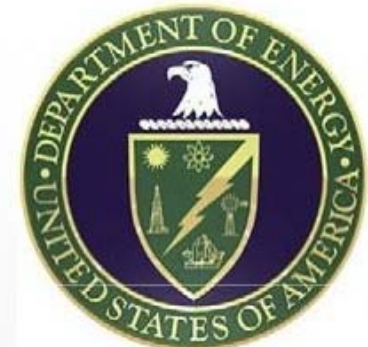


# From Nuclear Matter to Nuclear Reactions

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**Applications of nuclear forces  
in the medium include:**

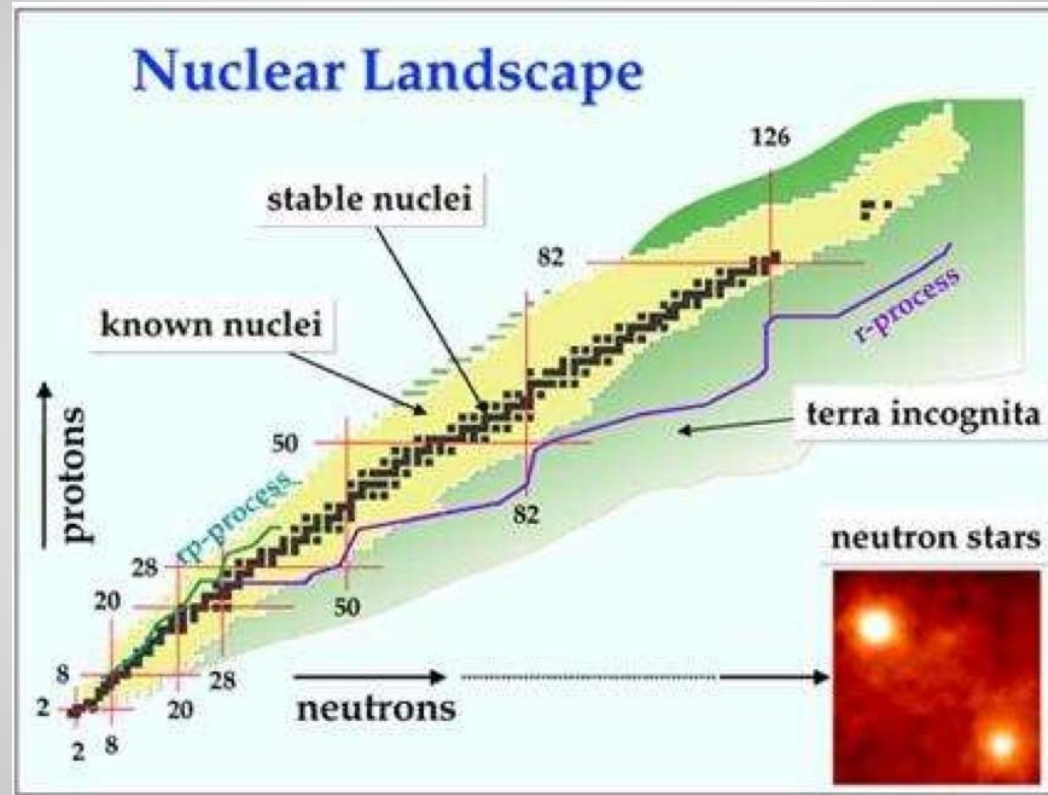
**Nuclear/neutron matter**

**Reactions**

**Structure of nuclei**

After more than 8 decades of nuclear physics, still a lot is unknown about the nuclear chart.

Particularly so for systems with large **isospin** asymmetry

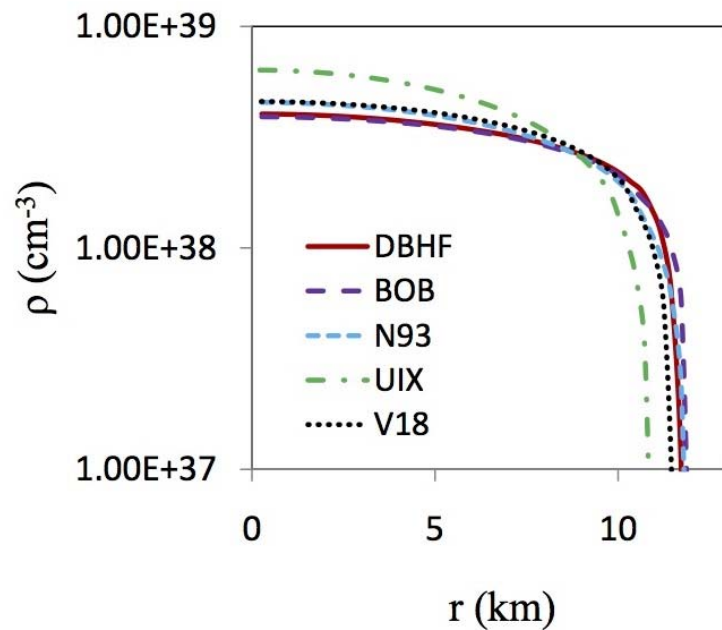


Isospin-asymmetric nuclear matter (IANM) is closely related to neutron-rich nuclei and is a convenient theoretical laboratory.

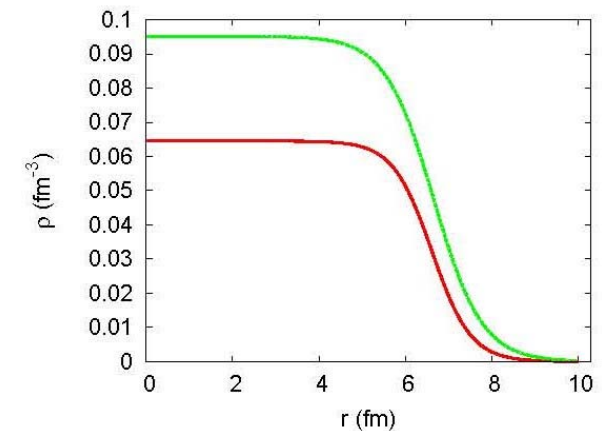
# Studies of IANM are far-reaching:

(Predictions from the same equation of state)

The density profile of a “canonical” mass NS



Neutron and proton densities in  $^{208}\text{Pb}$ .



# The philosophy of modern ab-initio calculations:



The parameters of the two- and many-body forces are constrained by the properties of the two- and few-nucleon systems and **not readjusted** in the many-body system.

Then, one can claim  
**PREDICTIVE POWER**

## How to develop basic interactions?

Our present (incomplete) knowledge of the nuclear force is the results of decades of struggle.

QCD and its symmetries led to the development of chiral effective theories.

**ChPT:** well-defined organizational scheme from which 2BF and many-body forces emerge on the same footing (the chiral expansion).

How good is the rate of convergence of the chiral expansion?

(More on this point later..)

Our traditional approach:

**Two-body sector:** a realistic meson-theoretic potential developed within a relativistic scattering equation (Bonn B).

**For the nuclear matter sector:**

Dirac-Brueckner-Hartree-Fock (DBHF).

Microscopic DB gives validation to the success of RMF theories.

**Microscopic relativistic nuclear physics:**

A paradigm which is important to pursue, reliable over a broad range of momenta/densities (whereas ChPT is a low-momentum expansion).

The symmetry energy has a long history:  
The “mass formula”, Bethe-Weizaecker:

$$\frac{B}{A} = a_V - \frac{a_{sym}(A - 2Z)^2}{A^2} - \frac{a_s}{A^{1/3}} - \frac{a_C Z(Z - 1)}{A^{4/3}} - \frac{\Delta E}{A} .$$

**B/A = Binding energy/nucleon**

**(N - Z)/A = neutron excess or isospin asymmetry**



**NOW LET THE SYSTEM BE INFINITE, AT SOME DENSITY  $\rho$ , AND IGNORE COULOMB INTERACTIONS:**

$$N \rightarrow \rho_n$$

$$Z \rightarrow \rho_p$$

$$\frac{N - Z}{A} \rightarrow \alpha = \frac{\rho_n - \rho_p}{\rho}$$

**THEN:**

$$\frac{E}{A} = e_0(\rho) + e_{sym}(\rho)\alpha^2$$

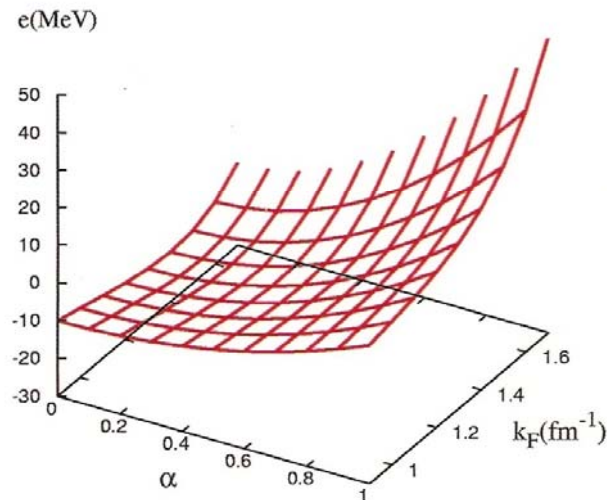
**Symmetry energy**

**This is consistent with the results of a proper (microscopic) calculation of the energy/particle in nuclear matter:**

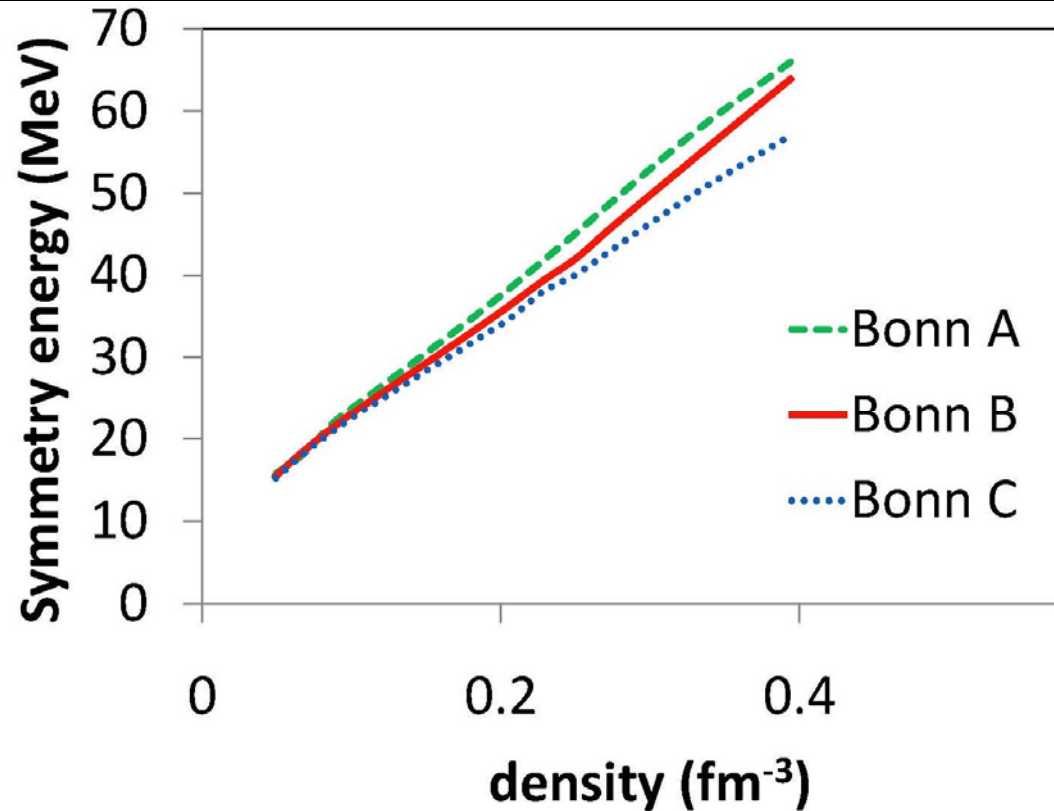
### THE ASYMMETRIC MATTER EOS

Energy/nucleon vs. density (or Fermi momentum) and the neutron excess parameter,  $\alpha$

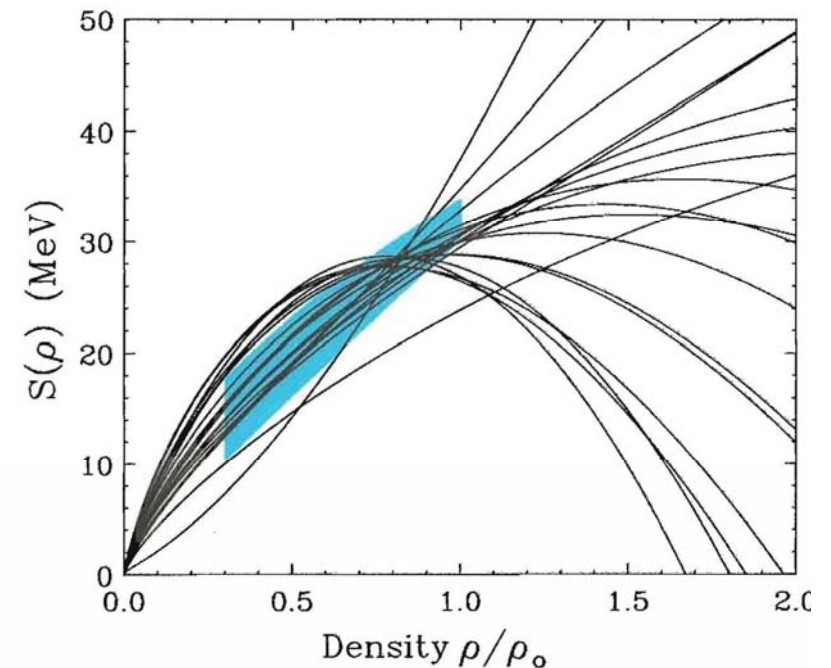
$$\rho = \rho_n + \rho_p \qquad \alpha = \frac{\rho_n - \rho_p}{\rho}$$



# The **symmetry energy** as predicted by three meson-theoretic NN potentials:



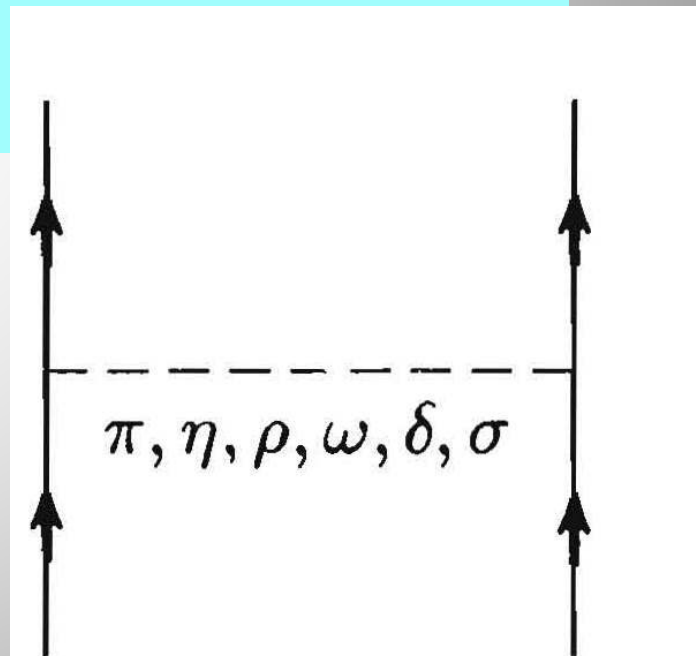
..and from various parameterizations of the Skyrme model:



In any **fundamental theory of nuclear forces**, the **pion** is the most important ingredient (crucial for **NN scattering data or the deuteron!**), followed by heavier mesons.

As demonstrated in F.S., PRC84, 044307 (2011), the pion gives the main contribution to the symmetry energy.

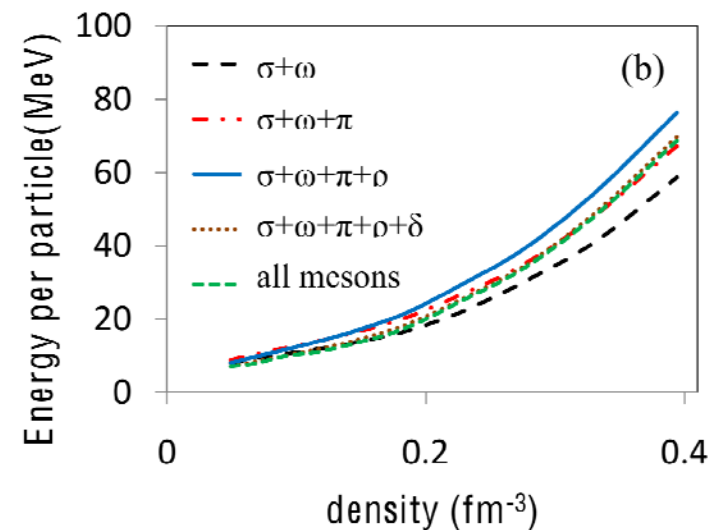
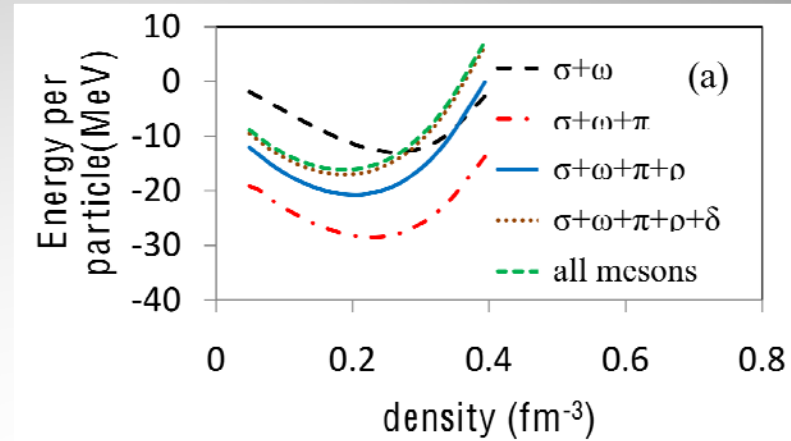
**Tensor force at short range: requires a proper description of the rho-meson, with both its vector and tensor coupling to the nucleon.**



# The role of the tensor force in nuclear matter as a powerful saturation mechanism is well known:

$$G = V + V \frac{Q}{E - E_0} G$$

$$G \approx V_C -$$



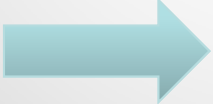
**A discussion on tensor force effects that does not start from a microscopic foundation is, to a large extent, arbitrary.**

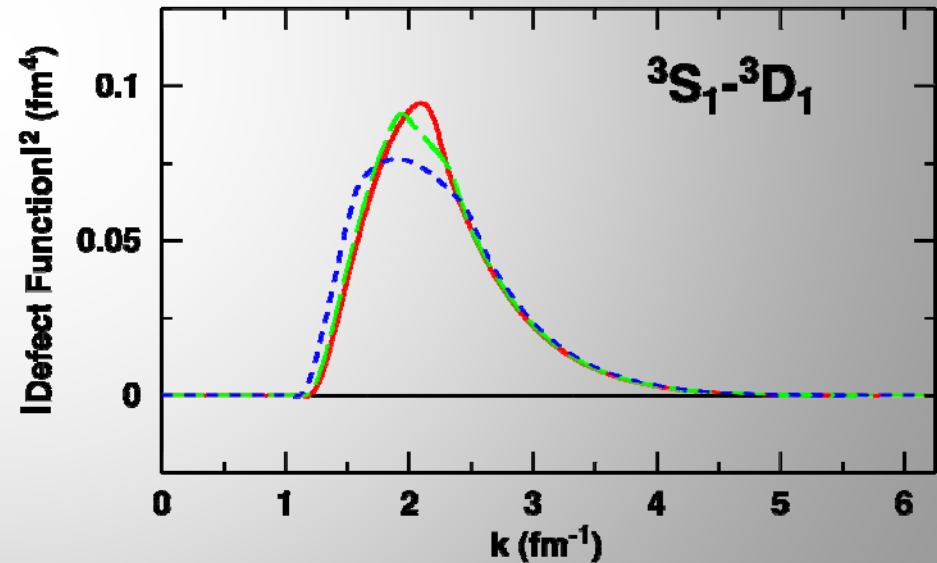
Tensor SRC can be investigated through the correlated wave function in the  $^3S_1$ - $^3D_1$  channel:

$$G\phi = V\psi$$

$$\psi = \phi + \frac{Q}{E - E_0}G\phi$$

$\psi - \phi$  is the defect function.

**Defect function** vs. momentum near saturation density at three levels of isospin asymmetry (DBHF predictions) 



A study of SRC including modern 2- and 3-body chiral interactions is coming soon.

**Key to improved understanding of the many-body system:**

**Comparative studies with ab initio approaches.**

**Recent calculations with consistent chiral 2BF and 3BF:**

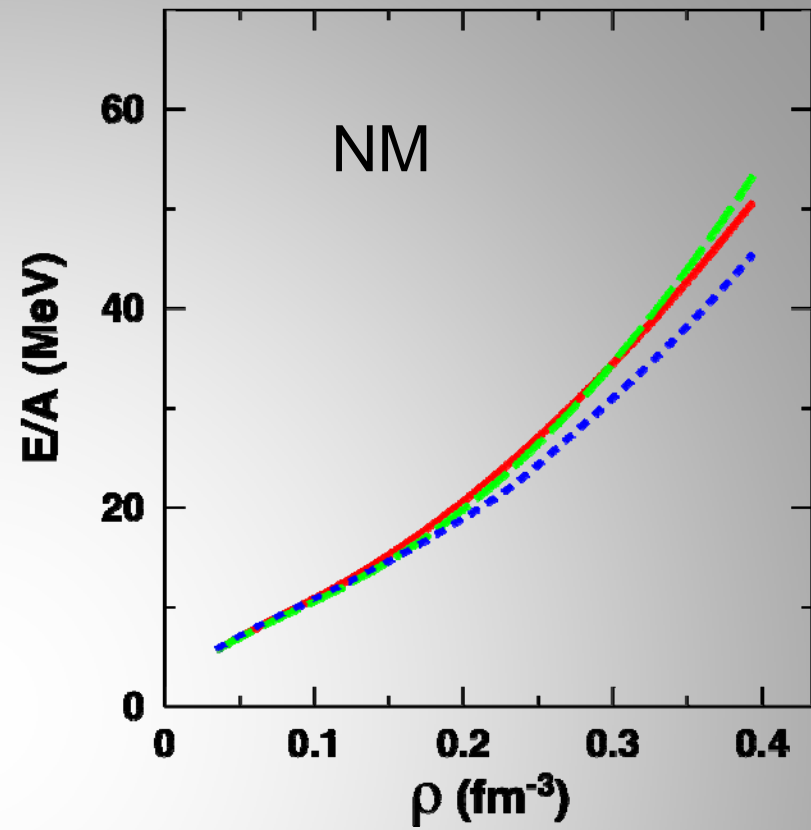
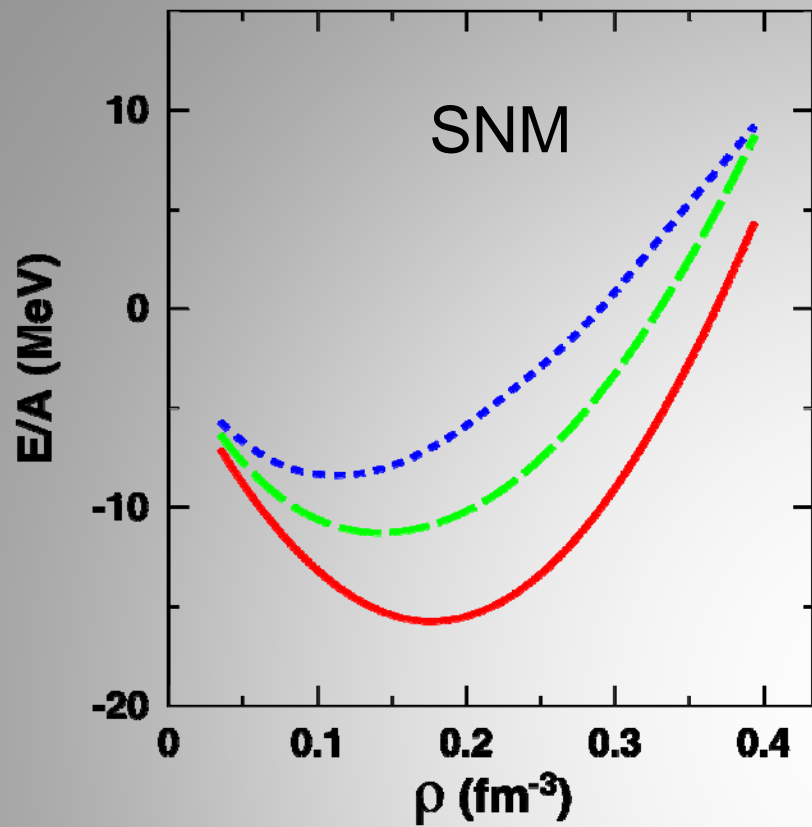
**(with L. Coraggio, N. Itaco, L.E. Marcucci, J. Holt, R. Machleidt)**

**2BF constrained by the NN system**

**3BF constrained by the A=3 system**

**Predictions at N3LO of the chiral 2BF, varying the cutoff in the regulator function applied to the chiral NN potential.**

$$f(p, p') = e^{[-(\frac{p}{\Lambda})^{2n} - (\frac{p'}{\Lambda})^{2n}]}$$



Red: 450 MeV

Green: 500 MeV

Blue: 600 MeV



## Preliminary conclusions:

Realistic saturation properties can be obtained with consistent 2BF and 3BF in a parameter-free calculation. Not a trivial task!

A systematic analysis of order-by-order convergence is in progress in our group.

Improved cutoff independence with increasing order is crucial for the success of EFT.

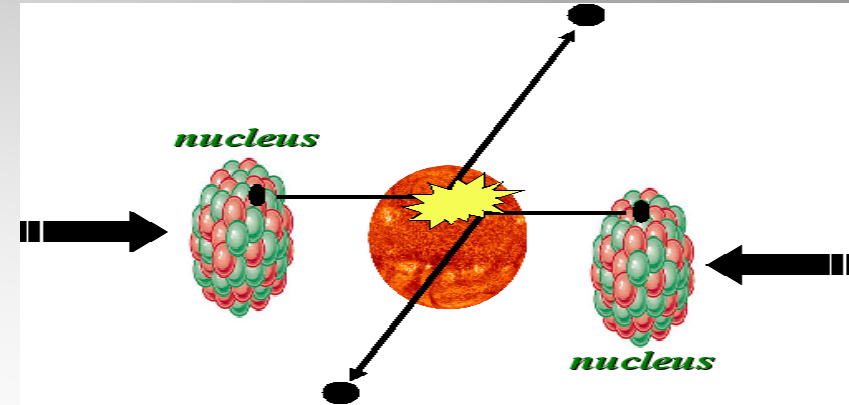
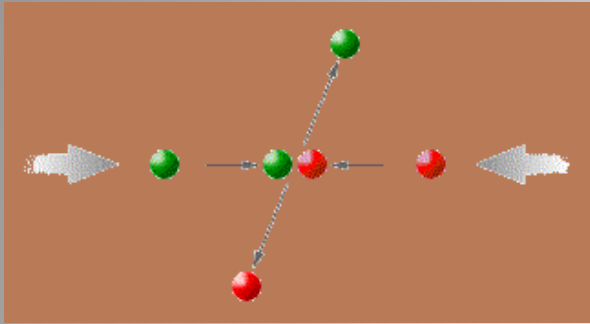
**Applications of nuclear forces  
in the medium include:**

**Nuclear/neutron matter  
(considered so far)**

**Reactions**

**Structure of nuclei**

## Our link with reactions: In-medium NN collision



Transport models of HI collisions are sensitive to both NN collisions and the average nuclear matter potential.

NN collisions are described by NN effective xsections.  
Our in-medium NN xsections are microscopic  
(i.e. driven by the NN scattering amplitudes.)

Using microscopic input has the advantage that different ingredients are internally consistent, as they all originate from the NN scattering amplitudes in the medium.

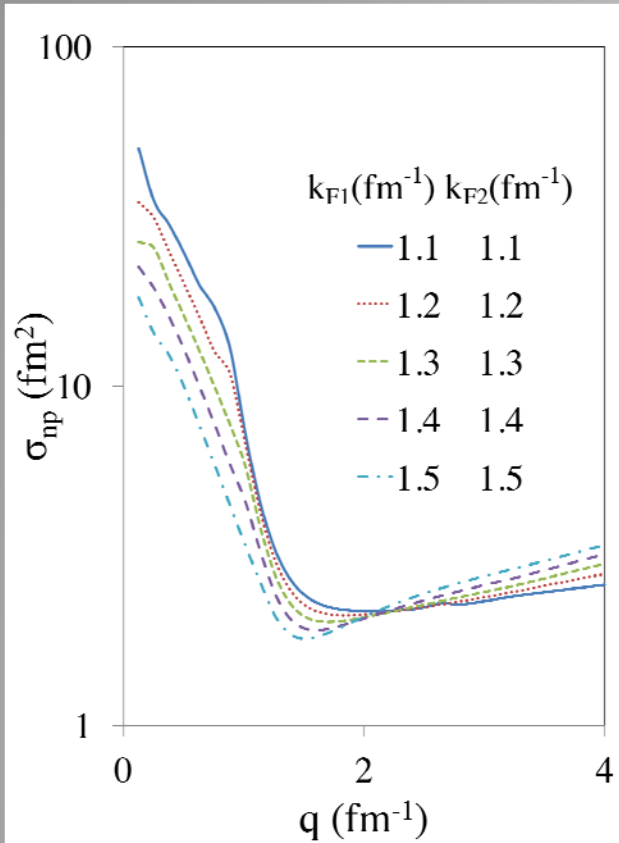
**Single-nucleon knockout reactions  
at intermediate energies involving  
unstable beams:**



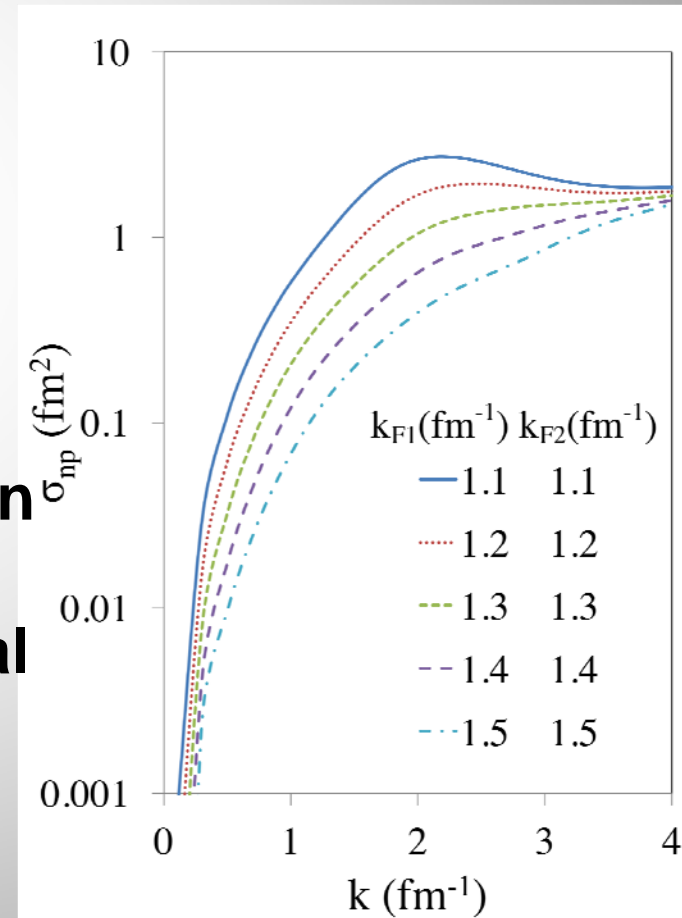
**(A very sensitive tool to study s.p. occupancies  
in the shell model through measurements of  
the momentum distribution.)**

**In the Glauber model, NN scattering amplitudes enter  
through the eikonal phase as effective scattering cross  
sections.**

# Microscopic in-medium NN cross sections as from DBHF G-matrix calculations.



**Average in-medium NN cross section for collision of two Fermi spheres, including Pauli restriction of the final scattering states.**



## Summary and Conclusions:

We reviewed some aspects of our previous work with IANM and the symmetry energy.

We reported on work in progress to explore SRC with modern interactions.

We reported on on-going investigations of order-by-order convergence of SNM and NM predictions with chiral two- and three-body forces.

Link with reactions: in the description of in-medium NN collisions. Effective NN xsections can be very model-dependent.

**Suggestion**: utilize reactions suitable as clean probes of the NN collision input.

**In all of the above, we stressed the importance of the ab initio approach.**