

# Influence of the N-N tensor force on the magicity of the $^{54}\text{Ca}$ nucleus

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# Outline of talk

- 1. Experimental facts in the Ca chain
- 2. The Skyrme EDF for ground and excited states
- 3. Single-particle spectra and subshell closures
- 4. Low-lying 2+ states
- 5. Conclusion

E. Yüksel, NVG, E. Khan, K. Bozkurt,  
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# LETTER

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## Evidence for a new nuclear ‘magic number’ from the level structure of $^{54}\text{Ca}$

D. Steffenbeck<sup>1</sup>, S. Takeuchi<sup>2</sup>, N. Aoi<sup>3</sup>, P. Doornenbal<sup>2</sup>, M. Matsushita<sup>1</sup>, H. Wang<sup>2</sup>, H. Baba<sup>2</sup>, N. Fukuda<sup>2</sup>, S. Go<sup>1</sup>, M. Honma<sup>4</sup>, J. Lee<sup>2</sup>, K. Matsui<sup>5</sup>, S. Michimasa<sup>1</sup>, T. Motobayashi<sup>2</sup>, D. Nishimura<sup>6</sup>, T. Otsuka<sup>1,5</sup>, H. Sakurai<sup>2,5</sup>, Y. Shiga<sup>7</sup>, P.-A. Söderström<sup>2</sup>, T. Sumikama<sup>8</sup>, H. Suzuki<sup>2</sup>, R. Taniuchi<sup>5</sup>, Y. Utsuno<sup>9</sup>, J. J. Valiente-Dobón<sup>10</sup> & K. Yoneda<sup>2</sup>

Nature 502, 207 (2013)

- Data from proton knock out reactions
- First 2+ state in  $^{54}\text{Ca}$  found at about 2 MeV: indication that  $2\text{p}1/2$  (neutron) is **partly** occupied while  $1\text{f}5/2$  (neutron) is **partly** empty.

How much « partly »?

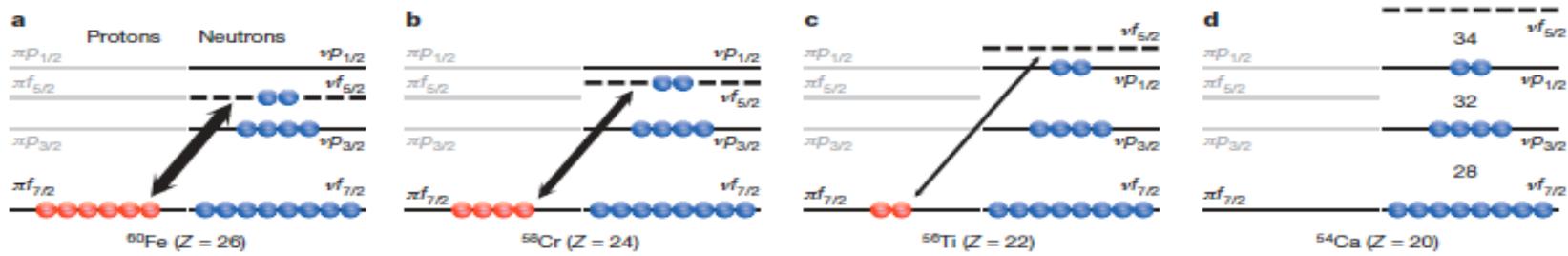
We show the importance of the effective tensor interaction in answering this question

# The N=34 isotones

## « Otsuka's effect »:

RESEARCH LETTER

Figure from Steffenbeck et al.



The interaction induced by a tensor force between a proton in a  $(l, j=l+1/2)$  state and a neutron in a  $(l, j=l-1/2)$  state is attractive

T.Otsuka, T.Suzuki, R. Fujimoto, H.Grawe, Y.Akaishi,  
Phys. Rev. Lett. 95, 232502 (2005)

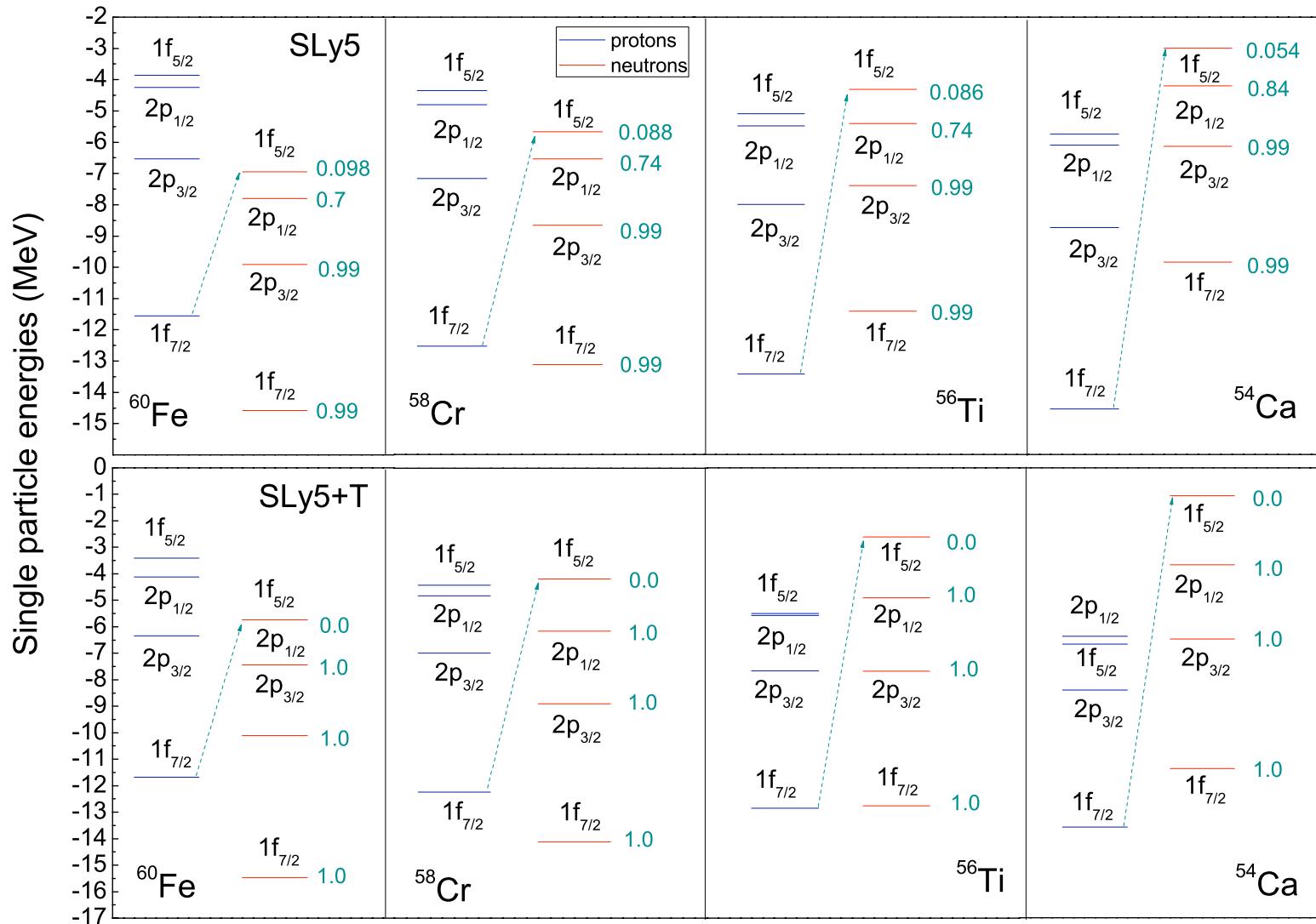
# Theoretical predictions of single-particle spectra

- **Model:** Hartree-Fock-Bogoliubov mean field
- **Inputs:** Skyrme-type Energy-Density Functionals
- **Focus:** effects of the tensor component of the EDF on the quasi-particle energies and occupation numbers

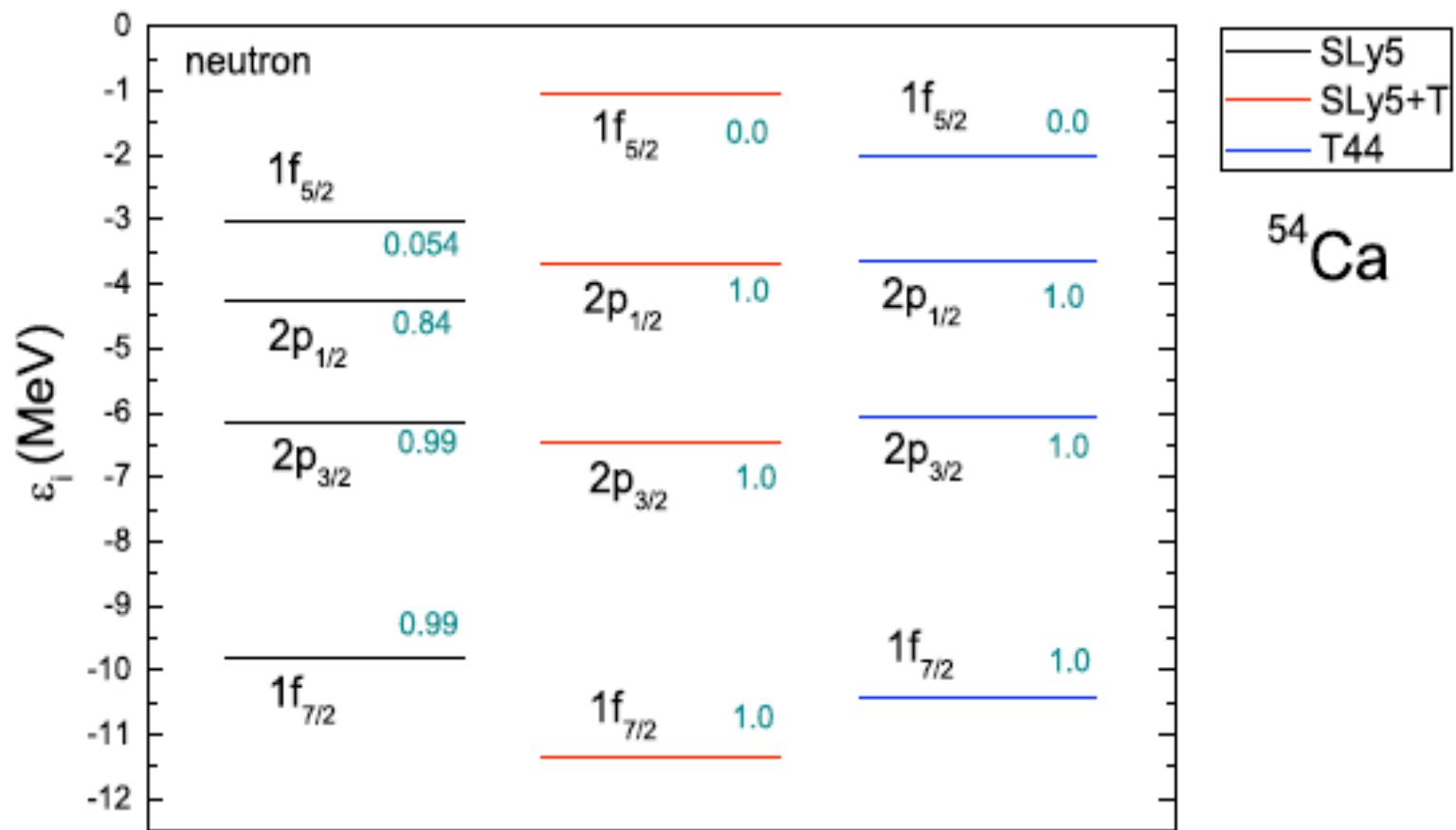
# Models used

- Recent work:
- M. Grasso, Phys. Rev. C 89, 034316 (2014)
- found magicity for 52,54Ca if described by Skyrme Hartree-Fock, using SLy5+Tensor
- This work:
- Skyrme Hartree-Fock-Bogoliubov for ground states
- QRPA for excited states
- SLy5, SLY5+T, T44 for interactions:
- SLY5+T: G.Colò et al, Phys.Lett.B 646,227(2007)
- T44: T.Lesinski et al, Phys. Rev. C 76, 014312 (2007)
- Contact, density-dependent pairing force adjusted on 2n separation energies and 2+ energies of 42-46Ca chain.

# Effects of tensor force on s.p. spectra and occupation probabilities in N=34 isotones



# Effect of tensor force on 2p1/2 closure in $^{54}\text{Ca}$

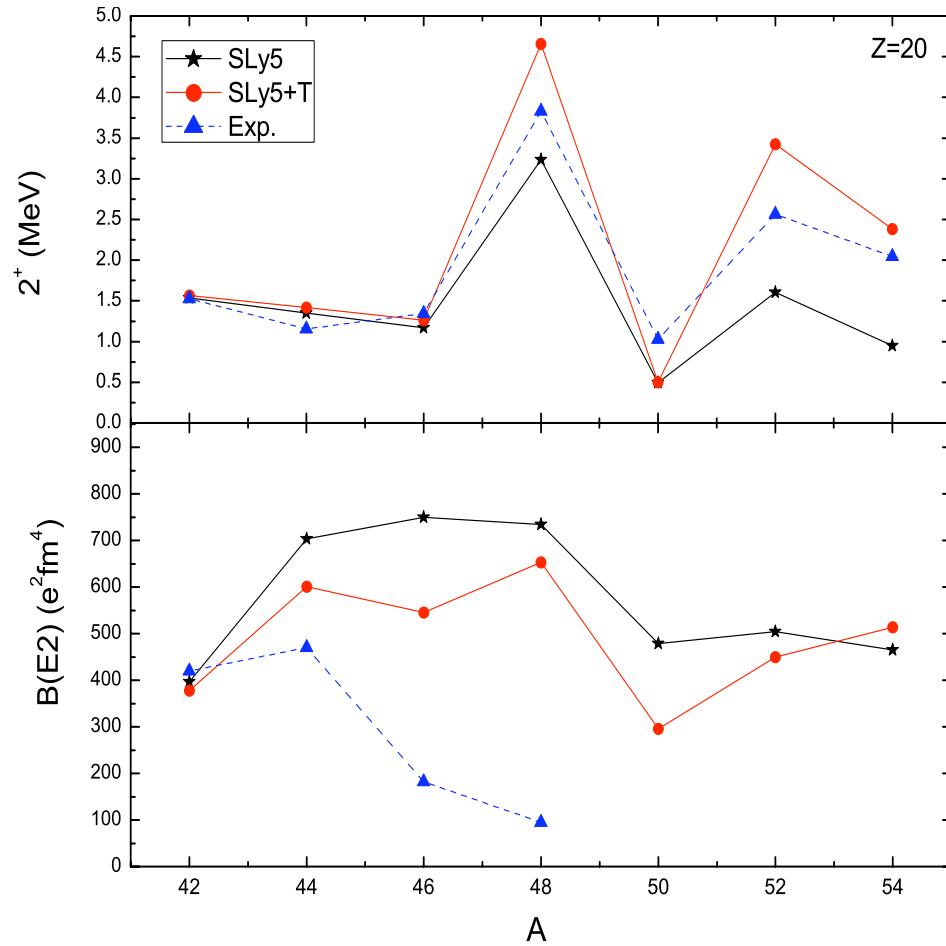


Model: HFB with Skyrme-type EDF

# First 2+ energies and B(E2) values

Exp.:

- S. Raman et al, At. Data & Nucl. Data Tables 78, 1128 (2001)
- D. Steffenbeck et al, Nature 502, 207 (2013)

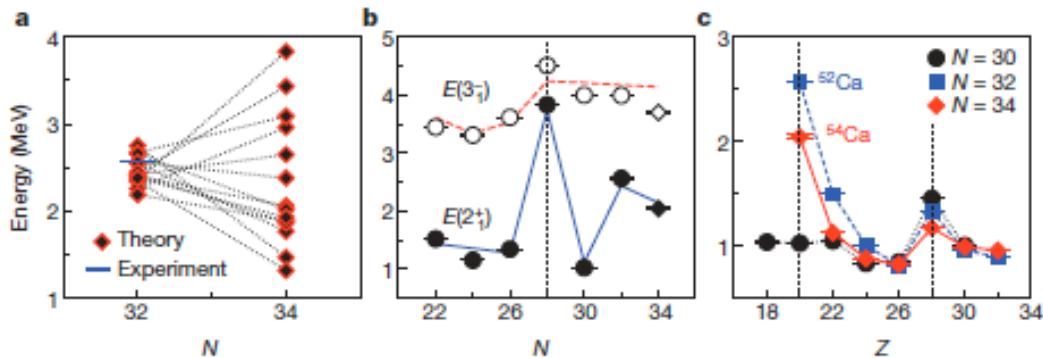


- General remarks about the low)lying J=2+ predictions:
- 2+ energies reasonably well described. The tensor interaction helps.
- Measured B(E2) values very small in 46,48Ca. The tensor interaction does not lead to such small values. Difficult to explain within QRPA.
- No experimental information on B(E2) in 50,52,54Ca.

# Summary

- -The 4 N=34 isotones: 60Fe, 58Cr, 56Ti, 54Ca are explored in a HFB-QRPA model
- The tensor component of the interaction determines the magic character of 54Ca (larger  $2p_{1/2}$ - $1f_{5/2}$  neutron gap, occupation numbers 1 and 0)
- It also brings the energy of the first  $2^+$  state in 54Ca close to the measured value.

# **THANK YOU !**



**Figure 2 | Systematics of excited-state energies in even–even Ca isotopes and neighbouring nuclei.** **a**, Theoretical predictions of the energy of the first  $2^+$  state for  $^{52}\text{Ca}$  ( $N = 32$ ) and  $^{54}\text{Ca}$  ( $N = 34$ ) (refs 14–16, 19–24). The solid blue line represents the experimental result for  $^{52}\text{Ca}$  (refs 6, 7). **b**, Energies of the first  $2^+$  (filled symbols) and  $3^-$  (open symbols) levels for even–even  $^{42-54}\text{Ca}$

isotopes. The results of the present study are indicated by diamonds at  $N = 34$ . The solid and dashed lines are shell-model predictions of the first  $2^+$  and  $3^-$  energies, respectively (see text for details). **c**,  $E(2_1^+)$  along the  $N = 30$ , 32 and 34 isotonic chains. The solid and dashed lines are intended to guide the eye. Vertical dotted lines represent the standard magic numbers.