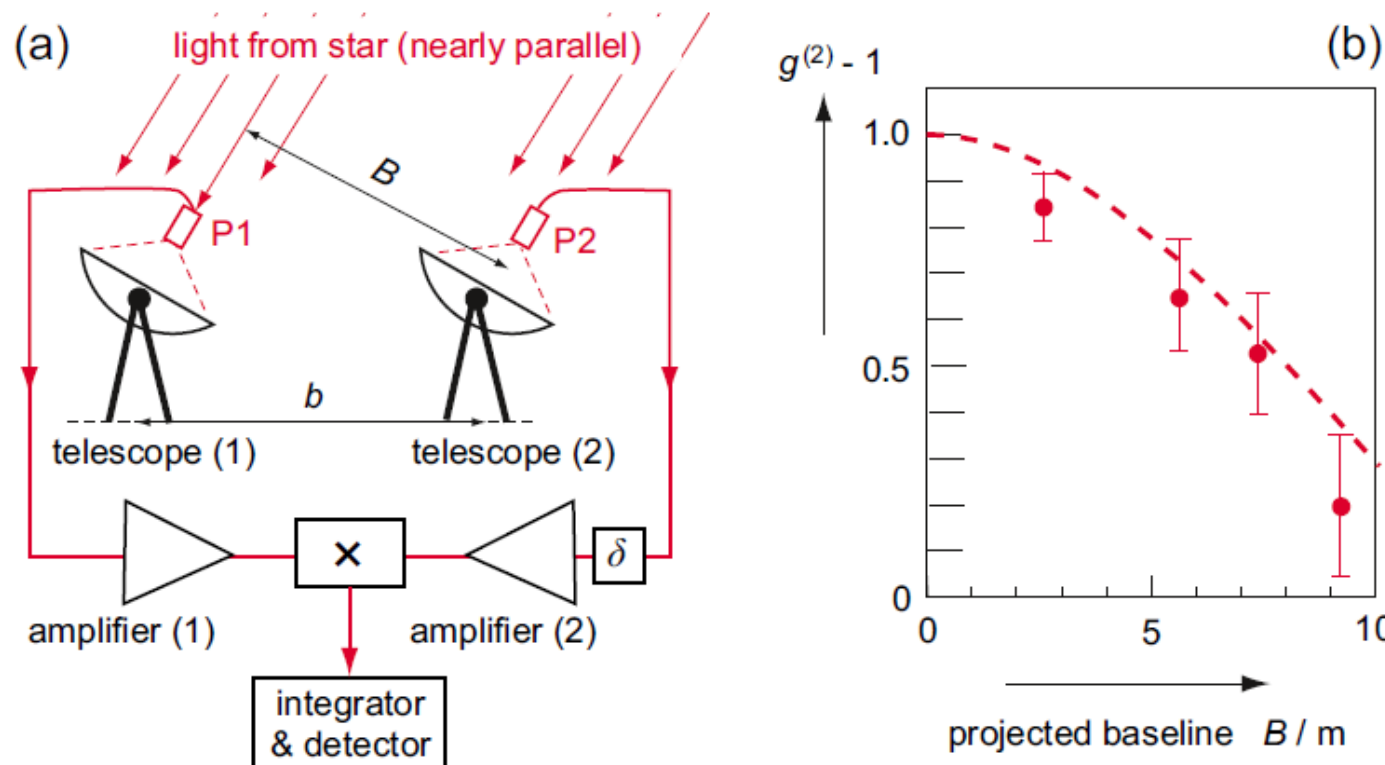
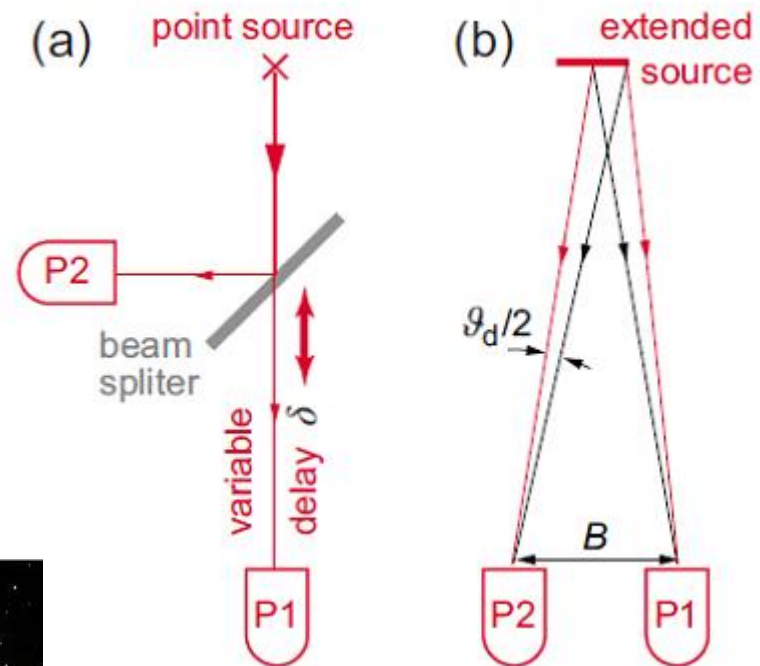
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3. Isospin effect HBT correlations in Heavy Ion Reactions (5)
4. Summary (2')



Hanbury Brown-Twiss Method

- 1950s, Hanbury Brown and Twiss propose an intensity interferometry to measure the size information of the stellar object.

Hanbury Brown and Twiss, *Nature* 177, 27 (1956)



- HBT is invented to measure the space information

Hanbury Brown and Twiss, *Nature* 178, 1046 (1956)

HBT correlation

Unlike the amplitude interference! HBT correlation is intensity interferometry, referring the correlation of the two intensities. It is the second order interference.

In a classic picture: the spherical waves emitted from a and b are :

$$\alpha e^{ik|\vec{r}-\vec{r}_a|+i\varphi_a}/|\vec{r}-\vec{r}_a| \quad \beta e^{ik|\vec{r}-\vec{r}_b|+i\varphi_b}/|\vec{r}-\vec{r}_b|$$

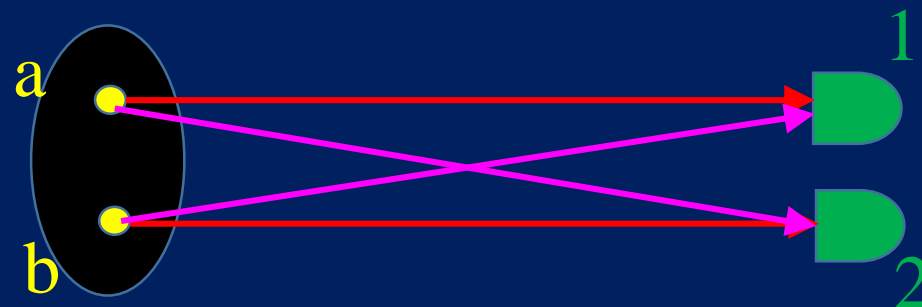
The amplitude of the signal seen in Detector 1:

$$A_1 = \frac{1}{L} [\alpha e^{ikr_{1a}+i\varphi_a} + \beta e^{ikr_{1b}+i\varphi_b}]$$

Do the average over time, one has: $\langle e^{i(\varphi_b-\varphi_a)} \rangle = 0$

One get the light intensity is:

$$\langle I_1 \rangle = \langle I_2 \rangle = \frac{1}{L^2} [\alpha^2 + \beta^2]$$



HBT correlation

Finally, One arrive at : $\langle I_1 I_2 \rangle = \frac{1}{L^4} \left[L^4 \langle I_1 \rangle \langle I_2 \rangle + 2\alpha^2 \beta^2 \cos \left((\vec{k}_2 - \vec{k}_1) \cdot \vec{R} \right) \right]$

The Correlation function is defined as :

$$C(\vec{d}, k_1, k_2) = \frac{\langle I_1 I_2 \rangle}{\langle I_1 \rangle \langle I_2 \rangle} = 1 + 2 \frac{\langle \alpha^2 \rangle \langle \beta^2 \rangle}{(\alpha^2 + \beta^2)^2} \cos \left((\vec{k}_2 - \vec{k}_1) \cdot \vec{R} \right)$$

Approximately, it reads :

$$C(\vec{d}, k_1, k_2) \approx 1 + \frac{1}{2} \cos \left((\vec{k}_2 - \vec{k}_1) \cdot \vec{R} \right)$$

Considering a source with density distribution $\rho(r)$, the correlation function is written as

$$C(\vec{d}, k_1, k_2) - 1 = \left| \int \rho(r) e^{i(\vec{k}_1 - \vec{k}_2) \cdot \vec{r}} d^3 r \right|^2$$

Obviously, C is as a function of d via Δk , d is the base line of the two detectors.

$C(\vec{d}, k_1, k_2)$ is the Fourier transformation of the density distribution of the source.

Application of HBT in nuclear physics

- 1960s, Goldhaber Analyzed the $\pi\pi$ correlation in $\bar{p}p$ annihilation
- 1977, S. Koonin extended the HBT to pp correlation in heavy ion reactions

Distribution of proton in the fireball

$$\frac{1}{\sigma} \frac{d\sigma}{d\mathbf{p}_1 d\mathbf{p}_2} = \int_{-\infty}^{\infty} dt_1 dt_2 \int d\mathbf{r}_1 d\mathbf{r}_2 D(\mathbf{r}_1 t_1, \mathbf{p}) D(\mathbf{r}_2 t_2, \mathbf{p}) \times \left\{ \frac{1}{4} |\Psi_{\mathbf{p}_1 \mathbf{p}_2}(\mathbf{r}'_1, \mathbf{r}_2)|^2 + \frac{3}{4} |\Psi_{\mathbf{p}_1 \mathbf{p}_2}(\mathbf{r}'_1, \mathbf{r}_2)|^2 \right\}. \quad (1)$$

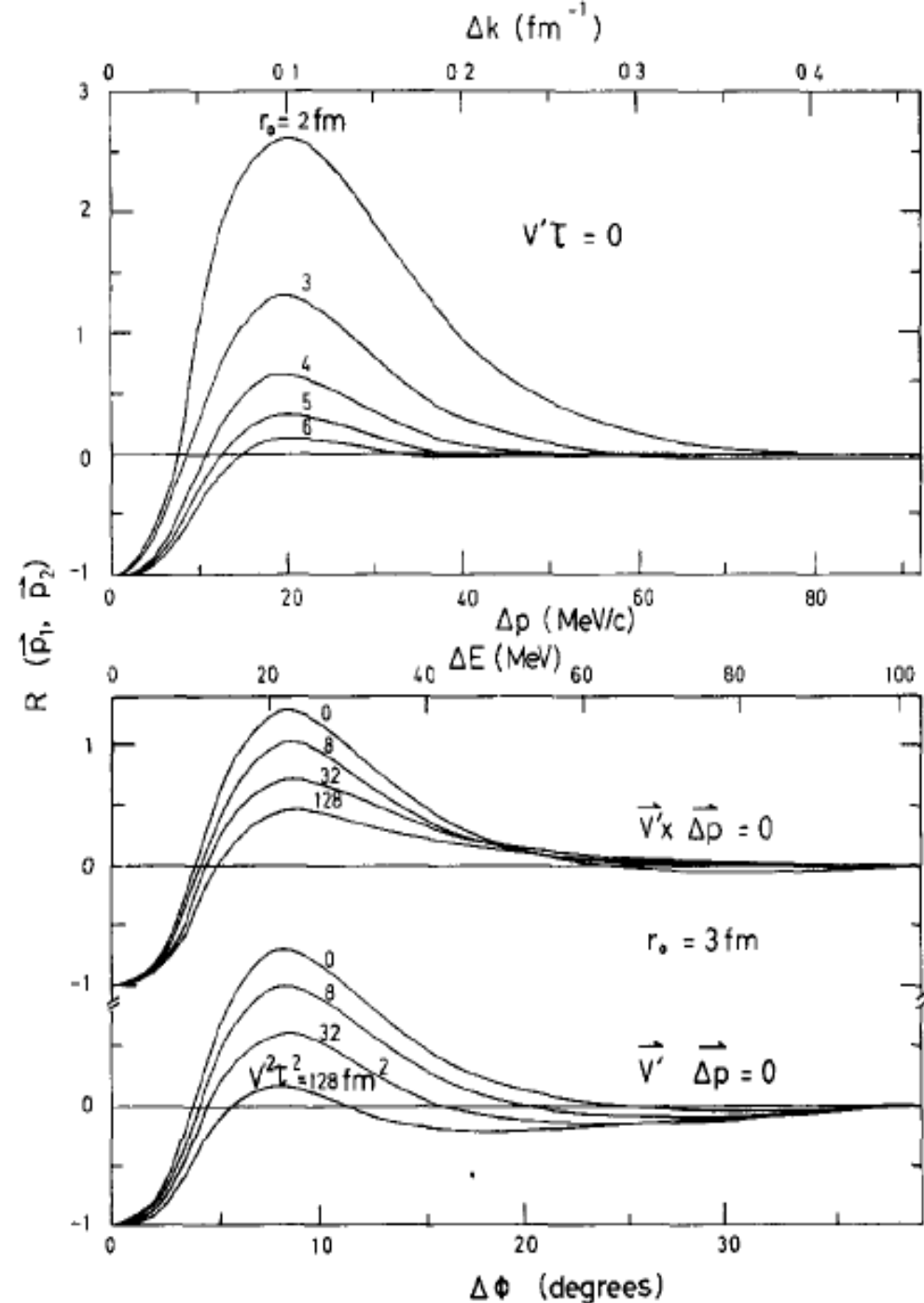
Plane wave multiplying the pp relative motion wave function.

$$D(\mathbf{r}t, \mathbf{p}) = \frac{1}{\sigma} \frac{d\sigma}{d\mathbf{p}} \left(\frac{1}{\pi^{3/2} r_0^3} e^{-(\mathbf{r} - \mathbf{V}_0 t)^2 / r_0^2} \right) \left(\frac{1}{\pi^{1/2} \tau} e^{-t^2 / \tau^2} \right) \quad (2)$$

PROTON PICTURES OF HIGH-ENERGY NUCLEAR COLLISIONS

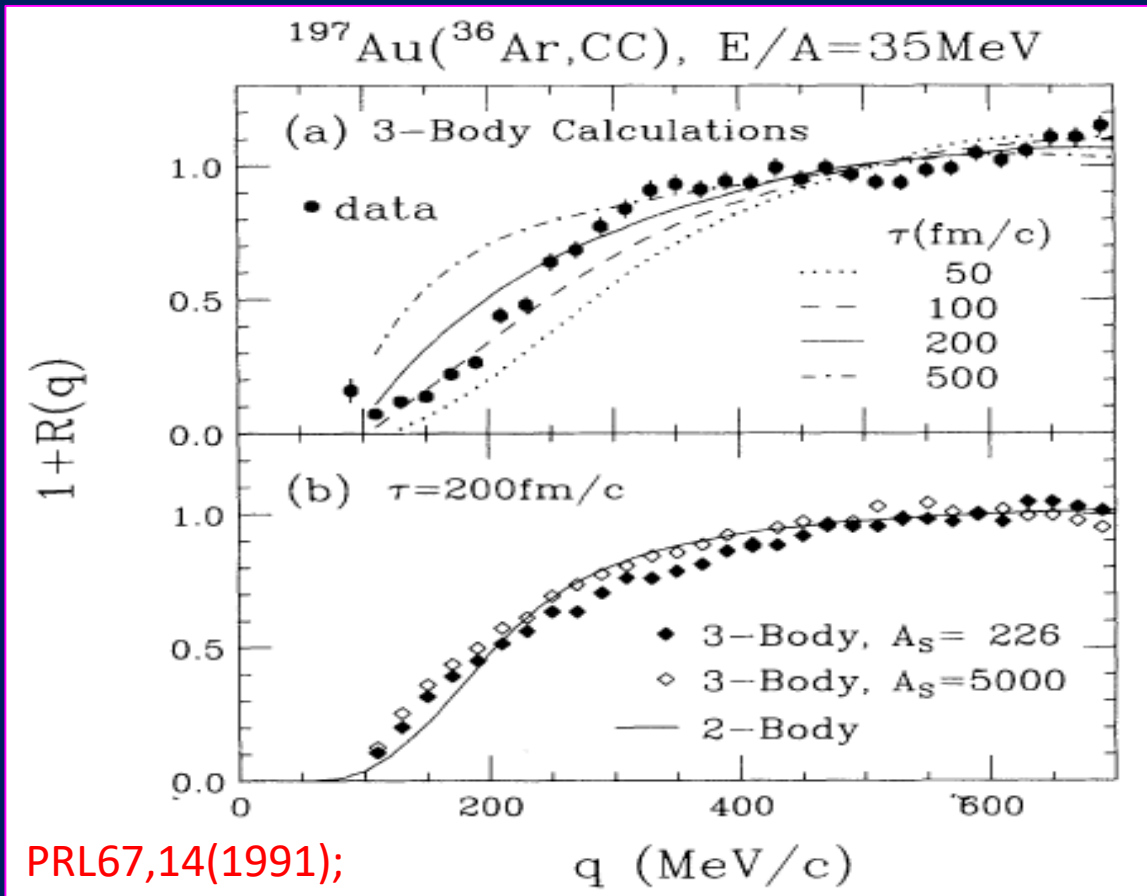
Steven E. KOONIN¹ **PLB70,43(1977)**

The Niels Borh Institute, Copenhagen, Denmark

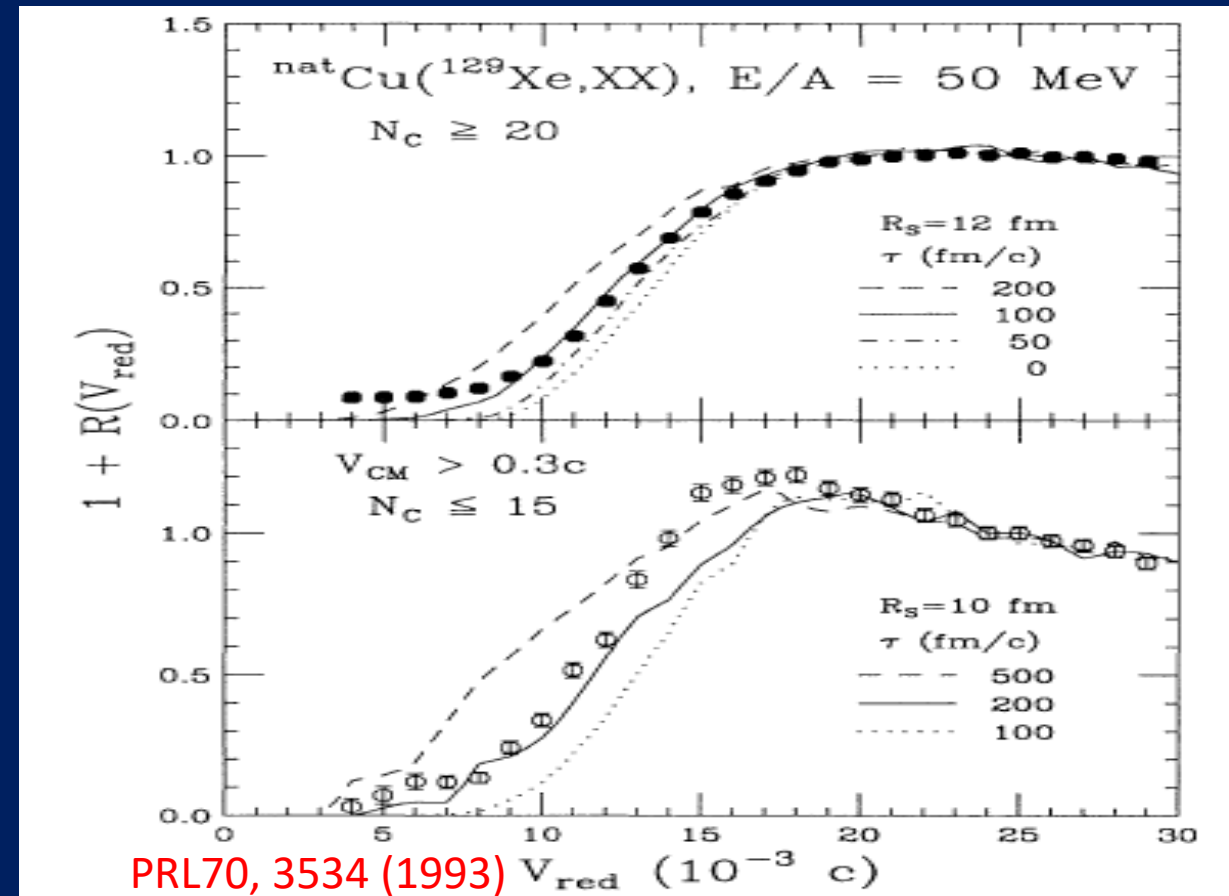


HBT extensively used in HIC since 1990s

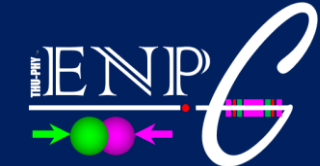
PLB70,43(1977), PRL67,14(1991);
 PRC51,1280(1995); PRC,69,031605R(2004);
 NPA620,214(1997); PRL 77,4508(1997) ; PRL70,
 3534 (1993).....



Y. D. Kim , IMF correlation function in 35 MeV/u Ar+Au ,
 IMF emission time scale: 100-200 fm/c.



D. Bowman , 50 MeV/u Xe+Cu, IMF correlation function at different centrality, time scale confirmed at 100 fm/c.

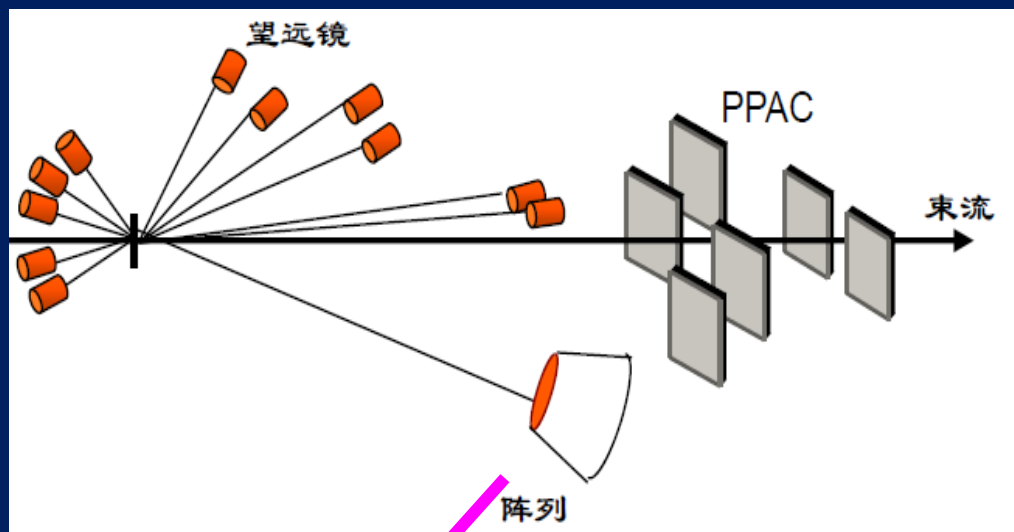


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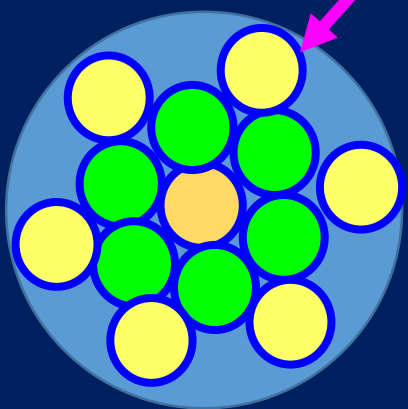
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4. Summary (2')



Experimental measurement of Isospin effect on IMF HBT correlation

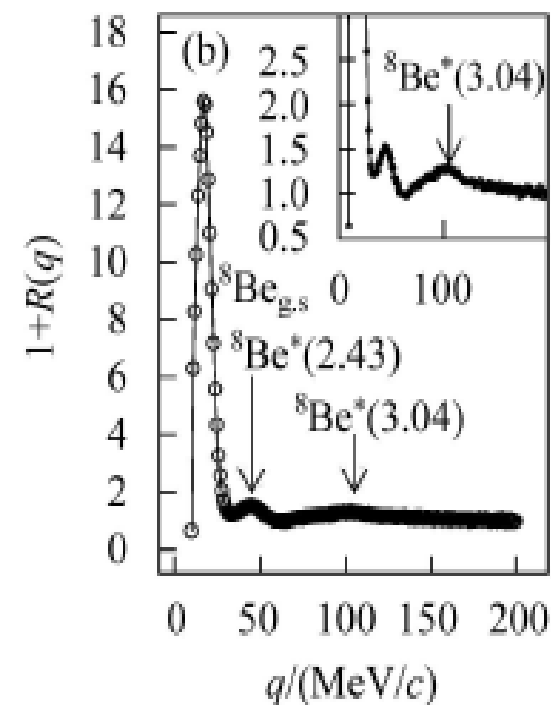
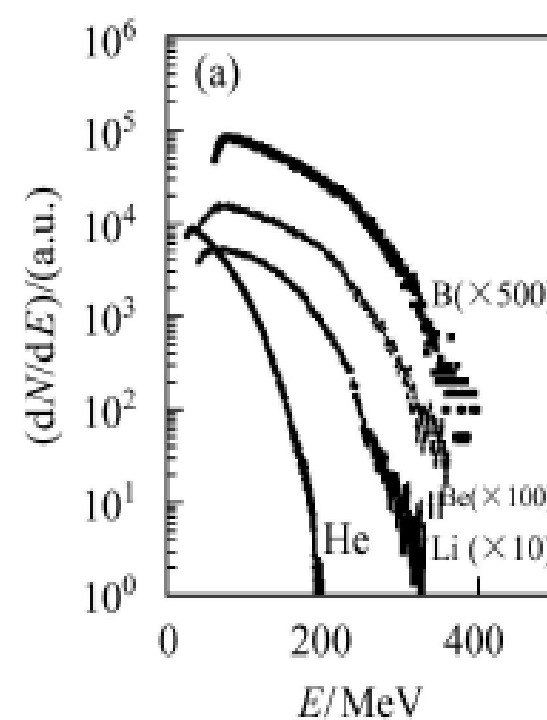
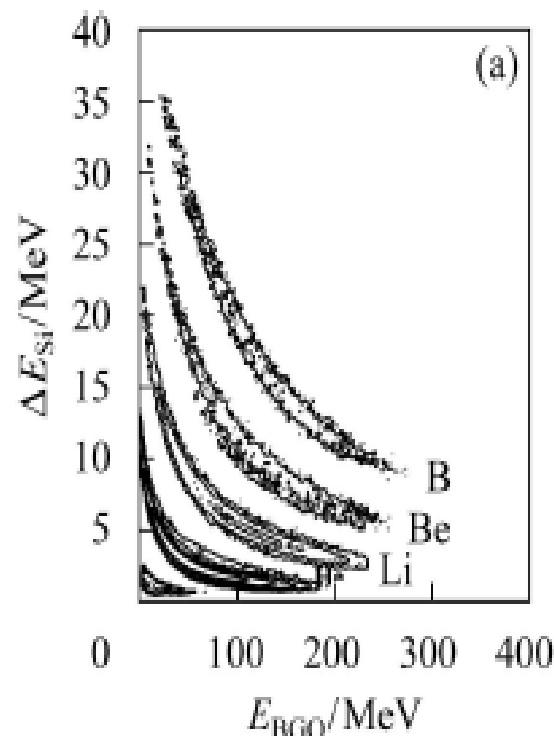


- Reaction: $35\text{MeV } ^{36}\text{Ar} + ^{112,124}\text{Sn}$
- Isospin effect on IMF HBT correlation

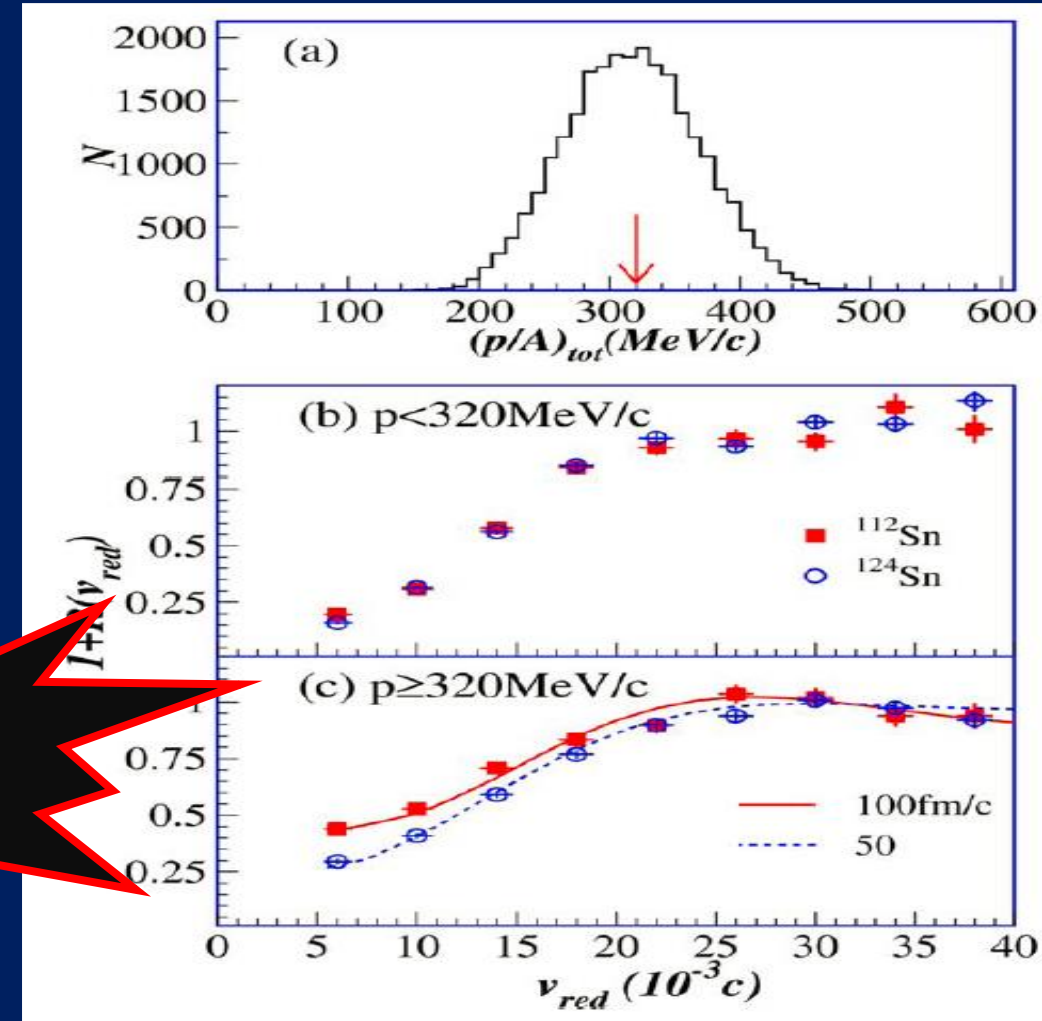
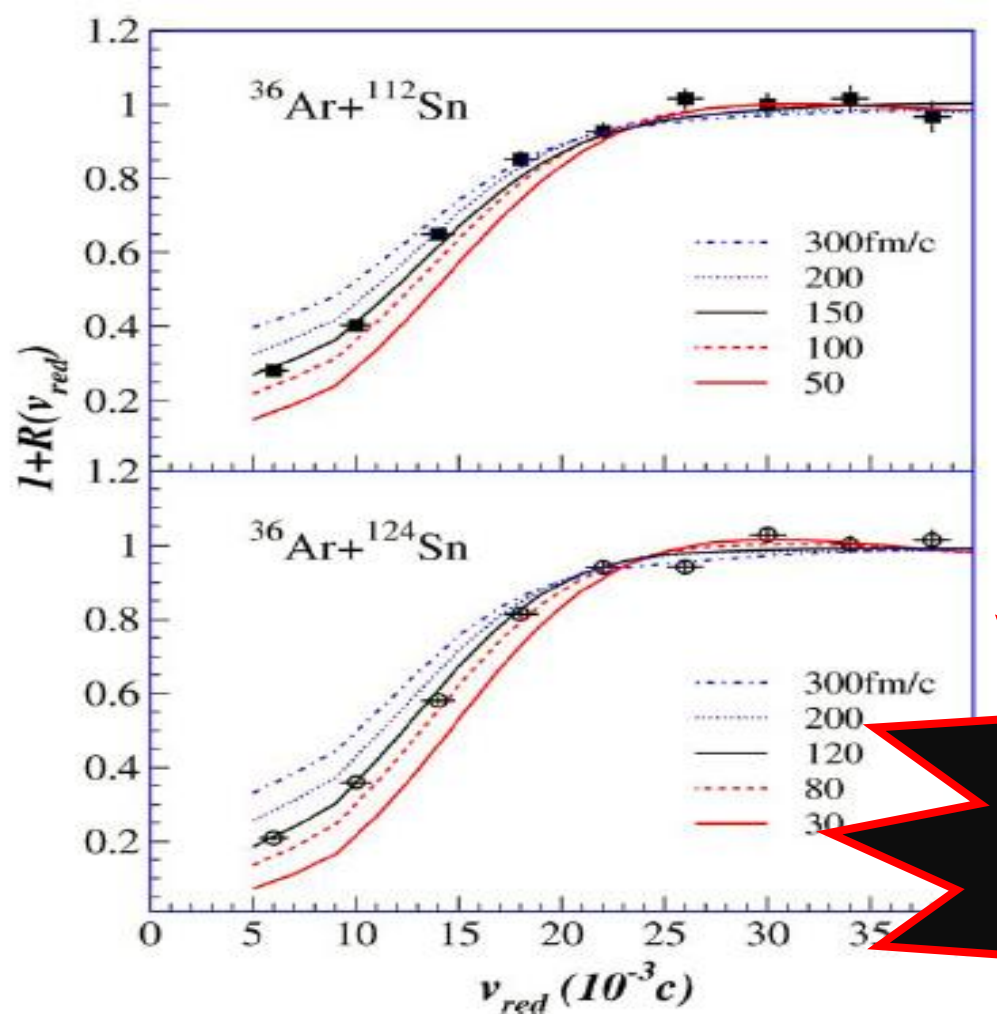


Hodoscope : 13-unit closely packed Si-BGO array

Hit position Resolution $\sim 1\text{cm}$



Experimental measurement of isospin dependent HBT correlation of IMF



~50 fm/c time resolution achievable

ZGX, R. J. Hu, H. Y. Wu et al., **PLB 639**,436 (2006) ;

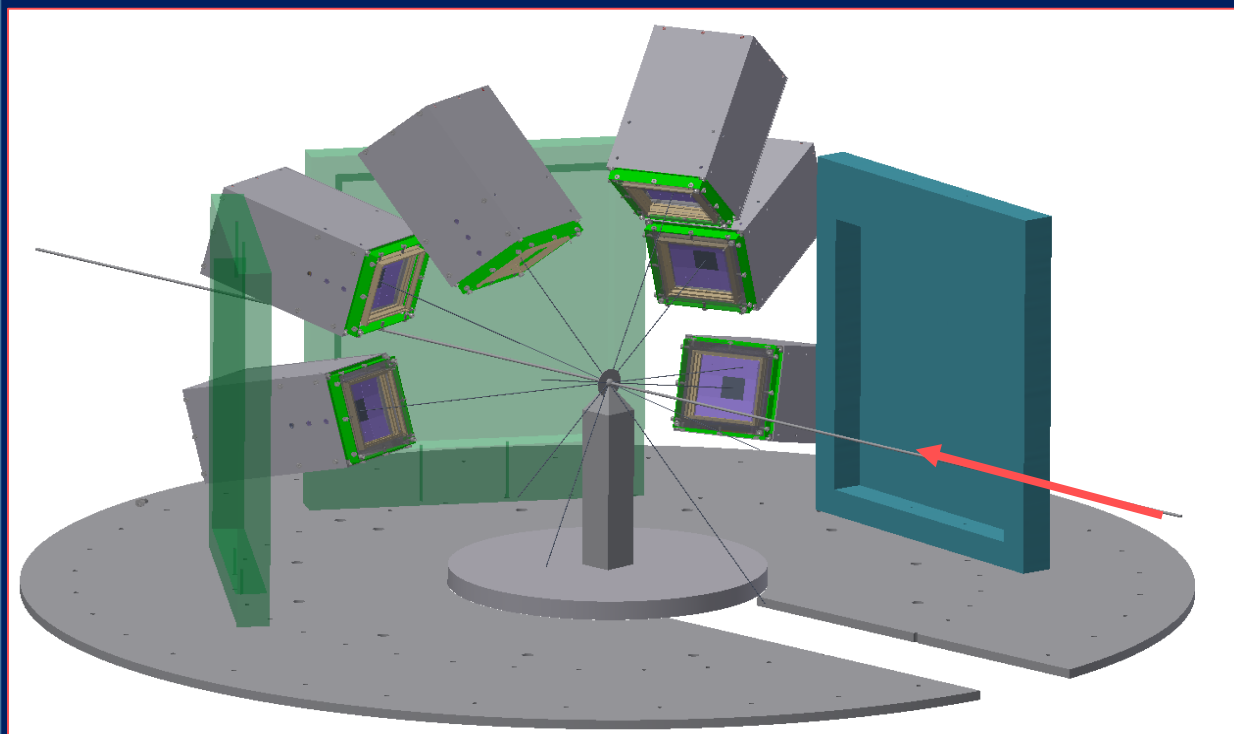
R. J. Hu, ZGX et al., **HEPNP 31**, 350 (2007)

- Stronger Coulomb anti-correlation is observed in $\text{Ar} + ^{124}\text{Sn}$, this difference arises from the isospin difference of the two system.

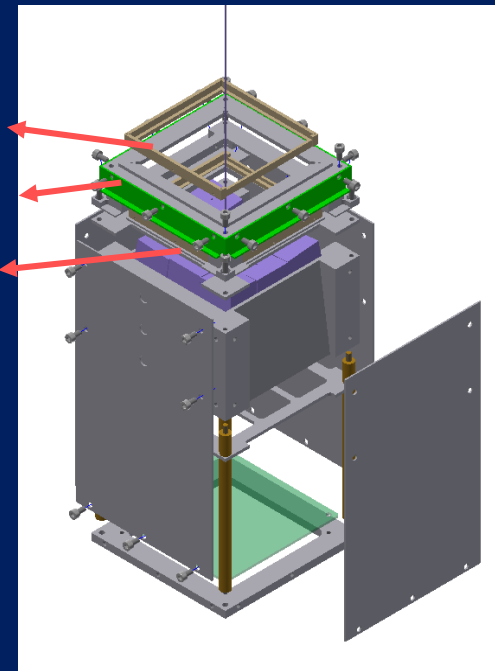
HIRA^{TU} : A future array for Isospin chronology in HIC

- **H**eavy **I**on **R**esearch **A**rray at **T**singhua **U**niversity (HIRA^{TU})

Build HIRA-type arrays + PPACs



SSD - $\Delta E1$
SSD - $\Delta E2$
CsI - E

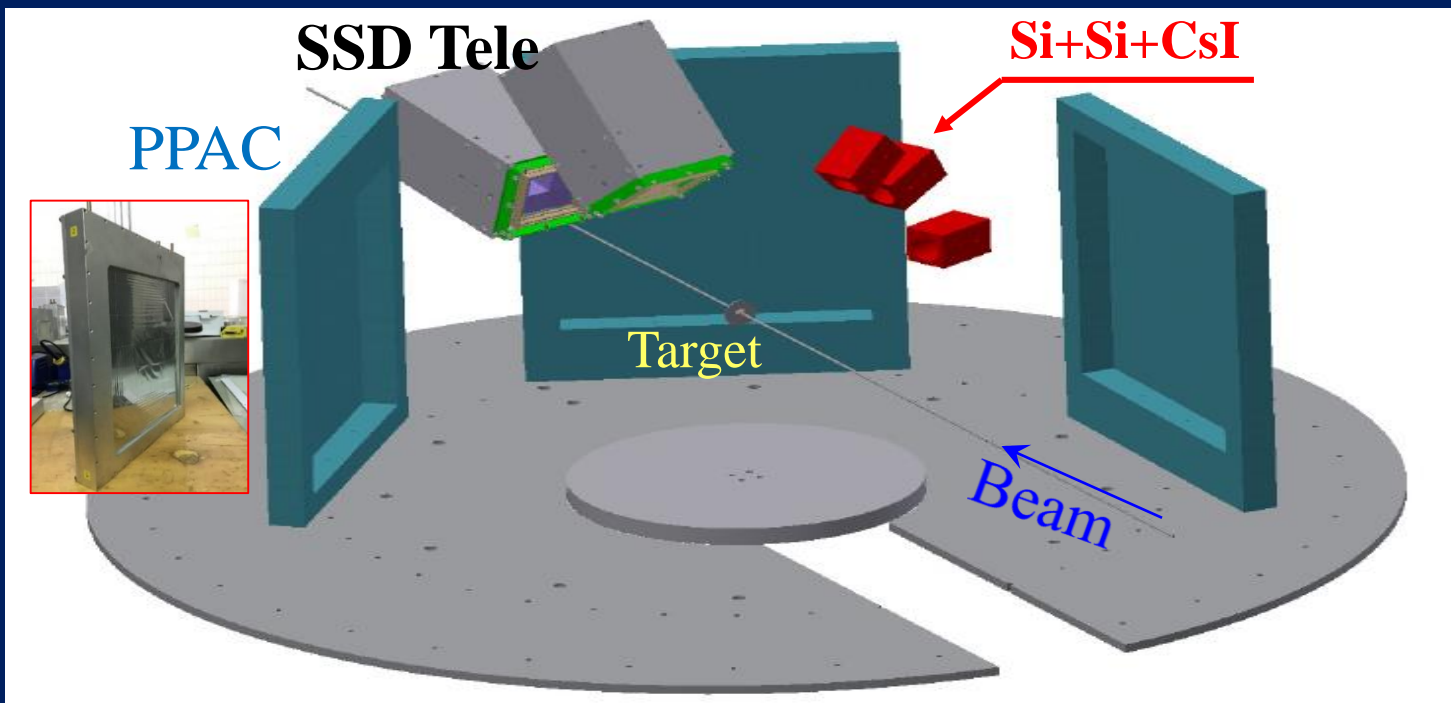
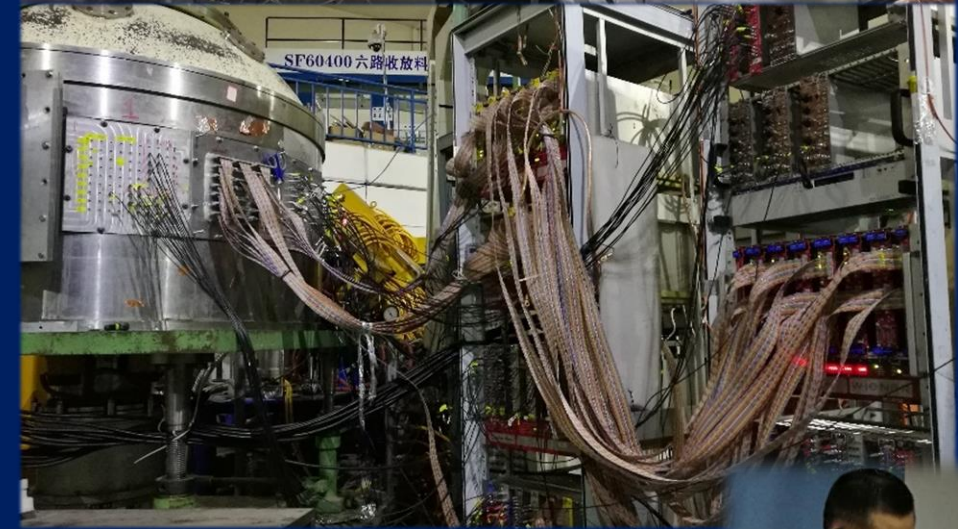
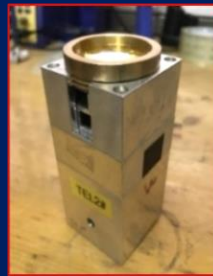
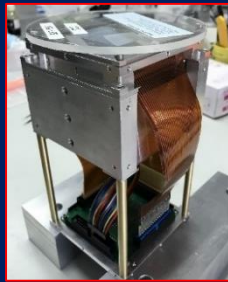


Hit position Resolution $\sim 2\text{mm}$



HIRA^{TU}: Phase-1 Experiment

- 3 PPAC (250 mm × 350 mm) ✓
- 2 SSD-telescopes (65 μm + 1500 μm + CsI) ✓
- 3 Si(Au)-CsI Telescopes (50 μm + 300 μm + CsI) ✓



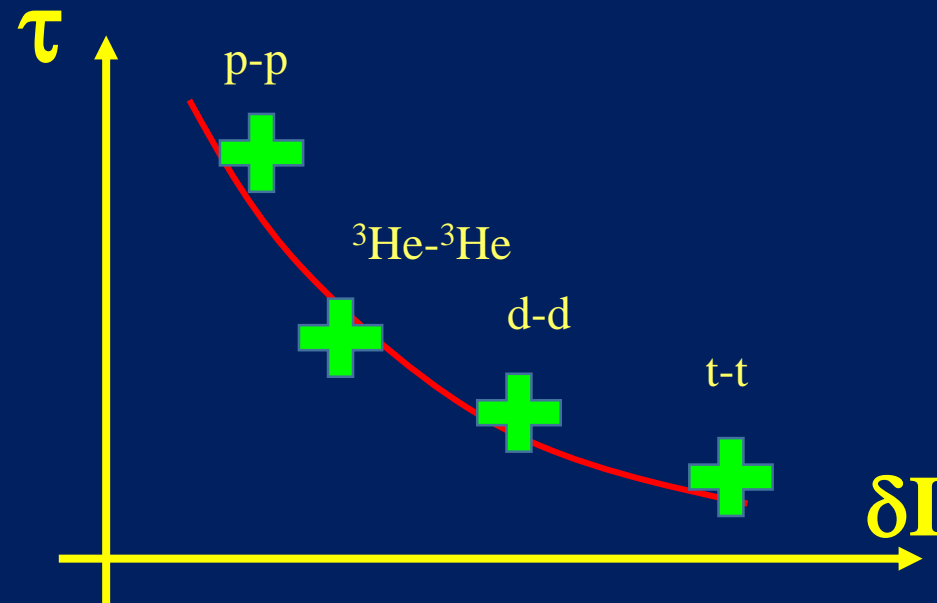
Beam time: 6-13 Feb., 2018;
Reaction: Ar+Au at 30 MeV/u;
Experiment at: RIBLL HIRFL



HIRA^{TU}: A future array for Isospin chronology in HIC

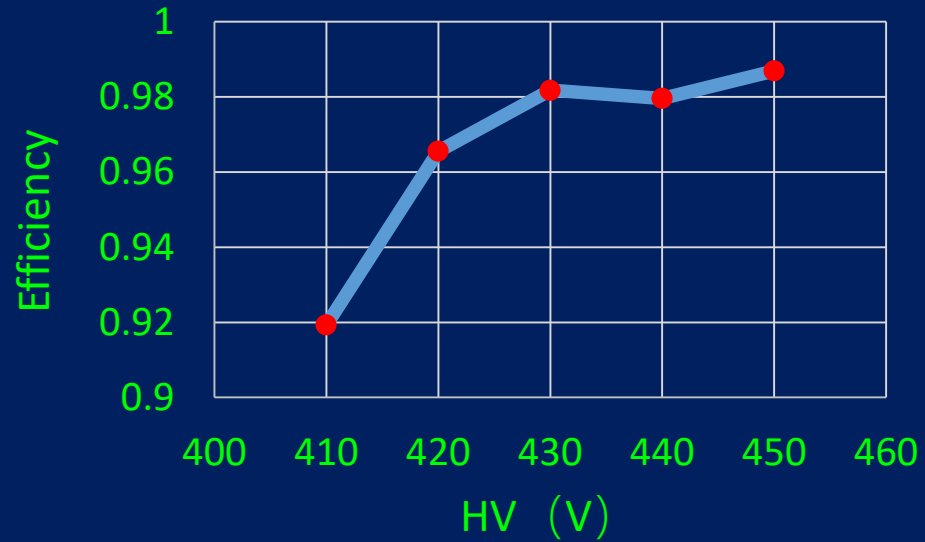
- Phase I Experiment: Isospin dependent of the particle emission time scale with HBT method.

First Physical goal: Isospin-resolved HBT

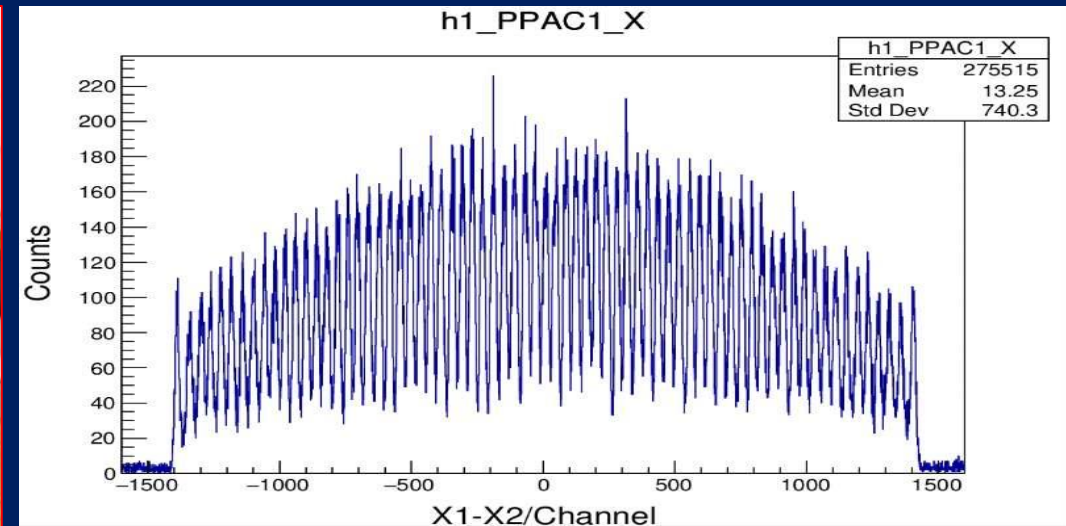
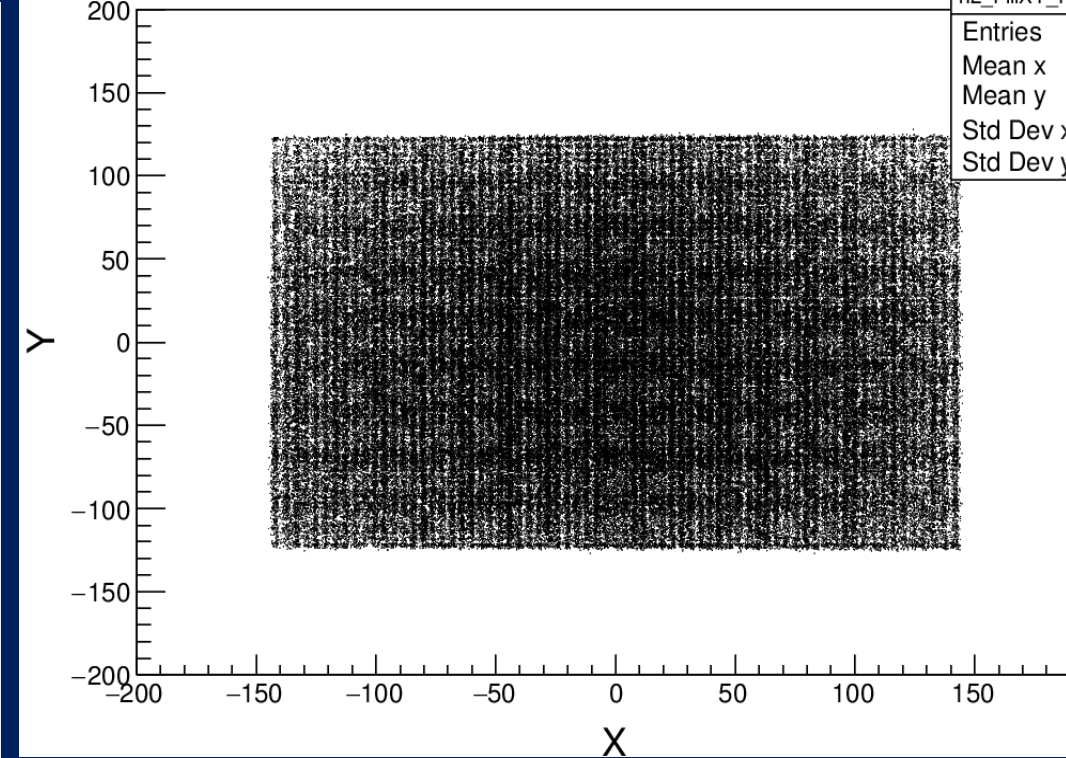
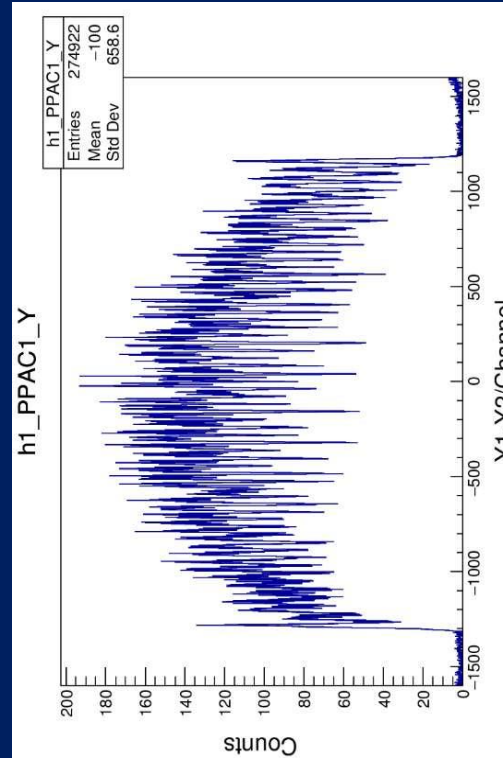
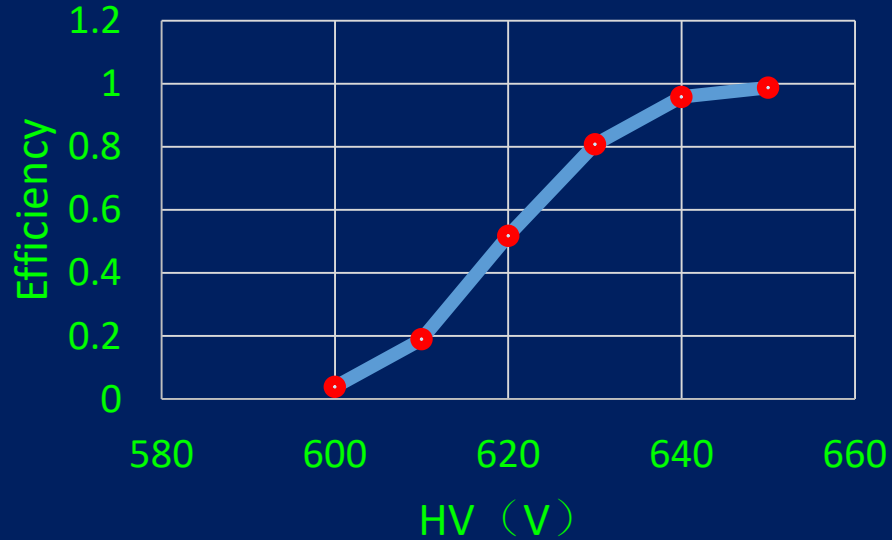


Performance of PPACs in beam experiment (30 MeV/u Ar+Au)

Efficiency for F. fragments/ Cf-252

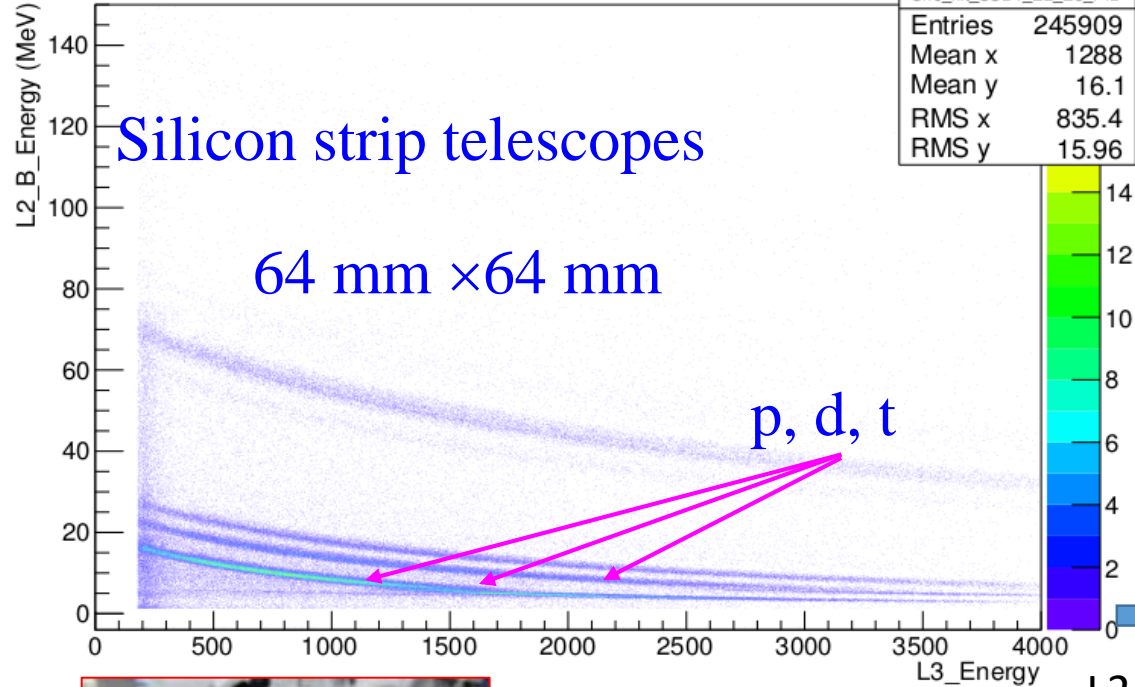


Efficiency for alpha/ Pu-239



one LCP in coincidence with Fission

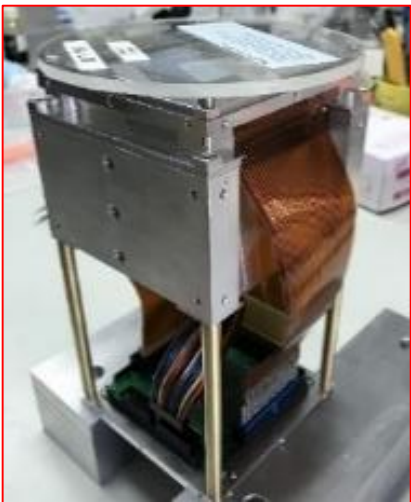
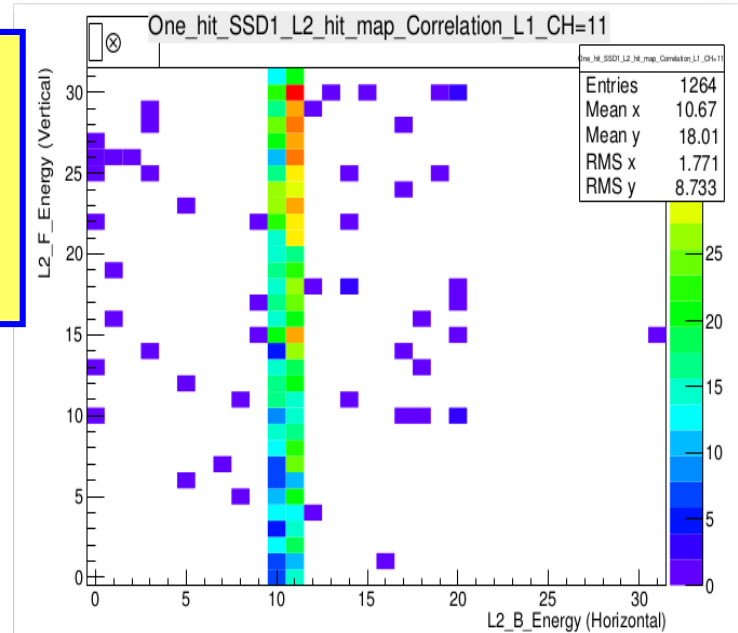
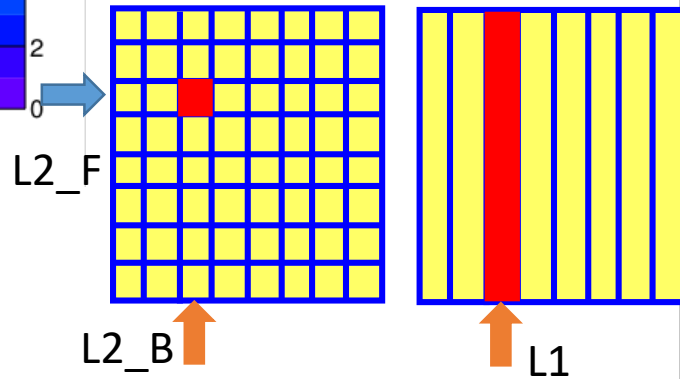
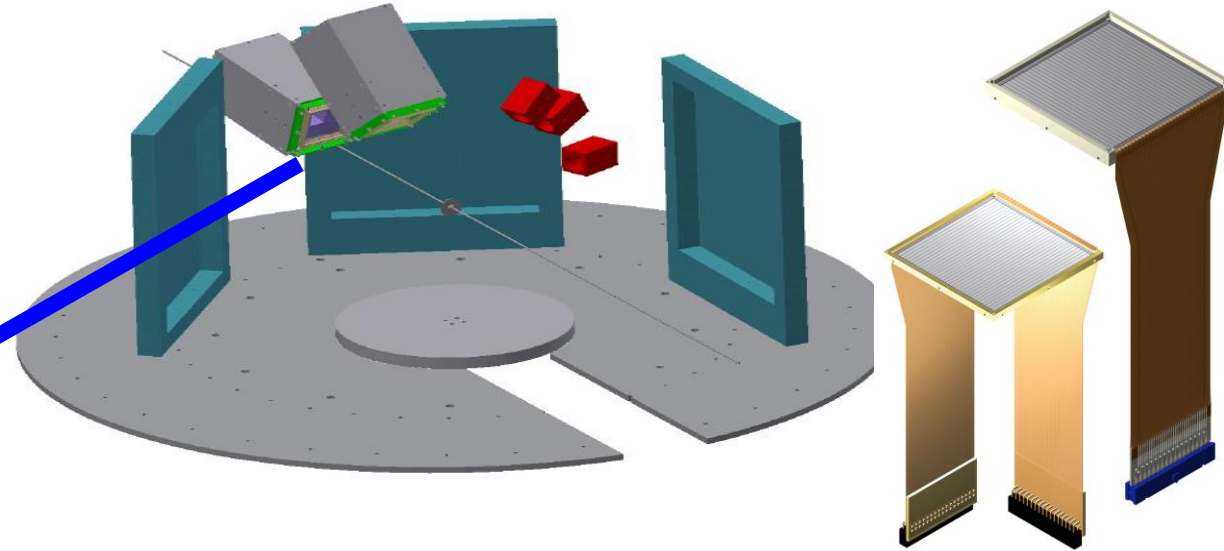
One_hit_SSD1_E2_E3_PID



Silicon strip telescopes

64 mm × 64 mm

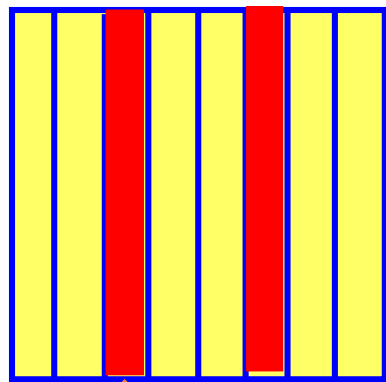
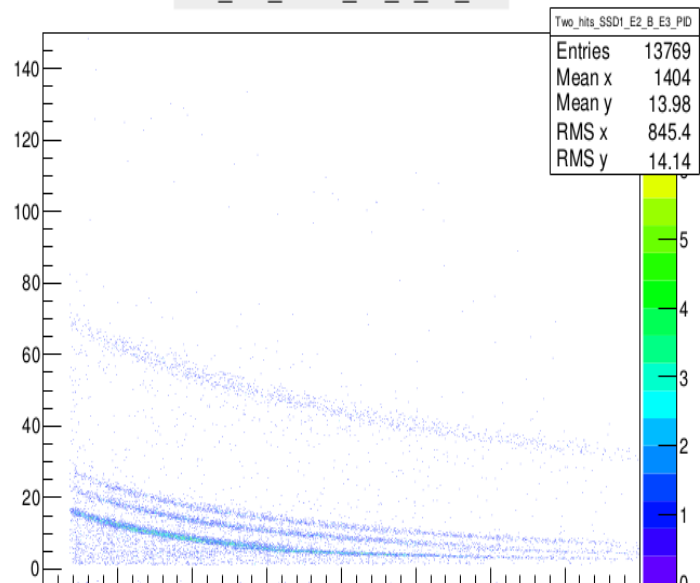
p, d, t



>98% matching efficiency of Layer 1 and Layer 2 of the SSD

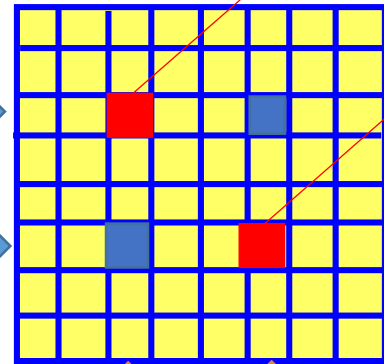
LCP-LCP correlation identified

Two_hits_SSD1_E2_B_E3_PID



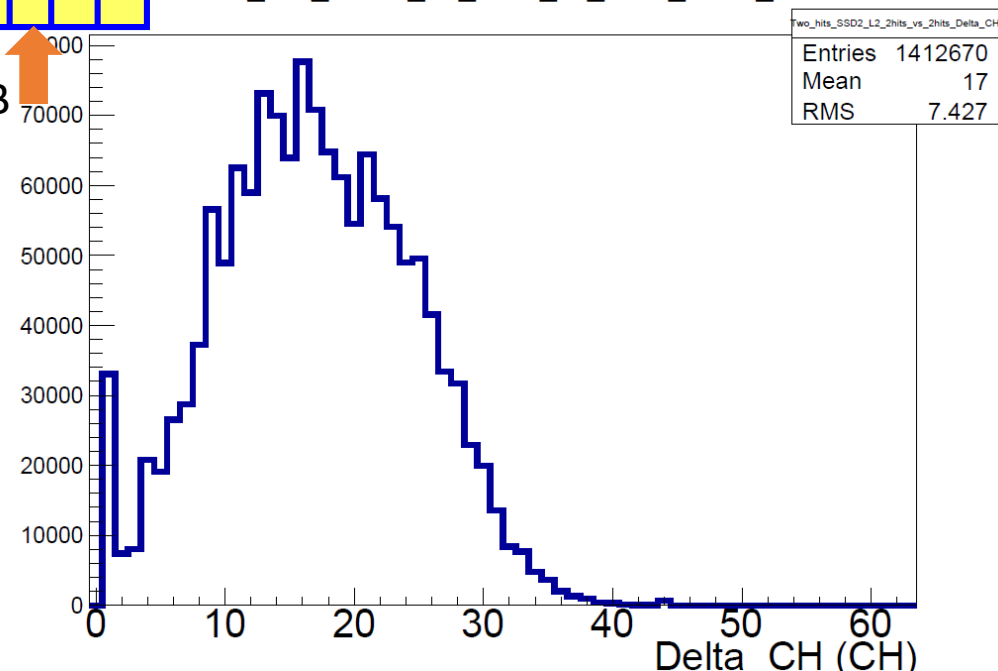
L1

L2_F



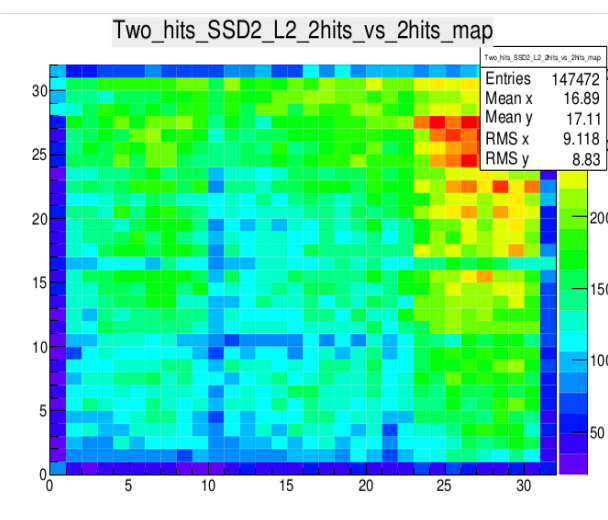
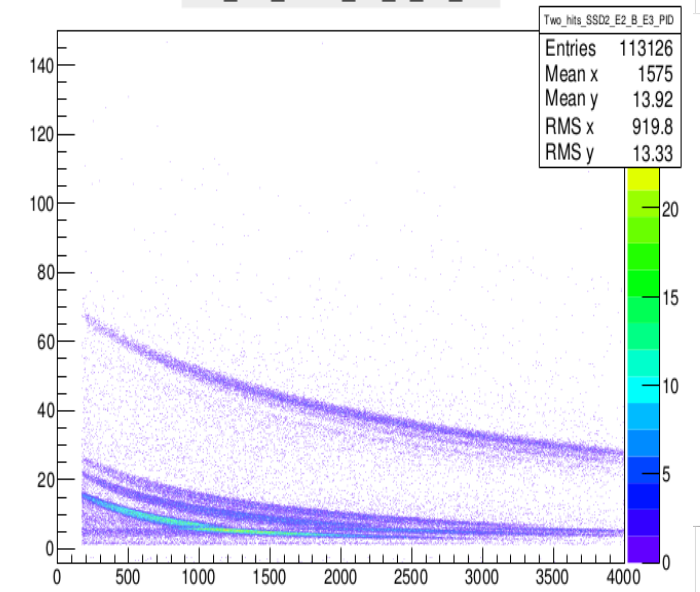
L2_B

Two_hits_SSD2_L2_2hits_vs_2hits_Delta_CH



Distance between two correlated particles

Two_hits_SSD2_E2_B_E3_PID



Physical output of phase 1 exp. is expected in near future!



4. Summary

Wealthy information of the transport of **isospin** DOF and $E_{\text{sym}}(\rho)$ is contained in **HIC**.

The isospin-dependent **emission hierarchy** of light charged particles has been observed, showing neutron-rich LCPs are emitted earlier. Wide-range angular distribution of the relative neutron richness of the set a constraint on $E_{\text{sym}}(\rho)$ with $L=33-61$ MeV at $S_0=28.3$ MeV (CL=95%)

HBT method can be used for the quantitative assessment of the emission time and isospin dependent hierarchy of particle emission. HBT correlation function dependence on the system N/Z has been observed. With improving the detector performance, the Isospin **chronology** studies using HBT method is expected with **HIRA^{TU}**.

Thank you!

